VITEEE 2021 Question Paper

Vellore Institute of Technology Engineering Entrance Examination

SOLVED PAPER (VITE EE nĀnĆ)

GENERAL INSTRUCTIONS

This question paper contains total 80 questions divided into four parts :

Part I: Physics Q. No - 1 to 25

Part II: Chemistry Q. No - 26 to 50

Part III: Mathematics Q. No - 51 to 75

Part IV: English & Logical reasoning Q. No - 76 to 80

. All questions are multiple choice questions with four options, only one of them is correct.

5.

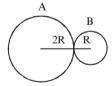
- For each correct response, the candidate will get 1 mark.
- There is no negative marking for the wrong answer.
- . The test is of 1½ hours duration.

PART - I (PHYSICS)

- 1. The distance of the centres of moon and earth is D. The mass of earth is 81 times the mass of the moon. At what distance from the centre of the earth, the gravitational force will be zero?
 - force **D**yill be a
- (b) $\frac{2D}{3}$ 9D
- (c) 4D
- (d) 10
- 2. Two wires A and B are of the same material. Their lengths are in the ratio of 1:2 and the diameter are in the ratio 2:1. If they are pulled by the 6. same force, then increase in length will be in the ratio of
 - (a) 2:1
- (b) 1:4
- (c) 1:8
- (d) 8:1
- 3. If x = at + bt2, where x is the distance travelled by the body in kilometers while t is the time in seconds, then the unit of b is
 - (a) km/s
- (b) kms
- (c) km/s2
- (d) kms2
- 4. A soap bubble of radius is placed on another soap bubble of mastiparating the two bubbles is

- (a) $r2 + r_2$
- (b) $\frac{\mathbf{r}^2 \mathbf{r}^1}{\mathbf{r}_1 \mathbf{r}_2}$
- $(c) \quad \frac{r_1 r_2}{r_2 r_1}$
- (d) $\sqrt{r_1^2 + r_2^2}$
- A charge q is moving with a velocity v parallel to a magnetic field B. Force on the charge due to magnetic field is
- (a) q v B
- (b) q B/v
- (c) zero
- (d) B v/q

Two spheres A and B of masses m and 2m and radii 2R and R respectively are placed in contact as shown. The COM of the system lies



- (a) inside A inside B at
- (b) the point of contact
- (c) None of these
- (d)

- Identify the correct statement.
 - (a) Static friction depends on the area of
 - (b) Kinetic friction depends on the area of
 - Coefficient of kinetic friction is more than the coefficient of static friction
 - (d) Coefficient of kinetic friction is less than the coefficient of static friction
- The distance travelled by a particle starting from 8.

rest and moving with an accelerations-2, in the third second is:

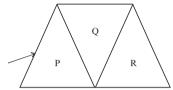
- (a) 6 m
- (b) 4 m
- (c)
- (d) $\frac{19}{3}$ m
- Photoelectric work function of a metal is 1eV. Light of wavelength l = 3000 Å falls on it. The photo electrons come out with a maximum velocity of:
 - (a) 10 metres/sec
- (b) 102 metres/sec
- (c) 104 metres/sec
- (d) 106 metres/sec
- 10. The coefficient of apparent expansion of merculty. in a glass vessel is 153×10 –6/°C and in a steel vessel is $144 \times 10-6$ °C. If a for steel is $12 \times 10-$ 6/°C, then that of glass is
 - (a) $9 \times 10-6/^{\circ}C$
- (b) $6 \times 10 6^{\circ}$ C
- (c) $36 \times 10 6$ °C
- (d) $27 \times 10-6$ °C
- 11. A step-up transformer operates on a 230 V line and supplies a load of 2 ampere. The ratio of the primary and secondary windings is 1:25. The current in the primary is
 - (a) 15 A
- (b) 50 A
- (c) 25 A
- (d) 12.5 A
- 12. Two bodies of same mass are projected with the 7 same velocity at an angle 30° and 60° respectively. The ratio of their horizontal ranges will be
 - (a 1:
- 1:2
-) 2: $\sqrt{2}$
- Two point charges $+3\mu$ C and $+8\mu$ C repel each other with a force of 40N. If a charge of -5μ C is added to each of them,)then the force between them will become
 - (a) -10N
- (b) +10N
- (c) +20N
- (d) -20N

- 14. A sphere rolls down on an inclined plane of inclination q. What is the acceleration as the sphere reaches the bottom?

 - (a) $\frac{5}{7}$ gsin q (b) $\frac{3}{5}$ gsin q
 - (c) $\frac{2}{7}g\sin q$ (d) $\frac{2}{5}g\sin q$

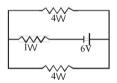
15.

A given ray of light suffers minimum deviation in an equilateral prism P. Additional prisms Q and R of identical shape and of same material as that of P are now combined as shown in figure. The ray will now suffer



- (a) greater deviation
- (b) no deviation
- same deviation as before
- (d) total internal reflection

The current in the 1W resistor shown in the circuit is



- 3 A
- (c) 6 A

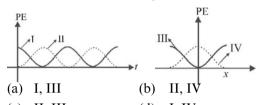
The root mean square velocity of hydrogen molecules at 300 K is 1930 metre/sec. Then the r.m.s velocity of oxygen molecules at 1200 K will

- (a) 482.5 metre/sec
- 965 metre/sec (b)
- (c) 1930 metre/sec Lenz's law gives
- (d) 3860 metre/sec
- (a) the magnitude of the induced e.m.f.
- (b) the direction of the induced current
- (c) both the magnitude and direction of the induced current
- (d) the magnitude of the induced current

19. A parallel plate capacitor with air between 25. A source producing sound of frequency 170 the plates has a capacitance of 8 pF. Calculate the capacitance if the distance between the plates is reduced by half and the space between them is filled with a substance of dielectric constant. (k = 6) (a)

(c) 72 81 рF рF

20. For 84 particle executing 6 S.H.M. the displacement x is given by $pF = A \cos wt$. Identify the graph which represents the variation of potential energy (P.E.) as a function of time t and displacement x.



(d) I, IV A radioactive sample contains 10–3 kg each of two nuclear species A and B with half-life 4 da 27. and 8 days respectively. The ratio of the amounts of A and B after a period of 16 days is

(a) 1:2

(b) 4:1

(c) 1:4

(d) 2:1

22. A string of 7 m length has a mass of 0.035 kg. If tension in the string is 60.5 N, then speed of a wave on the string is

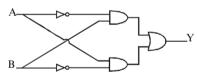
(a) 77 m/s

(b) 102 m/s

(c) 110 m/s

(d) 165 m/s

23. The following circut represents



OR gate

(b AND gate

NAND gate

None of these

As straight section PO of a circuit lies along the

and carries a steady current i. The magnetic field due to the section PQ at a point X = +a will be

(a) proportional to a

(b) proportional to a2

(c) proportional to 1/a

(d) zero

Hz is approaching a stationary observer with a velocity 17 ms-1. The apparent change in the wavelength of sound heard by the observer is (speed of sound in air = 340

ms-1) (a) 0.1 m

(b) 0.2 m

(c) 0.4 m

(d) $0.5 \, \text{m}$

PART - II (CHEMISTRY)

Consider the following reactions: NaCl + **\(\mathbb{R}\)**Cr2O7 + H2SO4 (Conc.)

