## **VITEEE 2013 Question Paper**

Vellore Institute of Technology Engineering Entrance Examination

# **SOLVED PAPER**

#### (a) 2k/x3 (b) -2k/x3(d) -k/x(c) k/x

7. A copper wire of length 2.2 m and a steel wire of length 1.6 m, both of diameter 3.0 mm are connected end to end. When stretched by a force, the elonation in length 0.50 mm is produced in the copper wire. The stretching force is

8.

11.

- $(Y_{cu} = 1 \times 1011 \text{ N/m})$ (a) 5.4 × 102 N (b) 3.6 × 102 N
- (d) 1.8 × 102 N (c) 2.4 × 102 N
- bf nepresents taned mean speed, root mean square and most probable speed of the molecules in an ideal monoatomic gas at temperature T and if m is mass of the molecule, then
- (a) vp < v < vrms
- (b) no molecule can have a speed greater than  $\sqrt{2}V_{rms}$
- (c) no molecule can have a speed less than

$$V_p / \sqrt{2}$$

- (d) None of the above
- Two balls of equal masses are thrown upwards along the same vertical direction at an interval of 2 s, with the same initial velocity of 39.2 m/s. The two balls will collide at a height902 (b) 73.5 m (d) 117.6 m ) m
- 10. the difficult formula of magnetic flux is

the time dependence of a physical quantity *P* is given by P = P ga (-at2), where is a constant and t is time. The constant a

- (a) is a dimensionless
- has dimensions of P (b)
- (c) has dimensions of T-2
- (d) has dimensions of T2

### PART - I (PHYSICS)

- ٦. The amplitude of an electromagnetic wave in vaccum is doubled with no other changes made to the wave. As a result of this doubling of the amplitude, which of the following statement is cor r ect?
  - The frequency of the wave changes only (a)
  - The wave length of the wave changes (b)
  - only The speed of the wave propagation (c)
  - (d) changes only Alone of the above is correct
- 2. An element with atomic number Z = 11 emits K a – X-ray of wavelength X-ray of wavelength number which emits K4is
  - (a) 4 (b) 6
  - (c) 11 (d) 44
- 3. Mobilities of electrons and holes in a sample of intrinsic germanium at room temperature are 0.36m2 V-1s-1 and 0.17m2V-1s-1. The electron and hole densities are each equal to  $2.5 \times 1019$ m3. The electrical conductivity of germanium is (h) 2.12 Sm-1 1 2 1 Cm 1 9.

(a) 
$$4.24 \text{ Sm} = 1$$
 (b)  $2.12$ 

- (d) 0.47 Sm-1 (c) 1.09 Sm-1
- If a radio-receiever amplifiers all the signal 4. frequencies equally well, it is said to have high (a) sensitivity (b) selectivity
  - (c) distortion (d) fidelity
- 5. If a progressive wave is represented as

x÷ö 4÷ø where x is in metre and t is

in second, then the distance travelled by the wave in 5 s is

(b) 10 m (a) 5 m

- (c) 25 m (d) 32 m
- 6. The gravitational potential at a place varies inversely with x2(i.e., V = k/x2), the gravitational field at that place is

2013

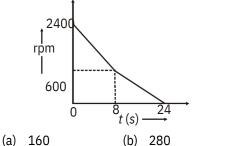
12. If the potential energy of a gas molecule is

$$U = \frac{M}{r} \frac{N}{12}M$$
 and N being positive

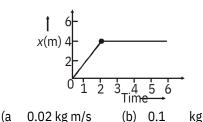
constants, then the potential energy at equilibrium must be (b) NM2/4 (a) zero

(d) M2/4N (c) MN2/4

13. A table fan rotating at a speed of 2400 rpm is 18. switched off and the resulting variation of revolution/minute with time is shown in figure. The total number of revolutions of the fan before it, comes to rest is



- (c) 380 (d) 420
- 14. In the adjoining figure, the position time graph of a particle of mass 0.1 kg is shown. The impulse20. Four equal charges *Q* each are placed at four at t = 2 s is



- 0.2 kg m/s 0.4 ) (d) m/s 15. (d)e pressure on a squarekglates is measured by measuring the force on the plate. If the maximum error in the measurement of force and length are respectively 4% and 2%, then the maximum error in the measurement of (b) 2% baressiling is (c) 4% (d) 8%
- The centre of a wheel rolling on a plane surface 16. on avera with the aspteted in of the wheel at the same level as the centre will be moving at speed
  - (a) zero (c) 2v<sup>0</sup> 2v0

17. A body of mass 5 m initially at rest explodes into 3 fragments with mass ratio 3:1:1. Two of fragments each of mass 'm' are found to move with a speed of 60 m/s is mutually perpendicular directions. The velocity of third fragment is (h) on  $\sqrt{2}$ 

(a) 
$$10\sqrt{2}$$
 (b)  $20\sqrt{2}$ 

(c)  $20\sqrt{3}$ (d) 60√2

A body of mass 2 kg moving with velocity of 6 m/s strikes in elastically with another body of same mass mass at rest. The amount of heat evolved during collision is

19. Two particles of equal mass m go round a circle of radius R under the action of their mutual gravitational attraction. The speed of each particle is

(a) 
$$\frac{1}{2}\sqrt{\frac{Gm}{R}}$$
 (b)  $\sqrt{\frac{4Gm}{R}}$   
(c)  $\sqrt{\frac{Gm}{2R}}$  (d)  $\frac{1}{2R}\sqrt{\frac{1}{Gm}}$ 

corners of a square of side a each. Work done in carrying a charge -q from its centre to infinity is

(a) zero pe<sub>o</sub>a

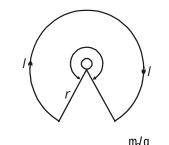
(c) 
$$\frac{q^2}{2pe_0 a}$$
 (d)  $\frac{\sqrt{2}q^2}{pe}$ 

21. A network of resistances, cell and capacitor C(= 2 mF) is shown in adjoining figure. In steady state condition, the charge on 2mF capacitor is Q, while R is unknown resistance. Values of Q and *R* are respectively

$$10 V_{A}^{\circ} \downarrow_{I=1A}^{\circ} \downarrow_{$$

(a 4mC and 10W (b) 4mC and 4W 2 mC and 2 W (d) 8mC and 4 W ) (c)

- 22. As the electron in Bohr's orbit of hydrogen atom passes from state n = 2 to, n = 1, the KE (K) and the potential energy (U) changes as
  - (a) *K* four fold, *U* also four fold
  - (b) K two fold, V also two fold
  - (c) K four fold, U two fold K
  - (d) two fold, *U* four fold
- 23. To get an OR gate from a NAND gate, we need
  - (a) Only two NAND gates
  - (b) Two NOT gates obtained from NAND gates
  - (c) and one NAND gate
  - Four NAND gates and two AND gates obtained from NAND gates None of the above
- 24. If a current I is flowing in a loop of radius r as shown in adjoining figure, then the magnetic field induction at the centre O will be



(a) Zero (b) 
$$\frac{10}{4pr}$$

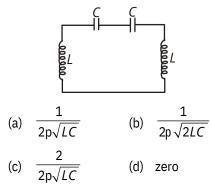
(c) 
$$\frac{\text{mO/sin q}}{4\text{p}r}$$
 (d)  $\frac{2\text{m}}{4\text{p}r^2}\frac{\sin q}{2\text{p}r^2}$ 

25. Two indentical magnetic dipoles of magnetic moment 1.0 Am2 each, placed at a separation of 2 m with their axes perpendicular to each other. The resultant magnetic field at a point midway between the dipoles is

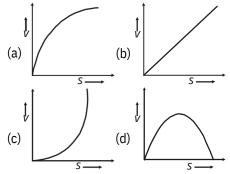
(a) 
$$\sqrt{5}' 10^{-7} T$$
 (b)  $5 \times 10^{7} T$ 

(c) 
$$10-7 T$$
 (d)  $2 \times 10-7 T$ 

26. The natural frequency of the circuit shown in adjoining figure is



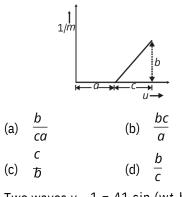
27. A lead shot of 1 mm diameter falls through a long column of glycerine. The variation of the velocity with distance covered (s) is correctly represented by



28. **Df a**nd m0 represent the permittivity and permeability of vaccum and and μ represent the permittivity and permeability of medium, then refractive index of the medium is given by

(a) 
$$\sqrt{\frac{e_0 m_0}{em}}$$
 (b)  $\sqrt{\frac{em}{em_0}}$   
(c)  $\sqrt{\frac{m_0 e_0}{e}}$  (d)  $\sqrt{\frac{m_0 e_0}{m}}$ 

29. A students plots a graph between inverse of magnification 1/m produced by a convex thin lens and the object distance u as shown in figure. What was the focal length of the lens used?

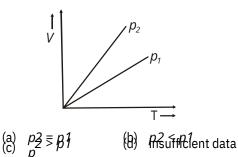


30. Two waves y 1 = A1 sin (wt-b1) andy2 = A2 sin (wt-b2) superimpose to form a resultant wave whose amplitude

is 
$$A1 + A2$$
  
(a)  $1 + A2|$   
(b)  $|A \sqrt{A_{1}^{2} + A_{2}^{2}} - 2A1A2 \sin(b1 - b2)}$   
(c) (d)  $\sqrt{A_{1}^{2} + A_{2}^{2}} + 2A1A2 \cos(b1 - b2)}$ 

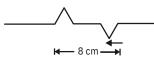
31. When a certain metallic surface is illuminated with monochromatic light of wavelength , the stopping potential for photoelectric current BWhen the same surface is illuminated with a light of wave length 2, the stopping potential is  $V_0$ . The threshold wavelength for this surface to photoelectric effect is

32. In the *V*-*T* diagram shown in adjoining figure, what is the relation between *p***1** and *p*2?



33. If a gas mixture contains 2 moles of **Q and/4s** of Ar at temperature *T*, then what will be the total energy of the system (neglecting all vibrational modes)

34. **(c)** the adjoining figure, two pulses in a stretched string are shown. If initially their centres are 8 cm apart and they are moving towards each other, with speed of 2cm/s, then total energy of the pulses after 2 s will be



- (a) Zero
- (b) Purely kinetic
- (c) Purely potential
- (d) Partly kinetic and partly potential
- 35. When two waves of almost equal frequency n 1 and n 2 are produced simultaneously, then the time interval between succesive maxima is

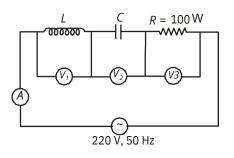
(a) 
$$\frac{1}{n1_{+}n2}$$
 (b)  $\frac{1}{n1_{+}} \frac{1}{n2}$   
(c)  $\frac{1}{n1} \frac{1}{n2}$  (d)  $\frac{-}{n1_{-}n2}$ 

36. A long glass capillary tube is dipped in water. It is known that water wets glass. The water level

rises by h in the tube. The tube is now pushed

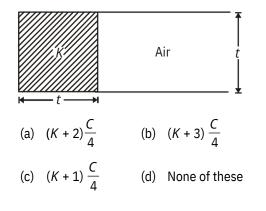
down so that only a length h/2 is outside the wateras afface. The amele  $60^{\circ}$  contact at the wates  $0^{\circ}$  (d)  $15^{\circ}$ 

37. In the adjoining of the tube will be the the adjoining of the tube will be V 1 and V2 are 300 volts each, then the reading voltmeter V3 and ammeter A are respectively

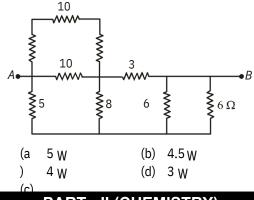


38. **(f**) the Work done in turking a magnet of magnetic moment *M* by an angle of 90° from the magnetic meridian is n times the corresponding work done to turn it through an angle of  $60^{\circ}$ , then the value of *n* is

39. The capacitance of a parallel plate capacitor with air as dielectric is *C*. If a slab of dielectric constant *K* and of the same thickness as the separation between the plates is introduced so as to fill 1/4th of the capacitor (shown in figure), then the new capacitance is

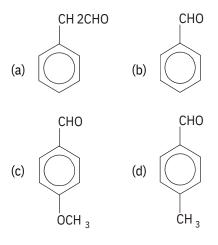


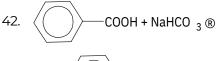
40. Seven resistance are connected between points *A* and *B* as shown in adjoining figure. The equivalent resistance between *A* and *B* is

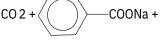


#### PART - II (CHEMISTRY)

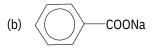
41. Which of the following does not undergo benzoin condensation?