(R) + Side products

(A) + NaOH ® (B) + Side products

(B) + H2SO4 (dilute) + H2O2

® (C) + Side products

The sum of the total number of atoms in one molecule each of (A), (B) and (C) is .

(a) 18

(b) 15

(d) 20 (c) 21

Xenon hexafluoride on partial hydrolysis produces compounds 'X' and 'Y'. Compounds 'X', 'Y' and the oxidation state of Xe are respectively:

(a) XeOF 4(+6) and XeO3(+6)

(b) XeO 2(+4) and XeO3(+6)

(c) XeOF 4(+6) and XeO2F2(+6)

(d) XeO 2F2(+6) and XeO2(+4)

The edge length of unit cell of a metal having molecular weight 75 g/mol is 5Å which crystallizes in cubic lattice. If the density is 2g/cc then find the radius of meta = a o the 23. Give the answer in pm.

N 217 (b 210

(a pm pm

29. Consider the following (state 205 nts:

- because in concentration of reactant
- increases the rate of a zero order reaction.

(d

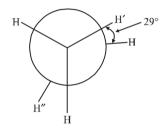
- II. Rate constant k is equal to collision frequency A if Ea = 0.
- III. Rate constant k is equal to collision frequency A if $\mathbb{R}^a = \mathbb{Y}$.
- IV. In k vs T is a straight line.
- V. In k vs 1/T is a straight line.

Correct statements are

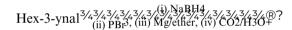
(a I and IV (b II and V III and IV II and III))

(c

- 30. To deposit 0.634 g of copper by electrolysis 35. of aqueous cupric sulphate solution, the amount of electricity required (in coulombs)
 - (%) 1930
- (b) 3960
- (c) 4825
- (d) 9650
- 31. In the following skew conformation of ethane, $H\not c - C - C - H dihedral angle is :$



- (a) 58o
- (b) 149o
- (c) 151o
- (d) 120o
- 32. What is the product of following reaction?



- (c)
- 33. In the following sequence of reactions,

CH3CH2OH³/₄P³/₄+I³/₄2®A³/₄3/₄Mg³/₄®B³/₄H³/₄C³/₄HO³/₄® (b) The equilibrium will shift in fo

C³/4 ½ 3/4 **D**³/4®

the compound D is

(ba)tapadpanal

- (b)
- reproportate all and hol (d)
- 34. Which of the following reactions can produce aniline as main product?

 - (c)
 - (d)

- Secondary structure of protein refers to
 - (a) mainly denatured proteins and structure of
 - prosthetic groups (b) three -dimensional structure, especially the bond between amino acid residues that are distinct from each other in the polypeptide chain
 - (c) linear sequence of amino acid residues in the polypetide chain
 - regular folding patterns of continous portions of the polypeptide chain
- The increasing order for the values of e/m (charge/mass) is
 - (a) e, p, n, a
- (b) n, p, e, a
- (c) n, p, a, e
- (d) n, a, p, e
- 37. In which of the following pairs both the ions are coloured in aqueous solutions?
 - (a) Sc3+, Ti3+
- (b) Sc3+, Co2+
- (c) Ni2+, Cu+
- (d) Ni2+, Ti3+
- 38. The total number of possible isomers for squareplanar [Pt(Cl)(NO)(\(\Delta\)3)(SCN\)†is:
 - (a) 16
- (b) 12
- (c) 8
- (d) 24
- 39. For the reaction,

 $2SO(g) + O_2(g)$ 2 SO3(g),

 $DH = -57.2 \text{ kJ mol} - 1 \text{ and } K = 1.7 \times 1016$

Which of the following statement is **INCORRECT?**

- (a) The equilibrium constant is large suggestive of reaction going to completion
- The equilibrium will shift in forward direction as the pressure increases.
- The equilibrium constant decreases as the temperature increases.
- (d) The addition of inert gas at constant volume will not affect the equilibrium constant.
- The half-life of a reaction is inversely proportional to the square of the initial concentration of the reactant. Then the order of the reaction is
 - (a) 0
- (b) 1
- (c) 2
- (d) 3

41. A galvanic cell is set up from electrodes A and **B4**.

ElectrodeA:
$$\frac{\text{CrO2}}{2}_{7}$$
 /Cr³⁺, Ered = + 1.33 V

Electrode B: Fe3+/Fe2+, oEed = 0.77 V

Which of the following statements is false?

- (a) Standard e.m.f of the cell is 0.56 V
- (b) (C) (add)ent will flow from electrode A to B in
- Ketothenekteantal reiecisin is observed in: A will act as cathode and have positive polarity

None of these

42.

(c)
$$HC_{6}C-H$$

- (d) Both (a) and (b)
- 43. In a set of reactions, ethylbenzene yield a product D.

Identify D:

What will be the final product in the following reaction sequence –

 $CH_{3} {\overset{CHCN}{\overset{3}{\cancel{4}}}}\overset{3}{\cancel{4}}\overset{3}{\cancel{4}}\overset{H}\overset{+}{\cancel{4}}\overset{+}{\cancel{4}}}\overset{H}{\cancel{2}}\overset{2}{\cancel{4}}O \text{ (BA 3/4 3)}\overset{3}{\cancel{4}}\overset{H}{\cancel{4}}\overset{1}{\cancel{4}}\overset{3}{\cancel{4}}\overset{3}{\cancel{4}}\overset{3}{\cancel{4}}\overset{1}{\cancel{4}}\overset{2}{\cancel{4}}\overset{1}{\cancel{4}}\overset{1}{\cancel{4}}\overset{2}{\cancel{4}}\overset{1}{$

- (a) CH 3 CH2 CONH2 (b) CH 3 CH2 CH2 NH2
- (c) CH
- (d) CH
- 45. In a set of reactions acetic acid yielded a product

3/4 H3/4C N3/4B/4H3/4O3/4H/B

The structure of (D) would be -

- In fructose, the possible optical isomers are
 - (a) 12
- (b) 8
- (c) 16
- (d) 4
- The position of both, an electron and a helium atom is known within 1.0 nm. Further the momentum of the electron is known within 5.0 × 10–26 kg ms–1. The minimum uncertainty in the measurement of the momentum of the helium atom is
 - (a) 50 kg ms-1
- (b) $80 \text{ kg ms}{-1}$
- (c) $8.0 \times 10-26 \text{ kg ms}-1$ (d) $5.0 \times 10-26 \text{ kg ms}-1$

48. The value of log K for a reaction A

(Given: $D^{H298K} = -54.07 \text{ kJ mol-1},$

 $DrS^{\circ}_{298K} = 10 \text{ JK-1mol-and } R = 8.314 \text{ JK-1}$

mol-1;

- $2.303 \times 8.314 \times 298 = 5705$
- (a) 5
- (b) 10
- (c) 95
- (d) 100
- 49. If $C(s) + Q(g) \frac{3}{4} \frac{3}{4} \otimes CO2(g)$; DH=R and

$$CO(g) + \frac{1}{2}O2(g)^{3}/_{4}^{3}/_{4} CO2(g); DH = S,$$

then heat of formation of CO is:

- (a) R + S
- (b) R-S
- (c) $R \times S$
- (d) S-R
- 50. Which of the following compounds does not follow Markownikoff's law?
 - (a) CH 36H = 6H2H36

PART - III (MATHEMATICS)

- 51. The value of c in Rolle's Theorem for the function $f(x) = ex \sin x$, $x \hat{I} [0, p]$ is

- 52. The equations 2x + 3y + 4 = 0; 3x + 4y + 6 = 0 and $(c) \sim q \triangleright p$ 4x + 5y + 8 = 0 are
 - (a) consistent with unique solution
 - (b) inconsistent
 - (c) consistent with infinitely many solutions
 - (d) None of the above
- 53. The shortest distance between the lines x = y + 2 = 6z - 6 and x + 1 = 2y = -12z is
- (c) 1
- 54. If the tangent at P(1, 1) on y2 = x(2-x)2 meets the curve again at Q, then Q is
 - (a) (2, 2)
- (b) (-1, -2)
- (d) None of these

- 55. If $f(x)=x + \frac{x}{1+x} + \frac{x}{(1+x)^2} + ... \text{ to } Y$, then at x = 0, f(x)
 - (a) has no limit
 - (b) is discontinuous
 - (c) is continuous but not differentiable
 - (d) is differentiable
- 56. Radius of the circle (x + 5)2 + (y 3)2 = 36 is
 - (a) 2
- (b) 3
- (c) 6
- (d) 5
- 57. If $a = 2i^2 2j^2 + k^2$ and $c = -i^2 + 2k^2$ then |c|.

 \vec{a} is equal to :

- (a) $2\sqrt{5}i^+ 25\sqrt{5} + 5\sqrt{5}$
- (b) $25\hat{i} 25\hat{j} + 5\hat{k}$
- (c) $\sqrt{5}i^{+} 5j^{+} 5k^{-}$
- (d) $\sqrt{5}i^+2\sqrt{5}j^++5k^-$
- If (-4, 5) is one vertex and 7x y + 8 = 0 is one diagonal of a square, then the equation of second diagonal is
- (a) x + 3y = 21
- (b) 2x 3y = 7
- (c) x + 7y = 31
- (d) 2x + 3y = 21
- 59. p p q can also be written as
 - (a)p $\dot{\mathbf{p}} \sim \mathbf{q}$
- (b) ~pÚq
- (d) None of these

60. Let
$$\partial \frac{x^{1/2}}{\sqrt{1-x^3}} dx = \frac{2}{3} \operatorname{gof}(x) + C$$
, then

- (a) $f(x) = \sqrt{x}$
- (b) f(x) = x3/2 and $g(x) = \sin(-1x)$
- (c) f(x) = x2/3
- (d) None of these
- 61. Which one of the following is an infinite set?
 - (a) The set of human beings on the earth
 - (b) The set of water drops in a glass of water
 - (c) The set of trees in a forest
 - (d) The set of all primes

The domain of the function

$$\sqrt{x^2-5x+6} + \sqrt{2x+8-x2} \text{ is}$$
(a) [2, 3] (b) [-2, 4] (c) [-2, 2] È [3, 4] (d) [-2, 1] È [2, 4]

63.	Area bounded by the curve $y = log x$ and the 70.
	coordinate axes is

(d)
$$2\sqrt{2}$$

64. The angle of intersection to the curve
$$y = x^2$$
, $6y = 7 - x^3$ at $(1, 1)$ is:

(a)
$$\frac{p}{2}$$

(b)
$$\frac{p}{4}$$

(c)
$$\frac{p}{3}$$

65. Angle formed by the positive Y-axis and the

tangent to y=x
2
 +4x-17 at c $\stackrel{\text{æ5}}{\rightleftharpoons} \frac{-3\ddot{0}}{2}$, $\stackrel{\text{-4o}}{\rightleftharpoons} \text{is}$

(a)
$$\tan^{-1} 9$$
 (b) $p - \tan^{-1} 9$

(c)
$$\frac{9}{2} + \tan^{-1} 9$$
 (d) -

66. The value of
$$(1 + i)4 \stackrel{\text{de}}{\underset{e}{\stackrel{}{=}}} + \frac{1}{i} \stackrel{\text{d}}{\underset{e}{\stackrel{}{=}}} is$$

67. (c) 8 (d) 16
The relation R defined on the set A =
$$\{1, 2, 3, 73, 4, 5\}$$
 by R = $\{(x, y) : |x2 - y2| < 16\}$ is given by

(a)
$$\{(1, 1), (2, 1), (3, 1), (4, 1), (2, 3)\}$$

(c)
$$\{(3,3),(4,3),(5,4),(3,4)\}$$

68.
$$\partial \frac{2dx}{(e^x + e^{-x})^2} =$$

(a)
$$\frac{-e^{-x}}{(e^{x} + e^{-x})} + C$$
 (b) $\frac{-1}{(e^{x} + e^{-x})} + C$

69. The value of
$$tan-1(1) + tan-1(0) + tan-1(2)$$

(b)
$$\frac{51}{4}$$

$$(c)$$
 $-$

In a culture the bacteria count is 1,00,000. The number is increased by 10% in 2 hours. In how many hours will the count reach 2,00,000 if the rate of growth of bacteria is proportional to the number present.

(a)
$$\frac{2}{\log_{10}^{11}}$$

(a)
$$\frac{2}{\log_{10}^{11}}$$
 (b) $\frac{2 \log 2}{\log_{\bullet} \div}$

(c)
$$\frac{\log 2}{\log 1}$$

$$(d) \quad \frac{\log 2}{\log \underbrace{\text{ello}}_{\dot{e}}}$$

71. What is the angle between the two straight lines

$$y = (2 - \sqrt{3})x + 5$$
 and $y = (2 + \sqrt{3})x - 7$?

72. If the angle qbetween the line
$$\frac{x+1}{1} = \frac{y-1}{2}$$

= $\frac{z-2}{2}$ and the plane $2x - y + \sqrt{1z} + 4 = 0$ is

such that $\sin q = \frac{1}{3}$ then the value of 1 is

(a)
$$\frac{5}{3}$$

(b)
$$\frac{-3}{5}$$

(d)
$$\frac{-4}{3}$$

The distance of the point (-5, -5, -10) from the point of intersection of the line $r = 2i^{-}j^{+}+2k^{+}+1(3i^{+}+4j^{+}+2k^{-})$ and the plane

$$r(i\hat{j}+k^{\hat{}})=5 is$$

(c)
$$4\sqrt{15}$$

(d)
$$10\sqrt{2}$$

74.
$$Q_{\log \sqrt{p/2}}^{\log \sqrt{p}} e^{2x \sec 2} e^{2x} e^{2x} Q_{\emptyset}^{\underline{p}} dx$$
 is equal to :

(a)
$$\sqrt{3}$$

(b)
$$\frac{1}{\sqrt{3}}$$

(c)
$$\frac{3\sqrt{3}}{2}$$

(c)
$$\frac{3\sqrt{3}}{2}$$
 (d) $\frac{1}{2\sqrt{5}}$

75. If
$$\frac{|x+3|+x}{x+2} > 1$$
, then xî

(a)
$$(-5, -2)$$

(b)
$$(-1, Y)$$

(c)
$$(-5, -2) \stackrel{.}{E} (-1, \frac{1}{4})$$
 (d) None of these

PART - IV (ENGLISH & LOGICAL REASIO NING)

Directions (76-78): Study the paragraph and answer the questions that follow.