Cis with the product (a) CO  $_2$ 



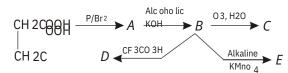
(c) Both (a) and (b)

(d) None of the above

43. Benzene diazonium chloride on treatment with hypophosphorous acid and water yield benzene. Which of the following is used as a catalyst in this reaction?(a) LiAlH (b) Red p

|        | 4 | (D) Rea |
|--------|---|---------|
| (c) Zn |   | (d) Cu+ |

44. Consider the following reaction sequence,

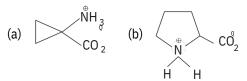


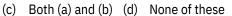
Isomers are

(a) C and E (b) C and D

| (c) D and E | (d) C,D and E |
|-------------|---------------|
|-------------|---------------|

- 45. When a monosaccharide forms a cyclic hemiacetal, the carbon atom that contained the carbonyl group is identified as the .... Carbon at om,becau se
  - (a) D, the carbonyl group is drawn to the right
  - (b) L, the carbonyl group is drawn to the left
  - (c) acetal,it forms bond to an -OR and an OR'
  - (d) anomeric, its substituents can assume an b or position
- 46. Which of the following is/ are amino acid?

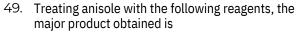




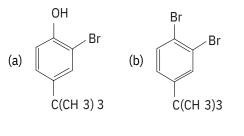
47. Calculate pH of a buffer prepared by adding 10 mL of 0.10 M acetic acid to 20 mL of 0.1 M sodium acetate [ $pk_a$  (CH3COOH) = 4.74]

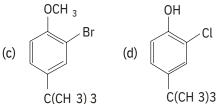
| (a) | 3.00 | (b) | 4.44 |
|-----|------|-----|------|
| (c) | 4.74 | (d) | 5.04 |

- 48. The equivalent conductance of silver nitrate solution at 250°C for an infinite dilution was found to be 133.3–1 cm2 equiv-1. The transport number of Ag+ ions in very dilute solution of AgNO 3 is0.464. Equivalent conductances of Ag and NO-3(in –1 cm2 e quiv<sup>-1</sup>) at infinite dilution are respectively
  - (a) 195.2, 133.3 (b) 61.9, 71.4
  - (c) 71.4, 61.9 (d) 133.3, 195.2



- I. (CH3)3 CCl, AlCl3 II. Cl2, FeCl3
- III. HBr, Heat





50. Ketones  $\begin{bmatrix} R-C-R' \end{bmatrix}$  where, R = R' = alkyl

group can be obtained in one step by (a)drolysis of esters (b)idation of primary alcohols (c)idation of secondary alcohols (c)action of acid halide with alcohols

- 5]. An optically active compound 'X' has molecular formula C4H8O3, It evolves CO2 with actieve an NaHCO achiral compound.'X' is
  - (a) СН <u></u>СН <u>С</u>НСООН
    - ОH
  - (b) CH 3CH CO O H | OMe
  - (c) CH 3CH CO O H | CH<sub>2</sub>OH

52. 
$$OH$$
 con c.H2S04 products.

(a) 
$$(a)$$
  $(b)$   $(b)$   $(c)$  None is correct  
(c) Both (a) and (b) (d) None is correct  
53.  $(c)$   $(c)$  Both (a) and (b) (d) None is correct  
(c)  $(c)$   $(c)$ 

(c) salicylic acid (d) flurorescein

55. C6H5NH2 
$$\xrightarrow{\text{NaNO}_2/\text{HCl}} X \xrightarrow{\text{CuCN}}$$

 $Y \xrightarrow{H20H} Z, Z \text{ is identified as}$ (a) 6H5 - NH<sub>5</sub>-CH3<sub>2</sub>

56. B'can be obtained from halide by van-Arkel method. This involves reaction

(a) 
$$2Bl_{3}ed hot W or Ta_{2B} + 3l_{2}$$

(b) 
$$2BCl_3 + 3H_2 \xrightarrow{\text{Red hot W or Ta}} 2B + 6HCl$$

(d) Both (a) and (b) None of the above

Product is/are

- 57. AVCL(s) is heated in a test tube. Vapours are brought in contact with red litmus paper, which changes it to blue and then to red. It is because of
  - (a) formation of NH4QH and HCl
  - (b) formation of NH
  - (c) greater diffusion of NH3 than HCl (d)
- Out of H 2S2O3, H2S2O4, H2SO5 and H2S2O8 58. peroxy acids are
  - H2S2O3,8(b) u2S2O4,H2SO5(d) (a H2\$263H2\$\$264 )
- 59. The density of solid argon is 1.65 g per cc at -233°C. If the argon atom is assumed to be a sphere of radius 1.54 × 10-8 cm, what per cent of solid argon is apparently empty space? (Ar = 40)
  - (a) 16.5% (b) 38% (b) 50%
  - (d) 62%
- 60. When 1 mole of CO 2(g) occupying volume 10L at 27°C is expanded under adiabatic condition, temperature falls to 150 K. Hence, final volume is

| (a) | 5 L  | (b) | 20 L |
|-----|------|-----|------|
| (c) | 40 L | (d) | 80 L |

61. Acid hydrolysis of ester is first order reaction and rate constant is given by

 $k = \frac{2.303}{t} \log_{\frac{V}{V} = -V0}^{\frac{V}{V}} \text{ where, } V0, Vt \text{ and } V \neq Vt}$ 

are the volumle of standard NaOH required to neutralise acid present at a given time, if ester is 50% neutralised then

(a) 
$$V_{\underline{X}} = V_{Vt} - VO$$
 (b)  $V_{\underline{X}} = (V_{VT} + V_{VO})$ 

- (c) V
- 62. A near UV photon of 300 nm is absorbed by a gas and then re-emitted as two photons. One photon is red with wavelength of the second photon is

| (a) | 1060 nm | (b) | 496 nm |
|-----|---------|-----|--------|
| (c) | 300 nm  | (d) | 215 nm |

- (c) 300 nm (d) 215 nm
- 63. Which of these ions is expected to be coloured in aqueous solution?

| I. Fe3 + | II. Ni2+ | III. Al3+ |
|----------|----------|-----------|
| ()       | (1)      |           |

(a) I and II (b) II and III (c) I and III (d) I, II and III

- 64. Select the correct statements(s).
  - (a) LiAlH 4 reduces methyl cyanide to methyl ami n e
  - (b) Alkane nitrile has electrophilic as well as nucleophilic centres
  - saponification is a reversible reaction (c)
  - (d) Alkaline hydrolysis of methane nitrile forms methanoic acids

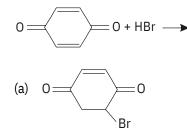
con c.HN 03 + conc.H2SO4 ► X Cl 2/FeCl3 Δ

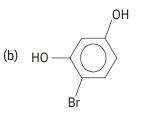
The product Y is

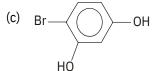
65.

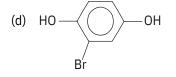
- (a) *p*-chloro nitrobenzene
- (b) o-chloro nitrobenzene
- (c) *m*-chloro nitrobenzene
- (d) *o*, *p*-dichloro nitrobenzene

66. End product of the following reaction is

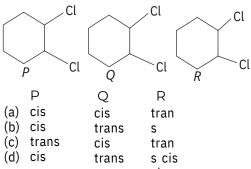








67. Following compounds are respectively ... geometrical isomers



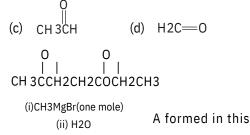
68. Which is more basic oxyger **fin** an ester?

- (a) Carbonyl oxygen,
- (b) Carboxyl oxygen, b
- (c) Equally basic
- (d) Both are acidic oxygen
- 69. In a Claisen condensation reaction (when an ester is treated with a strong base) (a) rboproton iforemonedrfrom the stabilised carbanion of the ester carbanion acts as a nucleophile in a nucleophilic acyl substitution (b) action with another ester molecule (c) a new C-C bond is formed
  - (d) All of the above statements are correct
- 70. An organic compound *B* is formed by the reaction of ethyl magnesium iodide with a substance *A*,

followed by treatment with dilute aqueous acid,

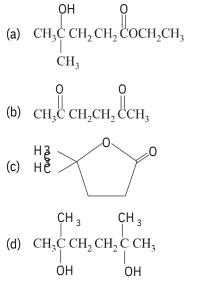
Compound B does not react with PCC or PDC in

dichloromethane. Which of the following is a (a)sSHb2e-CCH2pound fo(b)?CH 3 CH 2CCH3



reaction is

71.



72. For the cell reaction  $2Ce4 + Co^{\circ} 2Ce3 + + Co^{\circ} + Co^{\circ} + E^{\circ}_{Cell}$  cell is 1.89 V. If  $E_{Co}^{\circ} + E^{\circ}_{Cell} = -0.28$  V,

what is the value of  $E_{c}^{\circ}4+/Ceo3+?$ 

| (a) | 0.28 V | (b) | 1.61 V |
|-----|--------|-----|--------|
| (c) | 2.17 V | (d) | 5.29 V |

73. A constant current of 30 A is passed through an aqueous solution of NaCl for a time of 1 00 h. What is the volume of Cl

- (a) 30.00 L (b) 25.08 L
- (c) 12.54 L (d) 1.12 L
- 74. Consider the following reaction,

The reaction is of first order in each diagram, with an equilibrium constant of 104. For the conversion of chair form to boat form  $e-Ea/RT = 4.35 \times 10-8$  m at 298 K with preexponential factor of 1012 s-1. Apparent rate constant (= kA / kB) at 298 K is

(a)  $4.35 \times 104 \text{ s-1}$  (b)  $4.35 \times 108 \text{ s-1}$ 

(c) 
$$4.35 \times 10-8 \text{ s-1}$$
 (d)  $4.35 \times 1012 \text{ s-1}$ 

75. If for the cell reaction, Zn + Cu2+ Cu + Zn2+ Entropy change S° is 96.5 J mol-1K-1, then temperature coefficient of the emf of a cell is
(a) 5 × 10-4 VK-1 (b) 1 × 10-3 VK-1

(c) 2 × 10-3 VK-1 (d) 9.65 × 10-4 VK-1

- 76. What transition in the hydrogen spectrum would have the same wavelength as the Balmer transition, n = 4 to n = 2 of He+ spectrum 2 to n = (b) n = 3 to n =) 2 n = 2 to n (d) 2 n = 4 to n
- 77. (W) hat if the degeneracy of the level of H-atom  $\tilde{o}$

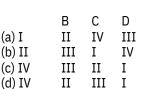
that has energy 
$$\begin{bmatrix} \frac{R}{2} & \frac{R}{90} \\ \frac{R}{2} \end{bmatrix}$$
?