A training calendar and schedule for Fire Agency Specialties Team (F.A.S.T.) membership is available in this office to all applicants for F.A.S.T. membership. Training will take place the third week of each month. Classes will be taught on Monday afternoons, Wednesday evenings, and Saturday afternoons. So that the F.A.S.T. can maintain a high level of efficiency and preparedness for emergency response situations, its members must meet certain requirements.

Fourst, oibe condeide for

membership on F.A.S.T., your department must be a member of the F.A.S.T. organization, and you must have written permission from your fire chief or your department's highest ranking administrator.

Once active, you must meet further requirements to maintain active status. These include completion of technician-level training and certification hazardous material (hazmat) operations. In addition, after becoming a member, you must also attend a minimum of 50% of all drills conducted by F.A.S.T. and go to at least one F.A.S.T. conference. You may qualify for alternative credit for drills by proving previous experience in actual hazmat emergency response.

If you fail to meet minimum requirements, you will be considered inactive, and the director of your team will be notified. You will be placed back on active status only after you complete the training necessary to meet the minimum requirements.

- 76. Potential F.A.S.T. members can attend less than half of F.A.S.T. drills if they
 - (a) complete technician-level training requirements.
 - (b) indicate prior real emergency experience.
 - (c) receive permission from their fire chief.
 - (d) enroll in three weekly training sessions.

- 7. Which of the following is the main subject of the passage?
 - (a) preparing for hazmat certification
 - (b) the main goal of F.A.S.T.
 - (c) completing F.A.S.T. membership
 - (d) r equirements

learning about your department's F.A.S.T. membership

Applicants must be available for training

- (a) three days each month.
- (b) three days each week.
- (c) every third month.
- (d) for 50% of classes.

Jatin starting from a fixed point, goes 15 m towards North and then after turning to his right, he goes 15 m. Then, he goes 10 m, 15 m and 15 m after turning to his left each time. How far is he from his starting point?

- (a) 15 m
- (b) 5m
- (c) 10 m
- (d) 20 m

Examine the following statements: All members of Mohan's family are **h** on est.

Some members of Mohan's family are not employed.

Some employed persons are not honest. Some honest persons are not employed. Which one of the following inferences can be drawn from the above statements?

- (a) All members of Mohan's family are employed
- (b)The employed members of Mohan's family are honest
- (c) The honest members of Mohan's family are not employed
- (d)The employed member of Mohan's family are not honest

SOLUTION S

PART - I (PHYSICS)

1. (d)
$$\frac{Gme}{x^2} = \frac{Gmm}{(D-x)^2}$$
or
$$\frac{G(8 \text{ lm})}{x^2} = \frac{m}{(D-x)^2}$$

$$x = \frac{9D}{10}$$

2. (c) We know that Young's modulus

$$Y = \frac{F}{pr^2} \cdot \frac{L}{l}$$

Since Y, F are same for both the wires, we h ave,

$$\frac{1 \text{ L1}}{\frac{r^{2} \ln 1}{r^{2} \ln 1}} = \frac{1 \text{ L}_{2}}{\frac{r^{2} \ln 2}{r^{2}}} \quad \text{or, } \quad \frac{\ln 1}{12} = \frac{\frac{r^{2} \ln 1}{r^{2} \ln 2}}{\frac{r^{2} \ln 1}{r^{2} \ln 2}} = \frac{(D - \frac{2}{r^{2} \ln 2})}{(D - \frac{1}{2})^{2} \ln 2}$$

or,
$$\frac{11}{1} = \frac{D2 \cdot L_1}{12 = 1.8} = \frac{D2}{(2D)^2} \cdot \frac{L_2}{2L_2} = \frac{1}{8}$$
 11.

So, | (a)
$$(c \quad [x] = [bt2]$$
. Hence $[b] = [x/t2] = km/s2$.

4 (c 14. (c)

And I m2

$$\begin{array}{ccc}
 & \text{And, } \frac{r_1}{r_2} = \frac{m_2}{m_1} \\
6 & (c & r_2 = \frac{m_2}{m_1}
\end{array}$$

7 (d rk < ms coefficient of static friction is always greater than kinetic friction.

.) Distance travelled in the nth second is

8 (c given by
$$dn = u + \frac{3}{2}(2n-1)$$

put u = 0, a=3ms-2, n = 3

$$4 (2 \times 3 - 1) = 4 (5 = 3 - 1)$$

$$d = 0 + \frac{4}{3 \cdot 2} (5 = \frac{10}{3} - 1)$$

9. (d)
$$hn = W + \frac{1}{2}mv^2 or \qquad \frac{hc}{+} = W + \frac{1}{2}mv^2$$

Here $l = 3000 \text{ Å} = 3000 \times 10 - 10 \text{ m}$
and $W = 1 \text{ eV} = 1.6 \times 10 - 19 \text{ joule}$

$$= \frac{(6.6 \cdot 10^{-34})(3'108)}{3000'10^{-10}}$$
$$= \frac{(1.6' \cdot 10^{19}) + \frac{1}{2}'(9.1'10^{-31})v2}{(9.1'10^{-31})v2}$$

Solving we get, v @ 106 m/s

10. (a) $g_{real} = g_{app.} + g_{vessel}$ So $(gapp. g_{vessel})_{glass} = (g_{app} + g_{vessel})_{steel}$

$$P 153'10- {}^{6} + (gvessel)glass$$

= $144 10-6 + (g_{vessel})st eel$

Further,

(g vessost ee = 3a = 3 (12 10
$$^{-6}$$
)
= 36′10-6/°C

D 153 '10-6 + (gyessel)glass = 144 10-6 + 36'10-6

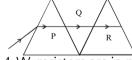
$$P(g \text{ vessel })glass 3a = \frac{27'10-6}{}$$

$$pa = 9 \frac{10-6}{°}$$

Horizontal range is same when angle of projection is q or $(90^{\circ} - q)$.

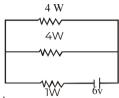
14. (a
$$a = \frac{g \sin q}{1 + \frac{K2}{R^2}} = \frac{g \sin q}{1 + \frac{2}{3}} = \frac{5}{7} g \sin q$$

When the ray suffers minimum deviation, it becomes parallel to the base of prism P. As prisms Q and R are of same material and have identical shape, therefore, the ray continues to be parallel to base of Q and R. Hence final deviation of the ray remains the same as before.



16. (d) Two 4 W resistors are in parallel combination. Their equivalent resistance

$$=\frac{4'4}{4+4}=\frac{16}{8}=2W$$



\ Total resistance of the network = 2 + 1 = 3W

\ Current through 1 Wesistor = $\frac{6}{3}$ = 2A

17. (b) Root-mean square-velocity is given by

$$vrms = \sqrt{\frac{3RT}{M}} \text{ i.e., } vrms\mu \sqrt{\frac{\ddot{\varphi}T\ddot{\varphi}}{\dot{\varphi}M\ddot{\varphi}}}$$

$$\frac{(v_{rms})O2}{(v_{rms})H_2} = \sqrt{\frac{\dot{e}T_{O2}}{\dot{e}T_{H2}}} \cdot \frac{H}{2} \cdot \frac{\dot{u}}{\dot{u}}$$

$$= \sqrt{\frac{\dot{e}}{\dot{e}} \frac{1200\ddot{\varphi}}{300}} \cdot \frac{\ddot{\varphi}Z\ddot{\varphi}\ddot{\varphi}\ddot{\varphi}}{\dot{e}^{32}\ddot{\varphi}\ddot{u}} = \frac{1}{2}^{2}$$

$$C$$

$$(v^{e} rms)O2 = (vrms)H2 \cdot \frac{1}{2} = \frac{1930}{2} = \frac{965 \text{ m/s}}{2}$$

- 18. (b Lenz's law helps to identify the direction of induced current.
- 19. Capacity of parallel plate capacitor

$$(d \quad C = \frac{ke_0A}{d}$$
 (For air kr = 1)

So,
$$\frac{e^{A}}{d} = 8 \cdot 10-12$$

If d ® $\frac{d}{2}$ and kr® 6 then new capacitance $C' = 6 \times \frac{\text{eOA}}{d/2} = 12 \frac{\text{eOA}}{d} = 12 \times 8 \text{ pF} = 96 \text{ pF}_{7.}$

- 20. (a) In x=Acoswt, the particle starts oscillating from extreme position. So at t = 0, its potential energy is maximum.
- 21. (c) Ratio of number of half life taken is given as:

After 16 days

$$n_{A1/2} = \frac{16}{4} = 4; n_{B1/2} = \frac{16}{8} = 2$$

$$N = N_0 \mathop{\text{def}}_{\sum 2\stackrel{\circ}{\phi}}^{\circ} p_{N_A}$$

$$= \frac{1}{2^4} : \frac{1}{2^2} = 22:24$$
$$= 4:16, = 1:4$$

22. (c) Given: Length (l) = 7 m

Mass (M) = 0.035 kg and tension (T) = 60.5

N. We know that mass of string per unit

length (m)

$$=\frac{0.035}{7}$$
 =0.005kg/m

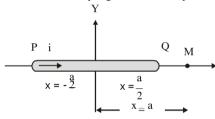
and speed of

$$wave = \sqrt{\frac{T}{m}} = \sqrt{\frac{60.5}{0.005}} = 110 \text{ m/s}.$$

23. (d) Output of upper AND gate = AB
Output of lower AND gate = AB
\Output of OR gate, Y=AB+BA-

This is boolean expression for XOR gate.

24. (d) Magnetic field at a point on the axis of a current carrying wire is always zero.



25. (a)
$$I = \frac{v}{n} = \frac{340}{170} = 2m, n' = \frac{340}{340-17}$$
 '170 $n' = 178.9 \text{Hz}$

Now
$$1' = \frac{v}{n'} = \frac{340}{178.9} = 1.9$$
 $0 = 1.9 = 0.1m$

PART - II (CHEMISTRY)

The sum of total no. of atoms in one molecules each of A, B & C = 5 + 7 + 6 = 18

27. (c)
$$XeF_6 + H2O^{3/4}/4pa^{3/4}rtia^{3/4}/60F_4 + 2HF$$

28. (a)
$$r = \frac{NAV}{NAV}$$

$$Z = \frac{r NAV}{M} = \frac{2.6 \cdot 1023'(5'10 - 8)3}{75}$$

$$Z = 2, \text{ which represents bcc structure}$$

\ r=
$$\frac{\sqrt{3}}{4}$$
a= $\frac{\sqrt{3}}{4}$ '5 = 2.165Å=216.5 pm »

217 pm

29. (b) According to Arrhenius equation, k = Ae - Ea/RT

\ when Ea = 0, k = A Also ln k vs 1/T is a straight line with slope = -Ea/R.

\ Statements (ii) and (v) are correct.

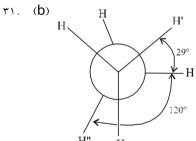
(a) In the electrolysis of cupric sulphate, the reaction that occurs at cathode is Cu2++2e-3/43/4®Cu

Thus 2F or 2×96500 C of electricity is required to deposit

= 1 mol of Cu = 63.5 g of CuIt means that to deposit 63.5 g of Cu, the amount of electricity required = $2 \times 96500 \text{ C}$ So, to deposit 0.634 g of Cu, the amount of

electricity required =
$$\frac{2^{96500}}{63.5} 0.634$$

» 1930 C



Angle between H' and H'' = $120^{\circ} + 29^{\circ} = 1360^{\circ}$ (d) 32.

33. (d) CH3CH2OH³/₄P³/₄+|³/₄P³/₆CH2I

CH2CH3 ³/₄H³/₄C³/₄H**Q**²C⁴**®**MgI Ή (C)

(d) Various products are formed when nitroarenes are reduced. These are given below for 66 H5 NO 2.

Medium Main product (6H5NH2) (d)In acidic medium Aniline (m et al /HCl) **NHOH**

(b)In neutral mediumPhenyl hydroxylamine, (Zn/NHC1)

(a) In alkaline medium NH_NF Hydrazobenzene

Thus, aniline will be main product in case of (d). (d

$$\frac{e}{m}$$
 for (i) neutron = $\frac{0}{1}$ = 0

(ii) a-particle $= \frac{2}{1} = 0.5$

35.

(iii) proton
$$= \frac{1}{1}$$

(iv) electron $= \frac{1}{1/1837} = 1837$

37. (d) $Sc3+(Z = 18): 1s2,s2p6 3s2p6d04s^0$; no unpaired electron. $Cu+(Z=28): 1s2,s2p6 3s2p6d 1@4s^0; no$ unpaired electron.

Ni2+ (Z = 26): 1s2, 2s2p6, 3s2p6d8, 4s0; unpaired electrons are present. Ti3+ (Z = 19): 1s2, 2s2p6, 3s2p6d1, 4s0; unpaired electron is present Co2+ (Z = 25): 1s2, 2s2p6, 3s2p6d7, 4s0; unpaired electrons are present So from the given options the only correct combination is Ni2+ and Ti3+.

38. (b) The square planar complex of the type [Mabcd]n \pm , where all four ligands are different, has 3 geometrical isomers. But if one of the ligands is ambidentate, then $2 \times 3 = 6$ geometrical isomers are possible. But if two ligands are ambidentate, then $4 \times 3 = 12$ geometrical isomers are possible.