(a) 16 (b) 9

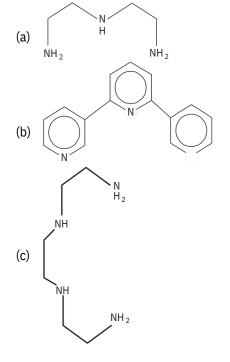
- 78. (c) 4 (d) 1 Match the following and choose the correct
- 78. Match the following and choose the correct option given below. Compound/Type Use
  - A: Bry ice Selderonductor
  - D. TEL
    - А

I.Anti-knocking compound II.Electronic diode or triode III. Joining circuits IV.Referigerant for

preserving food



79. Which of the following ligands is tetradentate?



C = 0 (d)  $^{CH_2}$ C = 0  $^{CH_3}$ 80. What is the EAN of [Al(C 40)]\_3  $^{3-?}$ (a) 28 (b) 2 (c) 16 (d) 2

CH<sub>3</sub>

#### PART - III (MATHEMATICS)

- 81. The relation *R* defined on set A = {*x* : | *x* | < 3, *x*e I } by *R* = {(*x*, *y*) : *y* = | *x* |} is
  - (a) {-2, 2), (-1, 1), (0, 0), (1, 1), (2, 2) }
  - (b) {(-2, -2), (-2, 2), (-1, 1), (0, 0), (1, -2), (1, 2), (2, -1), (2, -2)}
  - (c)  $\{0, 0\}, (1, 1), (2, 2)\}$
  - (d) None of the above
- 82. The solution of the differential equation

$$\frac{dy}{dx} = \frac{yf'()x-2 \ y}{f(x)}$$
 is

(a) 
$$f(x) = y+C$$
 (b)  $f(x) = y(x+C)$ 

(c) f(x) = x+C (d) None of the above

83. If a, b and c are in AP, then determinant

| X+<br> X +<br> X + | 2<br>3<br>4 | x +3<br>x +4<br>x +5 | x+<br>2a<br>x+<br>2b | is         |
|--------------------|-------------|----------------------|----------------------|------------|
| (a)                | 0           |                      | 210<br>X+ 2/10)      | 1          |
| (c)                | х           |                      | (d)                  | 2 <i>x</i> |

84. If two events A and B. If odds against A are as2:1 and those in favour of AÈB are as 3:1, then

| (a) $\pounds \frac{1}{2}(B) \pounds$ | $\frac{3}{4}$ | (b) | $\frac{5}{12}$ £ <i>P</i> ( <i>B</i> )£ | $\frac{3}{4}$ |
|--------------------------------------|---------------|-----|---|---------------|
| 1                                    | 3             |     |   |               |
| (c) £ <i>P<del>(</del>B</i> )£       | <del>5</del>  | (d) | None of thes                            | se            |

85. The value of  $2 \tan^{-1}(\operatorname{cosec} \tan^{-1} x - \tan \operatorname{cot}_X)$ 

| 15  |                |     |       |  |
|-----|----------------|-----|-------|--|
| (a) | tan–1 <i>x</i> | (b) | tan x |  |

(c)  $\cot x$  (d)  $\csc -1x$ 

- 86. The proposition ~  $(p \hat{U} q)$  is equivalent to (a)  $(p ~ q) \hat{U} (q \hat{U} ~ p)$ 
  - (b)  $(p\dot{U} \sim q)$   $(q\dot{U} \sim p)$
  - (c)  $(p\dot{U} \sim q)$   $\dot{U}$   $(q\dot{U} \sim p)$
  - (d) None of the above
- 87. If truth values of *P* be *F* and *q* be *T*. Then, truth value of  $\sim (\sim p q)$  is
  - (a) T (b) F
  - (c) Either T or F (d) Neither T not F
- 88. The rate of change of the surface area of a sphere of radius *r*, when the radius is increasing at the rate of 2 cm/s is proportional to

(a) 
$$\frac{1}{r}$$
 (b)  $\frac{1}{r^2}$   
(c)  $r$  (d)  $\frac{1}{r^2}$ 

- If N denote the set of all natural numbers and R 95. 89. be the relation on  $N \times N$  defined by (a, b) R (c, d), if ad (b + c) = bc (a + d), then R is
  - (a) symmetric only
  - (b) reflexive only
  - (c) transitive only
  - (d) an equivalence relation
- 90. A complex number z is such that arg

$$\zeta_{\overline{z}}^{\text{ez-20}}$$
  $\underline{z}^{\text{T}}$  he points representing this

complex number will lie on

- (a) an ellipse (b) a parabola
- (c) a circle (d) a straight line
- 91. If a1, a2 and a3 be any positive real numbers, then which of the following statement is true?

(a) 
$$3a_{12}a_{3} \pm a_{13} \pm a_{3} \pm a_{3} \pm a_{3}$$
  
(b)  $\frac{a_{1}}{a2} + \frac{a_{13}}{a3} + \frac{a_{13}}{2} + \frac{a_{13}}{2} + \frac{a_{13}}{2} + \frac{a_{13}}{2}$   
(c)  $(a_{1} + a_{2} + a_{3}) \frac{a_{13}}{c_{11}} + \frac{1}{a_{2}} + \frac{1}{a_{1}} +$ 

(d) 
$$(a1a2 a3 +) \begin{cases} 1 & 1 & a_3 + a_3 \\ a_1 & a_2 & a_3 \end{cases} 27$$

- 92. If |x2 x 6| = x + 2, then the values of x are (a) -2, 2, -4 (b) -2, 2, 4 (c) 3, 2, -2 (d) 4, 4, 3
- 93. The centres of a set of circles, each of radius 3, lie on the circle x2 + y2 = 25. The locus of any point in the set is

- (a) 4 £ x2 + y2 £ 64
- (b) x2+ y2 £ 25
- (c) x2+ y2 3 25 3 £ x2
- (d) + y2 £ 9
- 94. A tower *AB* leans towards west making an angle with the vertical. The angular elevation of *B*,
  - the top most point of the tower is b as observed from a point C due east of A at a distance 'd' from A. If the angular elevation of B from a point D due east of C at a distance 2d from C is r, then 2 tan can be given as
  - (a  $3 \cot b 2 \cot$  (b)  $3 \cot 2 \cot b$ )  $3 \cot b - \cot$  (d)  $\cot b - 3 \cot$
  - (c) and b are the roots of  $x^2 ax + b = 0$  and if
  - If n + bn = V n, then

(a) 
$$V_B \ddagger 1 \equiv g V_B \ddagger b V_B \ddagger 1$$

(d) *V* 96. The sum of the series

$$\sum_{r=0}^{n} (-1)^{r} C_{r} \frac{\alpha}{2r} \frac{1}{2r} + \frac{3r}{22r} + \frac{7r}{23r} + \frac{15r}{24r} \dots m \operatorname{term}_{\frac{1}{2}}^{\frac{1}{2}} \frac{1}{9}$$

$$(a) \quad \frac{2^{mn}}{2^{mn}(2^{n}-1)} \qquad (b) \quad \frac{2^{mn}-1}{2^{n}-1}$$

$$(c) \quad \frac{2^{mn}+1}{2^{n}+1} \qquad (d) \quad \text{None of these}$$

97. The angle of intersection of the circles x2+ y2
 -x + y − 8 = 0 and x2 + y2 + 2x + 2y − 11 = 0 is

(a) 
$$\tan -1 \underbrace{\underbrace{a19\ddot{p}}_{\dot{e},qg}}_{\dot{p},\dot{p},\dot{e}}$$
 (b)  $\tan -1(19)$ 

(c) 
$$\tan -1 \underset{\substack{\downarrow 19 \\ \downarrow 20 \\ \downarrow 0 \\ \downarrow$$

98. The vector b<sup>33</sup> 3j + 4k is to be written as the sum of a vector b1 parallel to a = i + j and a vector b2 perpendicular to a. Then b1 is equal to

(a) 
$$\frac{3}{2}$$
 (i + j)  
(b)  $\frac{2}{3}$  (i + j)  
(c)  $\frac{2}{3}$  (i + j)  
(d)  $\frac{1}{3}$  (i + j)

- 99. If the points (*x*1, *y*1), (*x*2, *y*2) and (*x*3, *y*3) are collinear, then the rank of the matrix
- (c) 1 (d) None 100. The value of the determinant

| $\begin{vmatrix} 1 & \cos( \ ) & \cos \\ \cos( \ ) & 1 & s \\ \cos & \cos & co1 \end{vmatrix}$ is |  |
|---|--|
| (a) $2^{2}$ (b) $2^{2}$   |  |
| (c) 1 (d) 0   |  |

- 101. The number of integral values of K, for which the equation  $7 \cos x + 5 \sin x = 2K + 1$  has a solution, is (a) 4 (b) 8
  - (c) 10 (d) 12
- 102. The line joining two points A(2,0), B(3,1) is rotated about A in anti-clockwise direction through an angle of 15°. The equation of the line in the now position, is
  - (a)  $\sqrt{3}x y 2\sqrt{3} = 0$
  - (b)  $x 3\sqrt{y} 2 = 0$
  - (c)  $\sqrt{3}x + y 2\sqrt{3} = 0$
  - (d)  $x + \sqrt{3}y 2 = 0$
- 103. The line  $2x + \sqrt{6}y = 2$  is a tangent to the curve  $x^2 2y^2 = 4$ . The point of contact is

(a) 
$$(4, -\sqrt{6})$$
 (b)  $(7, -2\sqrt{6})$ 

(c) 
$$(2, 3)$$
 (d)  $(\sqrt{6}, 1)$ 

104. The number of integral points (integral point means both the coordinates should be integer) exactly in the interior of the triangle with vertices (0, 0), (0, 21) and (21, 0) is

| (a) | 133 | (b) | 190 |
|-----|-----|-----|-----|
| (c) | 233 | (d) | 105 |

- 105. **(1+-**x )  $e^{x+1x}$  C dx is equal to
  - (a)  $(x \ 1)e^{x \ x^{1}}$
  - (b)  $(x \ 1)e^{x \ x^{1}} C$

(c) 
$$xe^{xx} + C$$
  
 $xe^{x} + x + C$   
106. If  $f(x) = x - [x]$ , for every real number x, where  $[x]$ 

is the integral part of x. Then,  $\partial f(x) dx$  is equal

| to<br>(a) | 1 | (b) | 2             |
|-----------|---|-----|---------------|
| (c)       | 0 | (d) | $\frac{1}{2}$ |

107. The value of the integral

(a) 
$$\log \frac{e^4 \underline{\ddot{o}}}{\xi_3 \underline{\sigma}^{\div}}$$
 (b)  $4 \log \frac{e^3 \underline{\ddot{o}}}{\xi_4 \underline{\sigma}^{\div}}$ 

(c) 
$$4 \log_{\frac{1}{2}3} \frac{94}{3} \frac{\ddot{0}}{\dot{2}}$$
; (d)  $\log_{\frac{1}{2}} \frac{93}{4} \frac{\ddot{0}}{\dot{2}}$ ;