In the given example, NO– and SCN– are

ambidentate ligands.

39. Aduilibrium constant has no relation with catalyst. Catalyst only affects the rate of the reaction.

Catalyst, V_2^{O} in the given reaction, is used to speed up the reaction.

40. (d) $t1/2\mu \frac{1}{a2}$

We know that $1/2\mu \frac{1}{a^{n-1}}$

i.e. n = 3

Thus reaction is of 3rd order.

- 41. (d)
- 42. (d) Keto-enol tautomerism is shown by carbonyl compounds having a-hydrogen atom.
- 44. (c) CH₂CN³/₄H₄,3/₄A³/₄O®CH3CHCOOH₂/₄N³/₄H³/₄3®

keto form

(b)

O
OH
H5C6 - C - CH 3 6 C H5 - C = CH2
keto form enolform

(c) C₆ H5 - - noa-HactomH

CH2 - CH3

COOH COOC2H5

3/43/4Br3/42Br3/450HB

Br

Br

CH3CH CONH2³4H³4of³4fma³4nb³4rom³6**i**d³6**rf**2¹4**af**2ⁱ4on³4® NaOBr (C)

COOH

(b) Fructose has 3 chiral centres and hence number of optical isomers are 23 = 8

47. (d) By Heisenberg uncertainty Principle $Dx'Dp = \frac{h}{4p}$ (which is constant)

As Dx for electron and helium atom is same thus momentum of electron and helium will also be same therefore the momentum of helium atom 33. equal to $5 \times 10-26$ kg. m.s-1.

48. (b)A $DG^{\circ} = DH^{\circ} - TDS^{\circ}$ $DG^{\circ} = -2.303 \text{ RTlpg K}$ -2.303 RT log0 K €H° - TS° $2.303 \text{ RT log0 K} = \square \text{TS}^{\circ} - \square \text{H}^{\circ}$

$$log_{10} K = \frac{TD8^{\circ} - DH^{\circ}}{2.303RT}$$
$$= \frac{298 \times 10 + 54.07 \times 1000}{2.303 \times 8.314 \times 298}$$
$$= 9.998 \times 10$$

49. (b) Let, $C(s) + Q(g) \frac{3}{4} \frac{3}{4} @CO2(g)$; D = R

and CO(g)
$$\stackrel{1}{\leftarrow}$$
 O2(g) $\stackrel{3}{\sim}$ 4 $\stackrel{3}{\sim}$ CO(g); H $\stackrel{\square}{\rightarrow}$ S

Subtracting equ. (i) from equ (ii), we get

$$C(s) + \frac{1}{2}2(g)^{3/4}\% CO(g); DH = R - S$$

Hence, heat of formation of CO = R - S

50. (c) Both the doubly bonded carbon atoms are identical.

PART - III (MATHEMATICS)

51. (d) Since Rolle's theorem is satisfied $\ f\phi(c) = b_{\beta}$ esincecosc=0

$$b ec{sinc+cosc}=0$$

$$\sqrt{\sin c + \cos c} = 0$$

$$P \tan c = -1 P c = \tan -1 \quad (-1) = p - \frac{p}{4} = \frac{3p}{4}$$

52. (a) Consider first two equations: 2x + 3y = -4 and 3x + 4y = -6

We have
$$D = \begin{vmatrix} 2 & 3 \\ 3 & 4 \end{vmatrix} = -1^{1} = 0$$

 $Dx = \begin{vmatrix} -4 & 3 \\ -6 & 4 \end{vmatrix} = 2$ and $Dy = \begin{vmatrix} 2 & -4 \\ 3 & -6 \end{vmatrix} = 0$

 $\ \ x = -2$ and y = 0 Now this solution satisfies all the equations, so the equations are consistent with unique solution.

(b) The lines are
$$\frac{x}{6} = \frac{y+2}{6} = \frac{z-1}{1}$$

$$\frac{x+1}{12} = \frac{y}{6} = \frac{z}{-1}$$

Here,
$$a_1 = -2j^+ k^-$$
, $b_1 = 6i^+ + 6j^+ + k^-$, $a_2 = -i^-$, $b_2 = 12i^+ + 6j^-$

$$\int_{0}^{1} f_{0} = \begin{vmatrix} \hat{i} & \hat{j} & k \\ 6 & 6 & 1 \\ 12 & 6 & -1 \end{vmatrix} = -12\hat{i} + 18\hat{j} - 36\hat{k}$$

Shortest distance $\frac{ \left| \begin{pmatrix} r & f_1 & (f_1 - f_2) \\ \hline & |f_1 + f_2| \end{pmatrix} \right|$

$$=\frac{\left|-i^{+}+2j^{-}k^{+}\right).-12ij^{-}36k^{+}}{\sqrt{(-1^{2})^{2}+(18)^{2}+(36)^{2}}}$$

$$=\frac{|+12+36+36|}{\sqrt{1764}}=\frac{84}{42}=2$$

$$= \frac{|+12+36+36|}{\sqrt{1764}} = \frac{84}{42} = 2$$
54. (c) $y2 = x(2-x)$ $y2 = x3 - 4x2 + 4x$...(i)

$$p 2y \frac{dy}{dx} = 3x2 - 8x + p \frac{d}{y} = \frac{3 \times 2 \cdot 8x + 4}{2y}$$

$$\stackrel{\text{\'ed}}{\text{D}} \stackrel{\text{\'u}}{\text{\'ee}} = \frac{3-8+4}{2} = -\frac{1}{2} \stackrel{d}{x}$$

\ Equation of tangent at P is: $y - \frac{1}{2}(x - 1)$

$$\triangleright x + 2y - 3 = 0$$

Using
$$y = \frac{3-x}{2}$$
 in (i),

we get:
$$\stackrel{\stackrel{\text{2}}{\rightleftharpoons}}{\stackrel{\text{2}}{\rightleftharpoons}} \stackrel{\stackrel{\text{2}}{\rightleftharpoons}}{\stackrel{\text{2}}{\rightleftharpoons}} = x3 - 4x2 + 4x$$

 $\stackrel{\text{4}}{\rightleftharpoons} 4x3 - 17x2 + 22x - 9 = 0$...(ii)

which has two roots 1, 1

(Because of (ii) being tangent at (1, 1)).

Sum of 3 roots
$$= \frac{17}{4} \setminus 3$$
rd root $= \frac{17}{4} - 2 = \frac{9}{4}$

Then,
$$y = \frac{3 - \frac{9}{4}}{2} = \frac{3}{8} \setminus Q \text{ is } \overset{20}{\cancel{6}}, \overset{3}{\cancel{6}} \overset{\circ}{\cancel{6}}$$

55. (b) For $x^{-1}0$, we have,

$$f(x) = x + \frac{x/1 + x}{1 - \frac{1}{1 + x}} = x + \frac{x/ + x}{1 + x} = x + 1$$

For
$$x = 0$$
, $f(x) = 0$. Thus, $f(x) = \hat{0}$, $f(x) = \hat{0}$, $f(x) = 0$ 65

Clearly,
$$\lim_{x \to 0^-} f(x) = \lim_{x \to 0^+} f(x) = 1^1 f(0)$$
.

So, f(x) is discontinuous and hence not differentiable at x = 0.

56. (c) Comparing the equation of the circle (x+5)2+(y-3)2=36

with
$$(x-h)2+(y-k)2=r2$$

\
$$-h = 5$$
 or $h = -5$, $k = 3$, $r2 = 36$ P $r = 6$
Centre of the circle is $(-5, 3)$ and radius = 6

If $a = 2i^-2j_+k$ and $c = -i^+2k$

$$|\mathfrak{e}| = \sqrt{(-1)^2 + 22} = \sqrt{1+4} = \sqrt{5}$$

$$|r|c_a^r = \sqrt{5} \cdot (2i^2 - \frac{2}{3} + k^2)$$

$$\left| \frac{1}{c} \right| . r a^{2} \sqrt{3} i^{2} - 2 \sqrt{3} j^{2} + \sqrt{3} k^{2}$$

 $\begin{array}{c|c}
 & \text{1.5} & \text{1.5} & \text{1.5} \\
 & \text{1.5} & \text{1.5} & \text{1.5} \\
 & \text{2.5} & \text{1.5} & \text{2.5} & \text{1.5} \\
 & \text{58.} & \text{(c)} & \text{One vertex of square is (-4, 5) and equation of one diagonal is } 7x - y + 8 = 0 \\
 & \text{3.5} & \text{3.5} & \text{3.5} & \text{3.5} \\
 & \text{4.5} & \text{4.5} & \text{4.5} & \text{4.5} \\
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 & \text{4.5}$ Diagonal of a square are perpendicular and bisect

Let the equation of the other diagonal be y = mx+ c where m is the slope of the line and c is the yintercept.

Since this line passes through
$$(-4, 5)$$

$$5 = -4m + c$$
 ... (i)

\ 5 = -4m + c ... (i) Since this line is at right angle to the line 7x - y + 8 = 0 or y = 7x + 8, having slope = 7,

$$7 \times m = -1 \text{ or } m = \frac{-1}{7}$$

Putting this value of m in equation (i) we get

$$5 = -\frac{\text{æ} \cdot \frac{1}{7} \ddot{o}}{\dot{e} \cdot 7} \ddot{o}$$

or
$$5 = \frac{4}{7} + c$$
 or $c = 5 - \frac{4}{7} = \frac{31}{7}$

Hence equation of the other diagonal is

$$y = -\frac{1}{2}x + \frac{31}{2}$$
 or $7y = -x + 31$

- or $x^{7} + 7y^{7} = 31 = 0$ or x + 7y = 31. 59. (b) $p pq^{\circ} p Uq$
- 60. (b)Put $x^{3/2} = t \frac{3}{2} x^{1/2} dx = dt$

\integral is

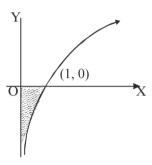
$$\frac{2}{3} dt \\
\frac{3}{\sqrt{1-t^2}} = \frac{2}{3} \sin^{-1} t + C = \frac{2}{3} \sin^{-1} (x^{3/2}) + C$$

(d) In the given sets, the set of all primes is an infinite set.

62. (c)
$$f(x) = \sqrt{(x-2)(x-3) + \sqrt{-(x-4)(x+2)}}$$

(c) $f(x) = \sqrt{(x-2)(x-3) + \sqrt{-(x-4)(x+2)}}$ The first part is real outside (2, 3) and the second is real in [-2, 4] so that the domain is [-2, 2] E [3, 4].

Observing the graph of $\log x$, we find that the required area lies below x-axis between x = 0and x = 1.



So required
$$\int_{0}^{1} area = \lambda \log x dx$$

(a) Let m and m be slope of curve $y = x_{2nd}$ 6y = $7 - x_{3}$ respectively.

Now,
$$y = x2$$
 b $\frac{dy}{dx} = 2x$

$$\triangleright \quad \stackrel{\text{dyö}}{\in} \frac{\text{dyö}}{\text{dx}} = 2 \text{ i.e. } m_1 = 2$$

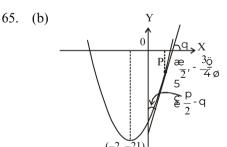
and
$$6y = 7 - x = 6$$
 $\frac{dy}{dx} = -3x^2$

$$\Rightarrow \frac{dy}{dx} = -\frac{3}{6}x^2 = -\frac{1}{2}x^2 =$$

$$\Rightarrow \begin{array}{ccc}
\frac{\partial \mathbf{g}}{\partial y} & \frac{\partial}{\partial y} & = -\frac{1}{2}(1)2 & \frac{1}{2}
\end{array}$$

$$\frac{d}{dx} = \frac{1}{2}$$
 m1 m2 = 2 : $\frac{1}{2}$ = -1

Angle of intersection is 90° i.e.



$$y = x^2 + 4x + 4 - 4 - 17$$

 $y = (x + 2)^2 - 21$ D Vertex is (-2, -21)

Also
$$y = x^2 + 4x - 17$$
 $\frac{dy}{dx} = 2x + 4$
P Slope of tangent $at \frac{5}{2} \underbrace{\frac{dy}{dx}}_{9:4}, -\frac{3}{4} \frac{\ddot{o}}{\dot{o}}$

66. (d)
$$(1+i)4 \times \frac{27}{5} + \frac{1}{i} \frac{\ddot{o}^4}{\ddot{o}} = (1+i)4 \times (1-i)4 = 24$$

67. (d)We have
$$R = \{(x, y) : |x2 - y2| < 16\}$$

Let $x = 1, |x2 - y2| < 16 P |1 - y2| < 16$

Define $|y2 - 1| < 16 P | y = 1, 2, 3, 4$

Let $x = 2, |x2 - y2| < 16 P |4 - y2| < 16$

Define $|y2 - 4| < 16 P | y = 1, 2, 3, 4$

Let $x = 3, |x2 - y2| < 16 P |9 - y2| < 16$

Define $|y2 - 9| < 16 P |9 - y2| < 16$

Define $|y2 - 9| < 16 P |9 - y2| < 16$

Define $|y2 - 9| < 16 P |9 - y2| < 16$

Define $|y2 - 16| < 16 P |9 - y2| < 16$

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Define $|y2 - y2| < 16 P |9 - y2| < 16$

Define $|y2 - y2| < 16$

De

68. (a)
$$\partial_{(ex_+e^{-x})/2}^{2dx} = \partial_{(ex_+e^{-x})/2}^{(e2x_+^2e^{-2x})/2}dx$$

$$= -\frac{1}{(e2x+1)} + c = -\frac{e-x}{e^x + e-x} + c$$
69. (a) $tan-1(1) + tan-1(0) + tan-1(2) + tan-1(3)$