108. If a tangent having slope of 
$$-\frac{4}{3}$$
 to the ellipse

 $\frac{x^2}{18} + \frac{y^2}{32} = 1$  intersects the major and minor axes

in points A and B respectively, then the area of OAB is equal to (O is the centre of the ellipse)

- (a) 12 sq units (b) 48 sq units
- (c) 64 sq units (d) 24 sq units

109. The locus of mid points of tangents intercepted

between the axes of ellips  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  will be

(a) 
$$\frac{g^2}{\chi^2} + \frac{b^2}{\gamma_2} = 1$$
 (b)  $\frac{g^2}{\chi^2} + \frac{b^2}{\gamma_2} = 2$ 

(c) 
$$\frac{2}{-2} + \frac{b^2}{2} = 3$$
 (d)  $\frac{2}{-2} + \frac{2}{-2} = 4$ 

110. If PQ is a double ordinate of hyperbola

 $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ . Such that *OPQ* is an equilateral triangle, O being the centre of the hyperbola, then the eccentricity 'e' of the hyperbola satisfies

(a) 
$$1 < e < \frac{2}{\sqrt{3}}$$
 (b)  $e = \frac{2}{\sqrt{3}}$   
(c)  $e = \frac{\sqrt{3}}{2}$  (d)  $e > \frac{2}{\sqrt{3}}$ 

- 111. AB& sidee AB, BC and CA of a respectively 3, 4 and 5 points lying on them. The number of triangles that can be constructed using these points as vertices is

  (a) 205
  (b) 220
  (c) 210
  (d) None of these
  - (d) 1000 of 1000 a+bx
- 112. In the expansion of  $\frac{1}{ex}$ , the coefficient of x r is

(a) 
$$\frac{a \cdot b}{r!}$$
 (b)  $\frac{a \cdot br}{r!}$ 

(c) 
$$(-1)^r \frac{a-br}{r!}$$
 (d) None of these

114. *P* is a fixed point (a, a, a) on a line through the

(b) 0

(d) -1

(b)  $\frac{3}{2a}$ 

(d) None of these

origin equally inclined to the axes, then any plane through *P* perpendicular to *OP*, makes intercepts on the axes, the sum of whose reciprocals is

117. If 
$$f(x) = \begin{bmatrix} 1 & |\sin x| \\ 1 + & |\sin x| \end{bmatrix}^{\sigma/|\sin x|}$$
,  $-\frac{p}{6}x < 0$   
 $b$ ,  $y \in x_{0}^{-}$ , then  
 $\lim_{x \to 0} 2x^{2}$ ,  $\frac{p}{6}$ 

the value of a and b, if f is continuous at x = 0, are respectively.

(a)  $\frac{2}{3}, \frac{3}{2}$  (b)  $\frac{2}{3}, e^{2/3}$ (c)  $-, e^{3/2}$  (d) None of these

118. The domain of the function

$$f(x) = \frac{1}{\log 10(1-x)} \quad \sqrt[4]{x+2} \text{ is}$$
(a) ] 3, 2.5 2.5,
(b) [2,0 0,1[

II3. If 
$$n = (1999) \prod_{x=1}^{1999}$$
 then alog *nx* is equal to he solution of the differential equation

$$(1+y^2) + (x e \tan^1 y) \frac{dy}{dx}$$
 0, is

(a)  $(x-2) = Ketan^{-1}y$ 

(c) ]0, 1[

(b) 
$$2xe^{\tan 1 y} = e^2 \tan (-1)y + K$$

(c) 
$$xe \tan - 1y = \tan - 1y + K$$

(d) xe2tan-1y = etan-1y + K

120. If the gradient of the tangent at any point (x, y)

is 
$$\begin{array}{c} \overset{ii}{y} - \sin 2 \overset{ii}{e} \overset{iii}{x} \overset{iii}{y} i$$
, then equation of the curve is  
(a)  $y = \operatorname{cot}_{\downarrow}^{\zeta_{-1}} e^{x}$   
(b)  $y = \operatorname{cot}_{\downarrow}^{-1} \overset{ii}{e} \operatorname{log} e^{\frac{x \ddot{0}}{e}} \frac{e^{\dot{1}}}{e^{\dot{1}}} \frac{e^{\dot{1}}}{e^$ 

(c)  $\frac{a}{2}$ 

(a) 1

equal to

(a) a

(c) 19991999

115. For which of the following values of m, the area of the region bounded by the curve  $y = x - x^2$ 

and the line y = mx equals  $\frac{9}{2}$ (a) (c) -4 (b) -2 If  $f: \hat{R}$  (d) 4 116. R be such that f(1) = 3 and f(1) = 6. Then,  $\lim_{\mathbb{R}} \int_{\hat{H}}^{\hat{T}} \frac{f(1+x)\ddot{u}\ddot{t}}{f(1)} \int_{\hat{V}}^{1/x}$  equals to (a) 1 (b) e1/2(c) e2 (d) e3

## SOLUTION S

6.

7.

8.

9.

#### PART - I (PHYSICS)

1. (d) As we know, velocity of electromagnetic

wave, 
$$c = \frac{1}{\sqrt{0}} = 3 \times 108 \text{ m/s}$$

It is independent of amplitude of electromagnetic wave, frequency and wavelength of electromagnetic wave.

2. (b) According to Moseley's law  $\sqrt{z} = a(z - b)$ or v = a2(z - b)2

or 
$$\frac{c}{-} = a^2 (z - b)^2$$

$$\frac{-\frac{1}{2}}{\frac{(z_2 \ 1)^2}{(z_1 \ 1)^2}}$$
Here 1 = ,, 2 = 4, z1 = 11 and z2 = ?  

$$\frac{-\frac{1}{2}}{\frac{(z_2 \ 1)^2}{(11 \ 1)^2}}$$
or (z2 - 1)<sup>2</sup> = 25 or z2 = 6

1

$$=\frac{1}{2}$$
 (ene nnn)

- = 1.6 × 10–19 [0.36 + 0.17] (2.5 × 1019)] = 2.12 Sm–1
- 4. (d) If a radio receiver amplifies all the signal frequencies equally well, it is said to have high fidelity.

5. (b) Given, y = 3 sin 
$$\frac{t}{2} \frac{x}{4}$$

$$= 3 \sin \frac{t}{2} \frac{x}{4}$$

Comparing it with standard equation

$$y = r \sin \frac{2}{\sqrt{vt}} (vt \quad x)$$
  
= rsin  $\frac{2 vt}{\sqrt{2x}} \frac{2 x}{\sqrt{2t}}$   
We have,  $\frac{2 v}{\sqrt{2t}} \frac{2}{\sqrt{2t}} or v = \frac{1}{4}$ 

and 
$$\frac{2}{4}$$
 or = 8 m v =  $\frac{8}{4}$  = 2 m/s

So, the distance travelled by wave in t second = vt = 2 × 5 = 10 m (a) Gravitational intensity,

$$I = \frac{dv}{dx} \qquad \frac{d}{dx} \frac{k}{x2} \qquad \frac{2k}{x3}$$

(d) For Cu wire, 
$$L = 2.2 \text{ m}$$
,  $r1 = 1.5 \text{ mm}$   
=  $1.5 \times 10-3 \text{ n}$   
Y =  $1.1 \times 119 \text{ N/m}^2$   
For steel wire,  $2 = 1.6 \text{ m}$ ,  $r2 = 1.5 \text{ mm}$   
=  $1.5 \times 10-3 \text{ m}$   
Y =  $2.0 \times 1011 \text{ N/m}2$   
Let F be the stretching force in both the wires the

For Cu wire, Y1 = 
$$\frac{F}{r_1^2}$$
  $\frac{l_1}{l_1}$   
F =  $\frac{Y1r_1^2}{l_1}$ 

$$= \frac{1.110^{-11}}{2.2} \frac{22}{7} \times (1.5 \times 10^{3} \times 0.5 \times 103)$$
$$= 1.8 \times 102 \text{ N}$$

(a) Mean speed, 
$$v = \sqrt{\frac{8kT}{m}} = 0.92v_{rms}$$
  
rms speed, vrms  $\sqrt{\frac{3kT}{m}}$   
Most probable speed  $v_p$ 

$$=\sqrt{\frac{2KT}{m}}$$
 0.816vrms

(b) Let two balls collide at a height s from the ground after t second when second ball is thrown upwards.
Time taken by first ball to reach the pair

Time taken by first ball to reach the point of collision = (t + 2) s

$$s = 39.2 (t + 2) + \frac{1}{2} (-9.8) (t + 2)2$$

= 39.2 (t + 2) - 4.9 (t + 2)2...(i)For second ball s =  $39.2t + \frac{1}{2} (-9.8) t2$ = 39.2t - 4.9 t2 ...(ii)From eqs. (i) and (ii) 15 39.2 (t + 2) - 4.9 (t + 2)2 = (39.2) t - 4.9 t2On solving we get, t = 3sFrom Eq. (ii), s =  $39.2 \times 3 - 4.9 \times (3)2 = 117.6 - 44.1 = 73.5$  m

10. (b)Magnetic flux, = B.A = 
$$\frac{F}{I}$$
.A  
=  $\frac{[M^{1}L^{-1}]L^{2}}{[A.L]}$  = [M1 L2 T-2 A-1]

$$=\frac{1}{T^2} T^2$$

12. (d) Given,  $U = \frac{M}{r6} \frac{N}{r12}$   $F = \frac{du}{dr} \frac{dM}{dr} \frac{N}{r6} \frac{N}{r12}$   $= \frac{6M}{r^7} \frac{12N}{r^{13}} = \frac{6M}{r^7} \frac{12N}{r13}$ For equilibrium position, F = 0 $\frac{6M}{r^7} \frac{12N}{r^{13}} \text{ or } r \stackrel{6}{=} \frac{2N}{M}$ 

Hence, U = 
$$\frac{M}{(2N/M)} \frac{N}{(2N/M)^2} \frac{M^2}{4N}$$

13. (b) Total number of revolutions = area under n-t graph

$$= \frac{1}{2} 8 \frac{1800}{60} 8 \frac{600}{60} \frac{1}{2} 16 \frac{600}{60}$$
$$= 120 + 80 + 80 = 280$$

14. (c) From the graph we can say, upto t = 2.0 s, the body moves with a constant velocity

> Slope of position-time graph =  $\frac{4}{2}$  = 2m/s After t = 2.0 s, position-time graph is parallel

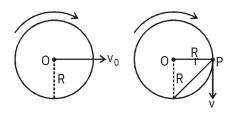
to time axis i.e., body comes to rest. Change in velocity = dx = 2 m/s Impulse = Change in momentum = mdv = 0.1 × 2 = 0.2 kg m/s

15. (d) Pressure = 
$$\frac{\text{force}}{\text{area}} = \frac{F}{L^2}$$

or

$$\frac{p}{p} = \frac{F}{F} = \frac{2 L}{L} = 4\% + 2 (2\%)$$

16. (d) The situation can be shown as



 $\sqrt{2}v_{n}$ 

Here v0 = R  
At. P, v = r  
= 
$$\sqrt{(R2 R2)} \sqrt{2R}$$

17. (b) Using principle of conservation of linear momentum,  $3m \times v = (m - 60)2 \times (-60)2$ 

$$= m 60 \sqrt{2}$$

18. (a) Common velocity,  $v = \frac{m1v1 m2v2}{m1 m2}$ 

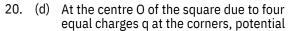
$$=\frac{2 \ 6 \ 2 \ 0}{2 \ 2} = 3 \text{ m/s}$$