69. (a)
$$\tan^{-1}(1) + \tan^{-1}(0) + \tan^{-1}(2) + \tan^{-1}(3)$$

$$= \frac{p}{4} + p + \tan^{-1}(\frac{2 + 3}{6}) - \frac{2 + 3}{6}$$
 (as 2.3 > 1)

$$= \frac{5p}{4} + \tan^{-1}(\frac{1}{2}) - \frac{p}{4} = p$$

70. Let y denote the number of bacteria at any instant t × then according to the question

$$\frac{dy}{dt}$$
 ayb $\frac{dy}{y} = k dt$... (i)

k is the constant of proportionality, taken to be + ve on integrating (i), we get $\log y = kt + c$ (ii)

 $\log y = kt + c$... (ii) c is a parameter. let \emptyset be the initial number of bacter 1 a i.e., at t = 0 using this in (ii), $c = \log y$

$$y = \underset{\hat{Q}}{\overset{\infty}{\rightleftharpoons}} y_0 + \underset{100}{\overset{10}{\rightleftharpoons}} y_0 \underset{\emptyset}{\overset{\circ}{\rightleftharpoons}} = \underset{0}{\overset{11}{\leadsto}} y_0, \text{ when } t = 2$$

So, from (iii), we get $\log \frac{10}{y} = k(2)$

$$b = k = \frac{1}{2} \log \frac{11}{10}$$
 ... (iv)

Using (iv) in (iii)
$$\log \frac{y}{\hat{y}_0} = \frac{1}{2} \xi \log \frac{11}{6} \ddot{\phi} \dot{\phi}$$

... (v) let the number of bacteria become 1, 00, 000 to 2,00,000 in 1 hours. i.e., y = 2y0 when t = 1 hours. from (v)

$$\log \frac{2y_0}{y_0} = \frac{1}{2} \exp \frac{11}{10} \stackrel{\circ}{\rightleftharpoons} t_1 P t_1 = \frac{2 \log 2}{\log \frac{11}{10}}$$

Hence, the reqd. no. of hours $\frac{2 \log 2}{\log 10}$

71. (a) The given lines are:

$$y = (2 - \sqrt{3}) x + 5$$
 and $y = (2 + \sqrt{3}) x - 7$

Therefore, slope of first line $=_1 \text{m} \not\supseteq -\sqrt{3}$ and slope of second line $= \underline{m} = 2 + \sqrt{3}$

$$\tan q = \left| \frac{m_2 - m1}{1 \text{ m 1 m 2}} \right| = \left| \frac{2 + \sqrt{3} - 2 + \sqrt{3}}{1 + (4 - 3)} \right|$$

$$= \left| \frac{2\sqrt{3}}{2} \right| = \sqrt{3} = \tan \frac{p}{3} \quad p \neq \frac{p}{3} = 60^{\circ}$$
72. (a) If q is the angle between line and plane

then $c_{\overline{2}}$ p $c_{\overline{1}}$ b is the angle between line and

normal to plane given by

$$\cos \frac{e}{k^{2}} - q = \frac{\$ + 2\$ + 2k^{-}\$}{3\sqrt{4+1+1}}$$

Psing =
$$\frac{2\sqrt{1}}{3\sqrt{5}} + 1 = \frac{1}{3}$$
 p | 4= 5 + | D | = $\frac{5}{3}$.

73. (a) Given equation of line is

$$r = 2i^-j^+ 2k^+ 13i^+ 4j^+ 2k^-$$

$$(xif yj^{+}+zk^{+}+3i^{+}+4j^{+}+2k^{+}) + 2(+31i)^{+}+(21z+4k^{+}j^{+}+ \frac{|x+3|-2}{x+2}) > 0 > 0$$
Any point on the line is

Since it also lie on the plane $r \cdot (i)$ $\Rightarrow \frac{-x+5}{x+2} > 0 \Rightarrow \frac{x+5}{x+2} < 0$

So, éë(2+3|)i^+(-1+4|)j^+(2)
$$k\hat{u}\hat{u}_{-}\hat{i} k_{-}$$

$$p = 2 + 31 + 1 - 41 + 2 + 21 = 5 \text{ pl} = 0$$

Therefore, coordinate of the point of intersection of line and plane is (2,-1, 2). \ Distance

$$d = \sqrt{(2+1)2+(1+5)2+(2+10)2} =_{13}$$

74. (a)
$$I = Q_{\log \sqrt{p/2}}^{\log \sqrt{p}} e^{2x} \sec^2 Q_{Q}^{2} e^{2x} Q_{Q}^{2} dx$$

Put
$$e^{2x} = t \triangleright 2e^{2x} dx = dt$$

When
$$x = \log \sqrt{p/2}$$
, $t = e^{\log p/2}$

$$= e^{\log p/2} = \frac{1}{2}$$

When $x = log \sqrt{p}$, t = e2log/p = p

$$\begin{aligned} | &= \sum_{\substack{3\frac{1}{2} \\ \frac{1}{2} \\ \frac$$

75. (c) We have $\frac{|x^{x} + 3| + x}{2} > 1$

$$\triangleright \frac{|x+3|+x}{x+2} - 1 > 0 \triangleright \frac{|x+3|-2}{x+2} > 0$$

Now, two cases arise:

Case I: When x + 3 = 0, i.e. $x^3 - 3$. Then,

$$\frac{|x+3|-2}{|x+2|} > 0 \Rightarrow \frac{|x+3-2|}{|x+4|} > 0$$

$$> \frac{x+1}{x+2} > 0$$

$$\triangleright \{(x+1) > 0 \text{ and } x + 2 > 0\}$$

or
$$\{x + 1 < 0 \text{ and } x + 2 < 0\}$$

$$\triangleright \{x > -1 \text{ and } x > -2\}$$

or
$$\{x < -1 \text{ and } x < -2\}$$

$$> -1$$
 or < -2

$$\triangleright x \mid (-1, \forall) \text{ or } x \mid (-\forall, -2)$$

Case II: When x + 3 < 0, i.e. x < -3

$$\frac{|x+3|-2}{x+2} > 0 \triangleright \frac{-x-3-2}{x+2} > 0$$

$$p \frac{-x+5}{x+2} > 0 p \frac{x+5}{x+2} < 0$$

(x + 5 < 0 and x + 2 > 0) or (x + 5 > 0)and x + 2 < 0

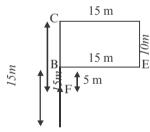
 \triangleright (x < -5 and x > -2) or (x > -5 and x < -2) it is not possible.

$$\triangleright x \hat{1} (-5, -2)$$
 ... (ii)

Combining (i) and (ii), the required solution is $\hat{\mathbf{x}}$ (-5, -2) $\hat{\mathbf{E}}$ (-1, $\hat{\mathbf{Y}}$).

PART - IV (ENGLISH & LOGICAL **REASIO NING)**

- 76. (b) See the last paraserate of the fourth (c) Virtually, the whole passage deals with
- 77. F.A.S.T. membership requirements. The choices are too narrow to be main ideas.
- 78. (a) (See the first paragraph. Let the fixed
- his nourneyon by here Jarlingtarhis walking directions are as follows.



AF = AB - FB = 15 - 5 = 10 meters So, Jatin is 10 meters away from the starting

point.

80. (b) F — Mohan's family members E — Employed members

H — Honest members



shaded area denotes employed members of Mohan's family members, who are h on est.