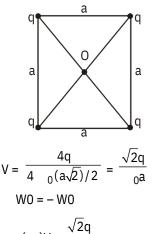
Initial kinetic energy (E1)

$$= \frac{1}{2}m_{1}y^{2} + \frac{1}{2}m_{2}v_{2}^{2} + \frac{1}{2} + 2 + (6)^{2} = 36J$$
$$= -(m_{1} + m_{2})V^{2} + \frac{1}{2}(2 + 2)(3)^{2} = 18J$$
Heat evolved =  $(36 - 18)J = 18J$ 

19. (a) From given condition

$$\frac{\text{Gmm}}{(2R)^2} \quad \frac{\text{mv2}}{\text{R}}, \text{v} \quad \frac{\text{Gm}}{4R} \quad \frac{1}{2}\sqrt{\frac{\text{Gm}}{R}}$$





$$(-q)V = \frac{\sqrt{2q}}{0a}$$

21. (a) In the steady state, current through capacitor

Using Kirchhof's voltage law to the circuit ACD We have,  $10 - 2 + 1 \times R + 1 \times 2 = 0$ or R = 10Potential difference across C and D V C - VD =  $2 \times 1 = 2V$ As V D =  $2 \times 1 = 2V$ So, V Potential difference across capacitor = 4 - 2 = 2VCharge on capacitor Q = CV =  $2F \times 2 = 4C$ 

22. (a) KE of an electron in nth orbit : K<sup>n</sup>  $\frac{1}{n^2}$ 

and PE of an electron in nth orbit :

$$U_n = \frac{1}{n^2}$$

When an electron passes from state n = 2 to n = 1

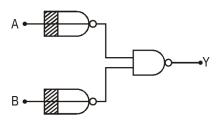
$$\frac{K}{2} \quad \frac{l^2}{2^2} \quad \frac{1}{4}$$

$$K$$

$$1$$

or K1 = 4K2  
U2  
U1  
or U 
$$\frac{l^2}{2^2} \frac{1}{4}$$

23. (b) To obtain OR gate from NAND gates we need two NOT gates obtained from NAND gates and one NAND gate as figure.



Boolean expression =  $\overline{A.B.} = \overline{\overline{A}} = \overline{\overline{B}}$ 

= A + B OR gate

24. (b)Magnetic field B = 
$$\frac{0}{4} \frac{2 I}{r}$$

Here, 2 =

$$\mathsf{B} = \frac{0}{4} \frac{\mathsf{I}}{\mathsf{r}}$$

25. (a) Since axes are perpendicular so mid point lies on axial line of one magnet and on equitorial line of other magnet

$$B_{1} = \frac{0}{4} \frac{2M}{d^{3}} = \frac{107 \ 2 \ 1}{1^{3}} = 2 \times 10^{7} \text{ T}$$

and B = 
$$\frac{0}{4} \frac{M}{4d^3} = \frac{107}{13} = 10-7T$$

As B1 B2 Resultant magnetic field  $= \sqrt{B^2 B^2 J^2} \sqrt{5107T}$ 26. (a) In the given circuit, two condensors and the inductor are in series. Ls = L + L = 2Land  $\frac{-1}{Cs} \frac{1^2}{C} \frac{-2}{C} Cs \frac{-C}{2}$ Natural frequency of the circuit  $v = \frac{1}{2\sqrt{L_sC_s}} \frac{-1}{2\sqrt{2L}\sqrt{C/2}}$   $= \frac{1}{2\sqrt{LC}}$  27. (a) In the beginning due to gravity pull, the 32. (b) In an isobaric process, p = constant lead shot will be accelerated and hence will move, with increasing velocity for some time When the viscous force balance the gravity pull, then the shot will move with constant velocity. As in the beginning, the velocity of shot is not fully linear with the effective distance covered by the shot. Γ

28. (b) Refractive index of a medium = 
$$\sqrt{\frac{1}{0.0}}$$

29. (c) Lens formula, 
$$\frac{1}{v} = \frac{1}{u} = \frac{1}{f}$$
  
or  $\stackrel{U}{\forall} = 1 = \frac{1}{m}$   
 $\frac{1}{m} = 1 = \frac{u}{f}$   
or  $\frac{1}{m} = \frac{1}{f} = u = 1$ 

this is the equation of a straight line whose slope

$$\frac{1}{f} \quad \frac{b}{c} \qquad f = \frac{c}{b} \qquad 35.$$

30. (d) Amplitudes A1 and A2 are added as vectors. Angle between the two vectors is the phase difference (1-2) between them. Resultant wave,

$$R = \sqrt{A2} \quad A22 \quad 2A1A2\cos(1 \quad 2)$$
  
hc

31. (a) Here, case (i) 
$$e(3V0) = - 0$$
 ...(i)

Case (ii) 
$$eVO = \frac{hc}{2} = 0$$
 ...(ii)  
From eqs. (i) and (ii),  
 $\frac{3hc}{2} = 3 = 0$   
or  $\frac{3hc}{2} = \frac{hc}{3} = 3 = 0$   
or,  $O = \frac{hc}{4}$   
Threshold wavelength  
 $_{0} = \frac{hc}{0} = \frac{h}{c} = 4 = 4$   
h

С

Hence, V Т

i.e., V = 
$$\frac{nR}{P}$$
 T

V–T graph is a straight line with  $slope_{D}$ 

(slope)2 > (slope)1  $n^2 < n^1$ 

$$U = 2 \frac{n1}{2}RT - 4 \frac{n2}{2}RT$$

For 02, n = 5 and for Ar, n2 = 3

$$U = 2 \frac{5}{2}RT - 4 \frac{3}{2}RT = 11RT$$

- 34. (b) Given, speed of each pulse = 2 cm/s Therefore distance travelled by both pulses in 2s = 4 cm toward each other. On their superposition, the resultant displacement at every point will be zero. Hence, total energy will be purely kinetic.
  - (d) Time interval between two successive maxima = time interval between two

successive beats = 
$$\frac{1}{n_1 \quad n_2}$$

36. (b) Here, 
$$h = \frac{2s \cos 0}{r g} \frac{2s}{r g}$$
 ...(i)

According to question,

Dividing eq. (ii) by (i) we get,

$$\frac{1}{2} \cos \\ \text{or} = 60^{\circ} \\ 37. \quad \text{(a)} \quad \text{Given, V 1 = V2 = 300V; V3 = ?, i = ?} \\ \text{As, V = } \sqrt{V_3^2} \quad \frac{(V_1 \quad V_2)^2}{(V_3^3 \quad V_7^2)^3} = 220V \\ 220 = \sqrt{V_3^2} \\ I = \frac{V3}{R} = \frac{22}{0} = 2.2A \\ 10 \\ 0 \end{bmatrix}$$

38. (b) We have, W =  $-MB(c\mathbf{Q} \le \cos 1)$ So, W1 =  $-MB(\cos 90^\circ - \cos 0^\circ) = MB$  $2 = -MB(\cos 60^\circ - \cos 0^\circ) = \frac{1}{2}MB$ As W1 = nW2  $n = \frac{W1}{W_2} = \frac{MB}{\frac{1}{2}MB} = 2$ 

39. (b) Capacitance, C = 
$$\frac{0^A}{d}$$

As one–fourth of capacitor is filled with dielectric of constant K, then,

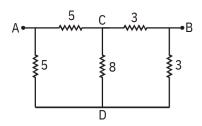
$$C1 = \frac{K_0 A / 4}{d}$$

=

and C2 =  $\frac{3A/4}{d}$ Both C<sub>1</sub> and C2 are in parallel.

$$CP = C1 + C2 = \frac{K_{0}A}{4d} = \frac{3_{0}A}{4d}$$
(K + 3)  $\frac{0^{0}A}{4d}$  (K = 3)  $\frac{C}{4}$ 

40. (c) The equivalent circuit of the given circuit is

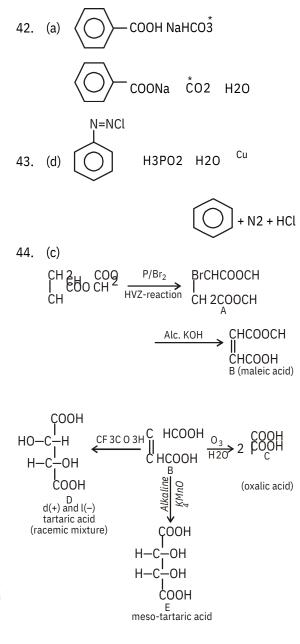


This is a balanced Wheatstone bridge. Therefore, the arm CD becomes in **eteres** and 3 are in series and they together are in parallel with (5 + 3)

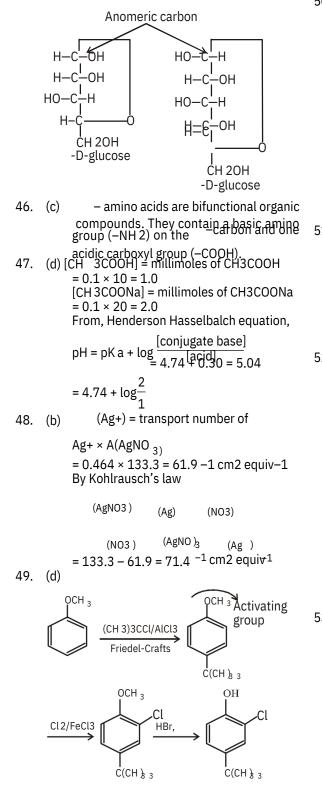
Net resistance =  $\frac{(5 \ 3 \ (5 \ ^3)}{(5 \ )} \ (5 \ ^3) \ 4$ 

#### PART - II (CHEMISTRY)

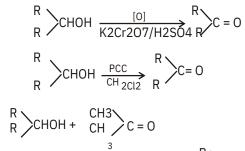
 (a) Benzoin condensation is performed by aromatic aldehydes (i.e., compounds in which –CHO group is directly attached with benzene ring).



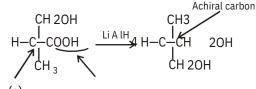
45. (d)When two cyclic forms of a carbohydrate differ in configuration only at hemiacetal carbons, they are said to be anomers. Thus, anomers are cyclic forms of carbohydrates that are epimeric at hemiacetal carbon and this carbon (C-1 of aldose) is called anomeric carbon, e.g.,



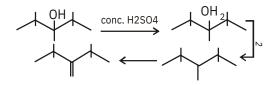
50. (c) Oxidation of Ketones, yield secondary a l coh ol

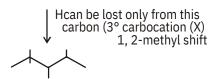


$$[(CH)_{3}CO] = C$$



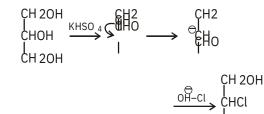
52. (a)



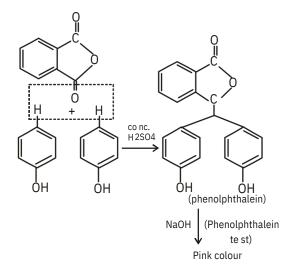


(3° carbocation (Y))

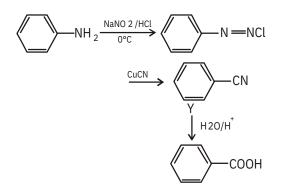
Y is less soluble than (X) due to lack of symmetry Chiral carbon. This is reduced to —CH 2OH



54. (a)



55. (d)



- 56. (a) According to Van–Arkel method, pyrolysis of BI<sup>3</sup> is carried out in the presence of red hot W or Ta filament.
  - 2BI<sub>3</sub> Red hot w or Ta filament 2B + 3I2

0

0

58. (b) Peroxy acids contain 
$$-0-0$$
 linkage.

H2SO<sub>5</sub> HO-SHO-O-H  
H2S2O<sub>8</sub> HO-SHO-O-H  
H2S2O<sub>8</sub> HO-SHO-O-SHO  
59. (d) Volume of one molecule  

$$= \frac{4}{3} r^{\frac{2}{3}} \frac{4}{3} (1.54 \times 10-8)3 \text{ cm}3$$

$$= 1.53 \times 10-23 \text{ cm}3$$
Volume of molecules in 1.65 g Ar  

$$= \frac{1.65}{40} N_0 \quad 1.5310 \quad {}^{23} = 0.380 \text{ cm}3$$
Volume of solid containing 1.65 g Ar = 1 cm3  
Empty space = 1 - 0.380 = 0.620  
Per cent of empty space = 62%  
60. (d) In adiabatic expansion  

$$\frac{T2}{T1} \frac{V}{1} \int_{1}^{1} \text{ for CO } \frac{1}{2} (\text{triatomic gas}) \text{ is,}$$

$$= 1.33^{2}$$

$$\frac{150}{300} \frac{10}{V2} \int_{2}^{0.33} \frac{10}{V2}$$

$$\frac{1}{2} \int_{1}^{0} \frac{10}{V_{2}} \int_{1}^{0.33} \frac{10}{V_{2}} \int_{1}^{0} \frac{10}{V_{2}} \int_{1}^{0.33} \frac{10}{V_{2}} \int_{1}^{0} \frac{10}{V_{2}} \int_{1}^{0.33} \frac{10}{V_{2}} \int_{1}^{0} \frac{1}{2} \int_{1}^{0} \frac{10}{V_{2}} \int_{1}^{0.33} \frac{10}{V_{2}} \int_{1}^{0} \frac{1}{2} \int_{1}^{0} \frac{10}{V_{2}} \int_{1}^{0.33} \frac{10}{V_{2}} \int_{1}^{0} \frac{1}{2} \int_{1}^{0} \frac{10}{V_{2}} \int_{1}^{0.33} \frac{1}{2} \int_{1}^{0} \frac{10}{V_{2}} \int_{1}^{0} \frac{1}{2} \int_{1}^{0} \frac{1}{V_{2}} \int_{1}^{0$$

о \_\_\_\_ -S\_\_\_ОН

HO

Ö

H2S2O<sub>4</sub>

$$V = a + V_{0}$$
If ester is 50% hydrolysed then,  $x = \frac{a}{2}$ 
or  $V = \frac{a}{2}$ 
 $V_{0}$ 
or  $a = 2Vt - 2V0$ 
 $V = 2V - 2V0 + V0$ 
 $= 2Vt - 2V0 + V0$ 
62. (b) Energy values are additives.  
 $E = E1 + E2$ 
67. (a)
$$\frac{hc}{n} = \frac{hc}{n} = \frac{hc}{2}$$

$$\frac{1}{3007602}$$

$$\frac{111}{2} = \frac{111}{300760}$$

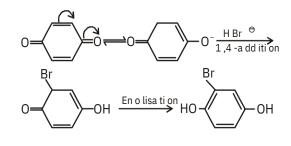
$$= 495.6 \text{ nm} = 496 \text{ nm}$$
68. (a)
63. (a) I. Fe2+ = Ar  $1 = 1 = 1 = 1$ 
3d<sup>6</sup>
4 unpaired electrons, Coloured ion, II. Ni2+ = Ar  $1 = 1 = 1$ 

$$3d^{8}$$
2 unpaired electrons, Coloured ion III. Al3+ = [Ne]
No unpaired electron in 3d, colourless ion.
64. (b) CH 3C  $N$ : CH 3C  $= N$ :
$$e = c \text{ tro ph ili c n ucle o ph ilic}$$
65. (c)
$$(C = 12/FeCI3)$$

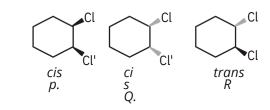
$$(C$$

Ŷ

66. (d)



67. (a)

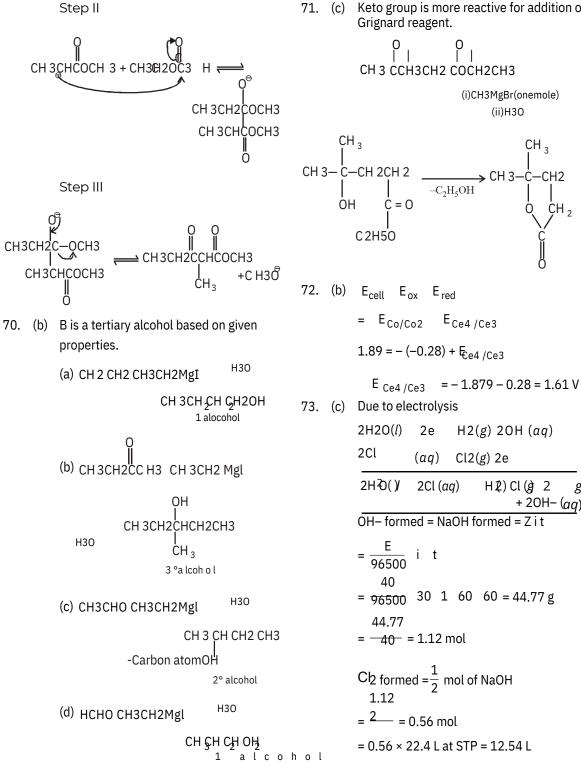


R– -O-R –O oxygen atom can donate lone pair of electron more easily, therefore, it is more basic than -oxygen.

(d)When two molecules of an ethylacetate undergo condensation reaction, in presence of sodium ethoxide involving the reaction is called as Claisen condensation and product is a -keto ester.

$$CH_3CH_2C CH COCH_3 + CH_3OH$$

Mecha n ism



71. (c) Keto group is more reactive for addition of

CH ,

-CH2

ĊΗ 2

g

+ 20H- (aq)

= 0.56 × 22.4 L at STP = 12.54 L

74. (b) K B = Ae Ea/RT  
= 1012 × 4.35 × 10-8  
= 4.35 × 104 s-1  
Also equilibrium constant, k = 
$$\frac{k_A}{k_B}$$
 = 104  
 $k_{\overline{A}}$  k B × 10<sup>4</sup> = 4.35 × 10<sup>8</sup> s<sup>-1</sup>  
75. (a) G = H - nFT  $\frac{dE}{dT}_{P}$   
and G = T - TS  
 $\frac{S}{nF} \frac{dE}{dT}_{P}$   
or  $\frac{96.5}{2\,96500} \frac{dE}{dT}_{P}$   
 $\frac{dE_{cell}}{dT}_{P} \frac{1\,10^3}{2} = 5 \times 10-4 \text{ VK}-1$ 

76. (c)We have to compare wavelength of transition in the H-spectrum with the Balmer transition n = 4 to n = 2 of He+ spectrum.

H = <sub>He</sub>

 $En = \frac{R H Z^2}{n^2}$ where, Z = atomic number, n2 = degeneracy  $R_{...}(1)^{2}$ 

For H-atom, En = 
$$\frac{R_{H}(1)}{n^{2}}$$
  
 $\frac{RH}{9} = \frac{R_{H}}{n^{2}}$ 

(d)

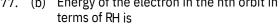
79. (c)

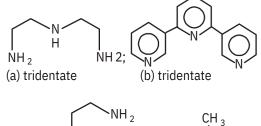
n2 = 9

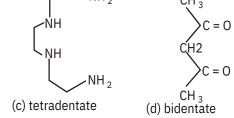
| 78. | (d) |                               |   |   |
|-----|-----|-------------------------------|---|---|
|     |     | Compound Symbol               |   | Uses  |
|     |     |                               | formla  |   |
|     | A.  | Dry ice                       | CO <sup>2</sup>                                       | Referigerant<br>for preserving<br>food        |
|     | В.  | Semicon<br>du ct or<br>Solder | Ge  | Electronic diode<br>and triode in<br>computer |
|     | C.  | TEL                           | Sn/Pb   | Joining circuits                              |
|     | D.  | (C 2H5)4 Pt                   | Antiknocking<br>compound for<br>petroleum<br>products |   |

 $RHZH^{2} \frac{1}{n_{1}^{2}} \frac{1}{\frac{2}{n_{2}^{2}}} R_{H}Z_{He}^{2} \frac{1}{2^{2}} \frac{1}{4^{2}}$ 1  $\frac{1}{n_{\perp}^2}$   $\frac{1}{n_{2}^2}$  4  $\frac{1}{4}$   $\frac{1}{16}$  $\frac{1}{n_1^2}$   $\frac{1}{n_2^2}$  4  $\frac{4}{16}$  $\frac{1}{n_1^2} \frac{1}{n_2^2} \frac{3}{4}$ If n1 = 1, then n2 = 2, 3, .... For first line n2 = 2, n1 = 1 $\frac{1}{1^2} \ \frac{1}{2^2} \ \frac{1}{1} \ \frac{1}{4} \ \frac{3}{4}$ 

Den2eotn1asj1ionilhgive spectrum of the same wavelength as that of Balmer transition, n = 4 to n = 277. (b) Energy of the electron in the nth orbit in







80. (b) Effective atomic number EAN = Atomic number - oxidation number + 2 × coordination number For [Al (C2O4)33-Z = 13 ON = 3 CN = 6  $EAN = 13 - 3 + 2 \times 6 = 22$ 

## PART - III (MATHEMATICS)

P(B)  
81. (a) 
$$A = \{x : |x| < 3, y\}$$
  
 $A = \{x : -3 < x < 3, x \ 1\} = \{-2, -1, 0, 1\}$   
 $A = \{x : -3 < x < 3, x \ 1\} = \{-2, -1, 0, 1\}$   
 $A = \{x : -3 < x < 3, x \ 1\} = \{-2, -1, 0, 1\}$   
 $A = \{x : -3 < x < 3, x \ 1\} = \{-2, -1, 0, 1\}$   
 $R = \{(-2, 2), (-1, 1), (1, 1), (0, 0), (2, 2)\}$   
85. (a) 2 tan<sup>-1</sup>  
82. (b)  $\frac{dy}{dx} \frac{yf(x)}{f(x)} \frac{y^2}{f(x)}$   
 $yf(x) dx - f(x) dy = y2 dx$   
 $\frac{yf(x) dx - f(x) dy}{y^2} = dx$   
 $d \frac{f(x)}{y} = dx$   
 $2 tan
On integration, we get
 $\frac{f(x)}{y} = x + C$   
 $f(x) = y (x + C)$   
83. (a) Let  $= \begin{vmatrix} x & 2 & x & 3 & x & 2a \\ x & 4 & x & 5 & x & b \end{vmatrix}$   
 $= 2 \frac{1}{x} \begin{vmatrix} x & 2 & x & 3 & x & 2a \\ 0 & 0 & 2(2b \ a \ c) \end{vmatrix}$   
 $= 2 \frac{1}{x} \begin{vmatrix} x & 2 & x & 3 & x & 2a \\ 0 & 0 & 2(2b \ a \ c) \end{vmatrix}$   
 $= 2 \frac{1}{x} \begin{vmatrix} x & 2 & x & 3 & x & 2a \\ 0 & 0 & 2(2b \ a \ c) \end{vmatrix}$   
 $= 2 \frac{1}{x} \begin{vmatrix} x & 2 & x & 3 & x & 2a \\ 0 & 0 & 2(2b \ a \ c) \end{vmatrix}$   
 $= 2 \frac{1}{x} \begin{vmatrix} x & 2 & x & 3 & x & 2a \\ 0 & 0 & 2(2b \ a \ c) \end{vmatrix}$   
 $= 2 \frac{1}{x} \begin{vmatrix} x & 2 & x & 3 & x & 2a \\ 0 & 0 & 0 & 2(2b \ a \ c) \end{vmatrix}$   
 $= 2 \frac{1}{x} \begin{vmatrix} x & 2 & x & 3 & x & 2a \\ 0 & 0 & 0 & 2(2b \ a \ c) \end{vmatrix}$   
 $= 2 \frac{1}{x} \frac{1}{x} \frac{2 & x & 3 & x & 2a \\ 0 & 0 & 0 & 2(2b \ a \ c) \end{vmatrix}$   
 $= 0$   
 $= 2 \frac{1}{x} \frac{1}{x} \frac{2 & x & 3 & x & 2a \\ 0 & 0 & 0 & 2(2b \ a \ c) \end{vmatrix}$   
 $= 0$   
 $= 2 \frac{1}{x} \frac{2}{x} \frac{2}{x} \frac{3}{x} \frac{2}{x} \frac{2}{x} \frac{3}{x} \frac{2}{x} \frac{2}{x}$$ 

$$P(B) P(A = B) = \frac{3}{4}$$

$$\frac{5}{12} P(B) \frac{3}{4}$$
(a)  $2 \tan^{-1}(\operatorname{cosec}\tan^{-1}x - \tan \cot^{-1}x)$ 

$$= 2 \tan^{-1}(\operatorname{cosec}\operatorname{cosec}^{-1}\frac{\sqrt{1 \times 2}}{x})$$

$$\tan \tan^{-1}\frac{1}{x}$$

$$= 2 \tan^{-1} \frac{\sqrt{1 \times 2}}{x} \frac{1}{x}$$

$$= 2 \tan^{-1} \frac{\sqrt{1 \times 2}}{x} \frac{1}{x}$$

$$= 2 \tan^{-1} \frac{\sec - 1}{\tan} (\operatorname{put} x = \tan )$$

$$= 2 \tan^{-1} \frac{1 \cos}{\sin}$$

$$= 2 \tan^{-1} \frac{2\sin 2}{2\sin 2}$$

$$= 2 \tan^{-1} \tan 2$$
(b)  $\frac{2 \sin^{-1} \tan 2}{2}$ 
(c)  $\frac{2 \sin^{-1} \tan 2}{2}$ 
(c)  $\frac{2 \sin^{-1} \tan 2}{2}$ 
(c)  $\frac{2 \sin^{-1} \tan^{-1} x}{x}$ 
(c)  $\frac{2$ 

Truth value of  $\sim$  ( $\sim$ p q) is F.

88. (c) Surface area of sphere, S = 4r2and  $\frac{d}{r} = 2$  $d_{\text{eff}}^{\text{glt}}$  4  $2r \frac{d}{d}$  8 r 2 16 r  $\frac{ds}{dt}$ r 89. (d) For (a, b), (c, d) N × N (a, b) R (c, d) ad (b + c) = bc (a + d)Reflexive : ab(b + a) = ba(a + b), ab N (a, b) R (a, b) So, R is reflexive, Symmetric : ad (b + c) = bc (a + d)bc(a + d) = ad(b + c)cd (d + a) = da (c + b)(c, d) R (a, b) So, R is symmetric. Transitive : For (a, b), (c, d), (e, f)  $N \times N$ Let (a, b) R (c, d), (c, d) R (e, f) ad (b + c) = bc(a + d), cf (d + e) = de (c + f)adb + adc = bca + bcd...(i)and cfd + cfe = dec + def...(ii)On multiplying eq. (i) by ef and eq. (ii) by ab and then adding, we have adbef + adcef + cfdab + cfeab = bcaef + bcdef + decab + defab adcf(b + e) = bcde(a + f)af (b + e) = be (a + f)(a, b) R (e, f) So, R is transitive. Hence R is an equivalence relation. 90. (c) arg  $\frac{z}{z}$  2 3 arg  $\frac{x \ 2 \ iy}{x \ 2 \ iy} = \frac{3}{3}$  $arg(x - 2 + iy) - arg(x + 2 + iy) = \frac{1}{3}$  $\tan^{-1} \frac{y}{x^2}$   $\tan^{-1} \frac{y}{x^2}$   $\frac{3}{3}$  $\frac{4y}{x^2 y^2 4} \sqrt{3}$  $\sqrt{3}(x^2)^2 4y 4\sqrt{3} = 0$ which is an equation of a circle.

$$(a.\underline{a}.a_{2} \ 3)^{1/3} \frac{3}{\frac{1}{a_{1}} \ \frac{1}{a_{2}} \ \frac{1}{a_{3}}}$$

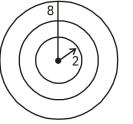
$$(a1.a2.a3) \frac{27}{\frac{1}{a1} \ \frac{1}{a2} \ \frac{1}{a_{3}}^{3}}$$

$$(a.\underline{a}.a_{2}.a_{3}) \frac{1}{a_{1}} \ \frac{1}{a_{2}} \ \frac{1}{a_{3}}^{3} \ 27$$
(b)  $|x2 - x - 6| = x + 2$ , then  
Case I:  $x2 - x - 6 < 0$   
 $(x - 3) (x + 2) < 0$   
 $-2 < x < 3$   
In this case, the equation becomes  
 $x2 - x - 6 = -x - 2$   
or  $x2 - 4 = 0$   
 $x = \pm 2$   
Clearly,  $x = 2$  satisfies the domain of the  
equation in this case. So,  $x = 2$  is a solution  
Case II:  $x2 - x - 60$   
So,  $x - 2$  or  $x$   
In this case, the equation becomes  
 $x2 - x - 6 = 0 = x + 2$   
i.e.,  $x2 - 2x - 8 = 0$  or  $x = -2$ , 4  
Both these values lie in the domain of the  
equation in this case, so  $x = -2$ , 4 are the  
roots.  
Hence, roots are  $x = -2$ , 2, 4.  
(a) Let (h, k) be any point in the set, then  
equation of circle is  
 $(x - h)2 + (y - k)2 = 9$ 

91. (d)We know that, GM HM

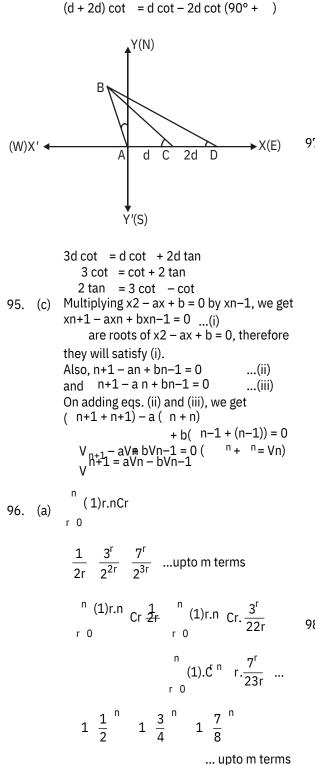
92.

93.



(h, k) lies on  $x^2 + y^2 = 25$ , then  $h^2 + k^2 = 25$  2 Distance between the two circles 8

$$\begin{array}{cccc} 2 & \sqrt{h^2 & k^2} & 8 \\ 4 & h^2 + k^2 & 64 \\ \text{Locus of (h, k) is 4} & (x^2 + y^2) & 64 \end{array}$$



94. (c) By m – n theorem at C

$$\frac{1}{2n}$$
  $\frac{1}{4n}$   $\frac{1}{8n}$  + ... upto m terms

$$=\frac{\frac{1}{2n} \ 1 \ \frac{1}{2^{mn}}}{1 \ \frac{1}{2n}} \quad \frac{2^{mn}}{2^{mn}(2^n \ 1)}$$

97. (c) Angle of intersection between two circles is given by

$$\cos = \frac{r21 r_2^2 d^2}{2r_1r_2} - \frac{\frac{17}{2} 13 \frac{10}{4}}{2\sqrt{\frac{17}{2}} \sqrt{13}}$$

here, 
$$\frac{r}{12} \sqrt{\frac{1}{2}^{2} + \frac{1}{2}^{2}} = \frac{1}{2}^{2} = \frac{1}{2}^{2$$

$$\cos = \frac{19}{\sqrt{442}}$$

or tan = 
$$\frac{1}{19}$$

$$= \tan{-1} \frac{9}{19}$$

98. (a) b1|| a b1 = a (i + j) b2 = b - b1 = (3 - a) i - aj + 4k Also, b 2 . a = 0

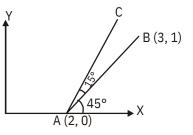
$$(3 - a) - a$$
  $a = \frac{3}{2}$   
 $b1 = \frac{3}{2} (i + j)$ 

x<sub>1</sub> y<sub>1</sub> 1 99. (b) The given matrix is  $x_2$   $y_2$  1  $x_{3} y_{3} 1$ using R<sup>2</sup> R2 - R1, R3 R3 - R1 х ٧ 1 1 1  $= x_2 x_1 y_2 y_1 0 = 0$  $x_3$   $x_1$   $y_3$   $y_1$  0 ( points are collinear i.e., area of triangle = 0)  $\begin{vmatrix} x^2 & x^1 & y^2 & y^1 \\ x^3 & x^1 & y^3 & y^1 \end{vmatrix} = 0$ So, the rank of matrix is always less than 2. 100. (d) On solving the determinant, we have  $1(1 - \cos 2) - \cos (-) [\cos (-)]$  $.\cos] + \cos [\cos .\cos(-)]$ – cos -cos ]  $= 1 - \cos 2 - \cos 2 - \cos 2 ()$  $+2\cos$  .cos .cos ( - )  $= 1 - \cos 2 - \cos 2 + \cos (-)$ [2coscos  $-\cos(-)]$  $= 1 - \cos 2 - \cos 2 + \cos (-)\cos($ +)  $[\cos(+) + \cos(-) - \cos($ -)]  $= 1 - \cos 2 - \cos 2 + \cos 2 \cdot \cos 2$ - sin2 . sin2  $= 1 - \cos 2 - \cos 2 (1 - \cos 2)$ - sin2 .sin2  $= 1 - \cos 2$   $- \cos 2$   $\sin 2$   $- \sin 2$   $\sin 2$  $= (1 - \cos 2) - \sin 2$ sin2 + cos2)  $= \sin 2 - \sin 2 1 = 0$ 101. (b)  $-\sqrt{72}$  52 (7cosx √72 52 5sinx)  $\sqrt{74}$  (2K 1)  $\sqrt{74}$ 8.6 (2K 1) 8.6 - 9.6 2K 7.6 -4.8 K 3.8 So, integral values of K are -4, -3, -2, -1, 0, 1, 2, 3 (eight values) 102. (a) Slope of AB =  $\frac{1}{1}$  $tan = m 1 = 1 or = 45^{\circ}$ 

Thus, slope of new line is tan (45° + 15°)

= tan 60° =  $\sqrt{3}$ ( it is rotated anti-clockwise, so the angle

will be  $45^\circ + 15^\circ = 60^\circ$ )



Hence, the equation is  $y = \sqrt{3}x + c$ But it passes through (2, 0),

So, c =  $-2\sqrt{3}$ 

Thus, required equation is  $y = \sqrt{3}x \quad 2\sqrt{3}$ 103. (a) Solving the equation of line and curve, we get

$$x^{2} \quad 2 \quad \frac{2 \quad 2x}{\sqrt{6}}^{2} = 4$$

$$x2 - \frac{1}{3} \times 4 (1 + x2 - 2x) = 4$$
  

$$3x2 - 4 - 4x2 + 8x = 12$$
  

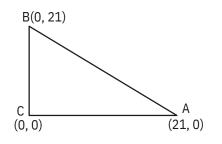
$$x2 - 8x + 16 = 0$$
  

$$(x - 4)2 = 0 \quad x = 4$$
  
and  $\sqrt{6}.y = 2 - 2 (4) = -6$ 

 $y = -\sqrt{6}$ 

Point of contact is  $(4, -\sqrt{6})$ .

104. (b) x + y = 21 The number of integral solutions to the equations are x + y < 21, i.e., x < 21 - y



Number of integral coordinates  
= 19 + 18 + ... + 1  
= 
$$\frac{19(19 \ 1)}{2}$$
  $\frac{19 \ 20}{2}$  = 190  
105. (c) (1 x x <sup>1</sup>)e<sup>x <sup>x</sup> 1</sup>dx  
=  $\begin{bmatrix} x.exx1 & 1 & \frac{1}{x^2} & exx ^{-1} \end{bmatrix}dx$   
[ xf (x) f(x)dx xf(x) C]  
(1 x x1)ex <sup>x 1</sup>dx xe<sup>x x 1</sup> C  
106. (a) f(x) = x - [x], -1 x < 0  
f(x) = x + 1  
When 0 x < 1  
f(x) = x  
1 f(x)dx f(x)dx f(x)dx  
1 0  
=  $\begin{pmatrix} x & 1 \end{pmatrix}dx ^{-1} x dx$   
1 f(x)dx f(x)dx f(x)dx  
1 0  
=  $\begin{pmatrix} x & 1 \end{pmatrix}dx ^{-1} x dx$   
1 0  
=  $\begin{pmatrix} x & 1 \end{pmatrix}dx ^{-1} x dx$   
1 1 2 0  
=  $0 - \frac{(-1)2}{2} - 1 - \frac{1}{2} - 1$   
107. (c)  $\frac{1/2}{1/2} - \frac{x - 1}{x - 1} - \frac{x - 1}{x - 1} - \frac{x - 1}{x - 1} - \frac{1/2}{x - 1} dx$   
=  $\frac{1/2}{1/2} - \frac{x - 1}{x - 1} - \frac{x - 1}{x - 1} - \frac{1/2}{x - 1} dx$   
=  $\frac{1/2}{1/2} - \frac{4x}{x - 2} dx - \frac{1/2}{x - 1} dx$ 

$$= 4 \frac{0}{1/2} \frac{x}{\frac{1}{x} \frac{x^2}{0}} dx \quad 4 \frac{1/2}{0} \frac{x}{\frac{1}{x} \frac{x^2}{x^2}} dx$$
$$= 2\{\log(1 \ ^2)\}_{1/2} \quad 2\{\log(1 \ x^2)\}_{0}^{1/2}$$
$$= 2\log 1 \ \frac{1}{4} \quad 2\log 1 \ \frac{1}{4}$$
$$= 4\log \frac{3}{4} \quad 4\log \frac{4}{3}$$

(i)

$$\frac{x^2}{18} \frac{y^2}{32} = 1$$
$$\frac{x_1^2}{18} \frac{y_1^2}{32} = 1...$$

The equation of the tangent at (x1, y1) is  $\frac{xx_1}{18} \quad \frac{yy_1}{32} = 1.$  This meets the axes at A  $\frac{18}{XT}$ , 0 and B  $0, \frac{32}{YT}$ . It is given that slope of the tangent at (x1, y1) is  $-\frac{4}{3}$ So,  $-\frac{x1}{18}, \frac{32}{YT} = -\frac{4}{3}$   $\frac{x1}{y1} = \frac{3}{4}$   $\frac{x_1}{3} \quad \frac{y_1}{4} = K$  (say) x1 = 3K and y1 = 4K Putting x1, y1 in (i), we get K2 = 1 Area of OAB $\frac{1}{2}$  - OA.OB  $= \frac{1}{2}, \frac{18}{x_1}, \frac{32}{y_1} = \frac{2}{(3K)(4K)} = \frac{24}{K2}$ = 24 sq units (K2 = 1) 109. (d) Let mid-point of part PQ which is in between the axis is R (x 1, y1, 0) then coordinates of P and Q will be (2x (0, 2y1), respectively.

, 2y1), respectively. Equation of line PQ is  $\frac{x}{2x_1} + \frac{y}{2y_1} = 1$ 

$$y = \frac{y_1}{x_1} \times 2y1$$

If this line touches the ellipse

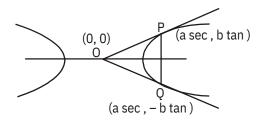
$$\frac{x2}{a2} \quad \frac{y2}{b2} = 1$$

then it will satisfy the condition, c2 = a2m2 + b2

So, 
$$(2y)_{1}^{2} = a^{2} \frac{y_{1}}{x_{1}}^{2} b^{2}$$
  
 $4y_{1}^{2} = \frac{a^{2}y_{1}^{2}}{x_{1}^{2}} b^{2}$   
 $4 = \frac{a^{2}}{x_{1}^{2}} \frac{b^{2}}{y_{1}^{2}} \frac{a^{2}}{x_{1}^{2}} \frac{b^{2}}{y_{1}^{2}} = 4$   
Required locus of (x1, y1) is

$$\frac{az}{x2} \quad \frac{bz}{y2} = 4$$

110. (d) Let P (a sec , b tan ), Q (a sec , - b tan )
be end points of double ordinates and (0, 0) is the centre of the hyperbola.
So, PQ = 2b tan



 $OQ = OP = \sqrt{a^2 \sec^2} b^2 \tan^2$ Since, OQ = OP = PQ

4b2 tan2 = a2sec2 b2tan2  
3b2 tan2 = a2 sec2  
3b2 sin2 = a2  
3a2 (e2 - 1) sin2 = a2  
3 (e2 - 1) sin2 = 1  

$$\frac{1}{3(e^2 - 1)} = sin2 < 1, (sin2 < 1)$$
  
 $\frac{1}{e^2 - 1} = 3e^2 - 1 = \frac{1}{3} = e^2 = \frac{4}{3}$   
 $e > \frac{2}{\sqrt{3}}$   
There are 3 + 4 + 5 = 12 points in a plane  
The number of required triangles

111. (a) There are 3 + 4 + 5 = 12 points in a plane. The number of required triangles = (The number of triangles formed by these 12 points) - (The number of triangles formed by the collinear points) = 12C3 - (C3 + C3 + C5)= 220 - (1 + 4 + 10) = 205112. (c) (a + bx) e-x = (a + bx)

$$1 \frac{x}{1!} \frac{x^2}{2!} \frac{x^3}{3!} \dots (1)n \frac{xn}{n!} \dots$$

The coefficient of xr = a.

$$\frac{(1)^{r}}{r!} \quad b\frac{(1)^{r}}{(r+1)!} = \frac{(1)^{r}}{r!}(a \quad br)$$

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So, its equation is 
$$\frac{x}{1} = \frac{y}{1} = \frac{z}{1}$$
.

A point P on it is given by (a, a, a). So, equation of the plane through P (a, a, a) and perpendicular to OP is 1 (x - a) + 1 (y - a) + 1 (z - a) = 0

( OP is normal to the plane)

i.e., x + y + z = 3a

$$\frac{x}{3a} \frac{y}{3a} \frac{z}{3a} = 1$$

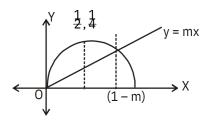
Intercepts on axes are 3a, 3a and 3a, therefore sum of reciprocals of these intercepts.

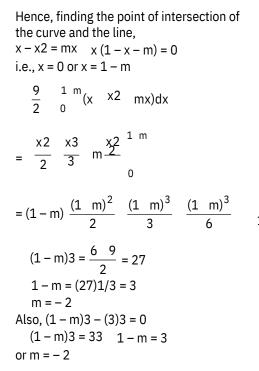
$$=\frac{1}{3a}\quad\frac{1}{3a}\quad\frac{1}{3a}\quad\frac{1}{3a}\quad\frac{1}{a}$$

115. (b) The equation of curve is  $y = x - x^2$  $x^2 - x = y$ 

$$\begin{array}{ccc} x & 2 & -x - y \\ x & \frac{1}{2} & y & \frac{1}{4} \end{array}$$

which is a parabola whose vertex is  $\frac{1}{2}$ ,  $\frac{1}{4}$ 





116. (c) 
$$e^{\lim_{x \to 0^{x}} \frac{f(1 x)}{0 x} \log f(1)]}$$
  
=  $e^{\lim_{x \to 0^{x}} \frac{f(1 x)/f(1 x)}{1}}{e^{f(1)/f(1)}} e^{613} e^{2}$   
117. (b) (1 |sinx)<sup>a/|sinx|</sup>, - x

$$\begin{array}{cccccccc} (1 & |\sin x|^{a/|\sin x|}, & - & x & 0 \\ f(x) & b & , & x & 0 \\ & e^{\tan 2x/\tan 3x} & ,0 & x & - \\ & & & & & 6 \end{array}$$

For f(x) to be continuous at x = 0limf(x) = f(0) = limf(x)x 0 x 0 lim(1 + |sin x|)a / | sinx | x 0  $\lim_{a \to a} |\sin x| |\sin x| = ea$ Now, lime tan2x/tan3x x 0  $\frac{\tan 2x}{2x}$  2x /  $\frac{\tan 3x}{3x}$  3x lime = x 0 <sup>2/3</sup> e<sup>2/3</sup> = lime Since, f(x) is continuous at x = 0. ea = e2/3  $a = \frac{2}{3}$ and  $b = e^{2}/3$ 118. (b) x + 2 0, i.e., x -2 or -2 x log10(1-x) = 01-x 1 x 0 Again, 1 - x > 01 > x x < 1Combining all the results for values of x, we get -2 x < 0 and 0 < x < 1

119. (b) 
$$(1 + y2) + (x e^{\tan^{1}y}) \frac{dy}{dx} = 0$$
  
 $(1 + y2) \frac{dx}{dy} x e^{\tan^{1}y}$   
 $\frac{dx}{dy} \frac{x}{1 y^{2}} \frac{e^{\tan^{1}y}}{(1 y^{2})}$   
 $IF = e^{\frac{1}{1 y^{2}} dy} e^{\tan^{1}y}$   
 $x. e^{\tan^{1}y} = \frac{e^{\tan^{1}y}}{1 y^{2}} \cdot e^{\tan^{1}y} \cdot dy$   
 $x(e^{\tan^{1}y}) \frac{e^{2\tan^{1}y}}{2} c$   
 $2xe^{\tan^{1}y} e^{2\tan^{1}y} K$   
120. (c)  $\frac{dy}{dx} \frac{y}{x} \sin^{2} \frac{y}{x}$   
Put  $y = vx$   $\frac{dy}{dx} v x \frac{dy}{dx}$ 

C = 1  

$$\cot \frac{y}{x} = \log x + \log ee$$
  
 $\cot \frac{y}{x} = \log xe$   
 $y = x \cot^{-1} (\log xe)$