# VITEEE 2008 Question Paper Vellore Institute of Technology Engineering Entrance Examination

# SOLVED PAPER

## VITE EE

2008

PART - I	(PHYSICS)

- Two beams of light will not give rise to an interference patern, if
  - (a) they are coherent
  - (b) they have the same wavelength
  - (c) they are linearly polarized perpendicular to each other
  - (d) they are not monochromatic
- A slit of width 'a' is illuminated with a fmronmo cahromatic light of wavelength distant source and the diffraction pattern is

8, observed on a screen placed at a distance 'D' from the slit. To increase the width of the central maximum one should

d(ae)crease D d(be)crease a d(ce)crease

t(dh)e width cannot be changed

- 3. A thin film of soap solution (n = 1.4) lies on the top of a glass plate (n = 1.5). When visible light is incident almost normal to the plate, two adjacent reflection maxima are observed at two wavelengths 420 and 630 nm. The minimum thickness of the soap solution is
  - (a 420

(b 450 nm ) 1260 nm

ewdhose

- 4. If the6 s3p0eed of a wave doubles as it passes from shallonwm water into deeper water, its wavelength will be
  - (a) (cu) nAc hliagnhgt fr(ebq)uehnaclyv eisd equal to 6 ×
- 5. 1014d oHuzb lies di ncident o(nd ) a qui eatdarlu pwlheodse work function is

2eVh 6.631034Js 1eV 1.6 1019J

The maximum energy of the electrons emitted will be

(a) 2.49

(b) 4.49

(c) eV 0.49 (d) eV

eV

5.49

eV

 An electron microscope is used to probe the atomic arrangements to a resolution of 5Å. What

should be the electric potential to which the electrons need to be a delerated?

(c) 2.5 kV

(d) 5 kV

7. Which phenomenon best supports the theory that matter has a wave nature?

- (a) Electron momentum
- (b Electron diffraction (a) Photon diffraction

The radioactivity of a certain material drops to

 $\frac{11}{16}$  of the initial value in 2 hours. The half life of

this radionuclide is

- (a) 10 min
- (b) 20 min
- (c) 30 min
- (d) 40 min
- 9. An observer 'A' sees an asteroid with a radioactive element moving by at a speed = 0.3 c and mAe. aAsnuorethse trh oeb rsaedrioxtead t'hbeintes dmeocvaiyn

asteroid and measures its decay time as T TA and TB are related as below

- (a) T BT < TA Either (A) or (C) depending on
- BAAh e=>t hTTeBAr the asteroid is approaching or moving away from A
- 10. 2U3 4has 92 protons and 234 nucleons total in its nucleus. It decays by emitting an alpha particle.

  After the decay it becomes
  - (a) 232U

(b) 232Pa

- (c) 230Th
- (d) 230Ra
- 11. K and K x-rays are emitted when there is a transition of electron between the levels
  - (a) n = 2 to n = 1 and n = 3 to n = 1 respectively
  - (b) n = 2 to n = 1 and n = 3 to n = 2 respectively
  - (c) n = 3 to n = 2 and n = 4 to n = 2 respectively
  - (d) n = 3 to n = 2 and n = 4 to n = 3 respectively

12. A certain radioactive material XA starts emitting 18. and particles successively such that the end

product is Z3YA8 . The number of and

particles emitted are

- (b) 2 and 1 respectively
- ) 3 and 4 respectively
- (c) 3 and 8 respectively

In the circuit shown above, an input of 1V is fed into the inverting input of an ideal Op-amp A. The output signal Vout will be

- (a) +10 V
- (b) -10 V
- (c) 0 V
- (d) infinity
- 14. When a solid with a band gap has a donor level just below its empty energy band, the solid is
  - (a) an insulator
  - (b a conductor
  - ) a p-type semiconductor
  - (c) an n-type semiconductor
- - (a) (kT/e) ln (4×1012)
  - (b (kT/e) ln (2.5×1023)
  - (kT/e) ln (1023)
  - (c) (kT/e) ln (109)
- 16. AdZener diode has a contact potential of 1V in the absence of biasing. It undergoes Zener breakdown for an electric field of 106 V/m at the

depletion region of p-n junction. If the width of the depletion region is 2.5 m, what should be the reverse biased potential for the Zener breakdown to occur? (a)3255

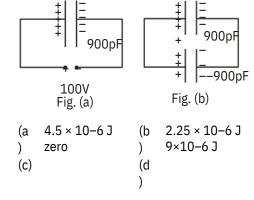
(c) V

(d) V

- 17. In Co1l.p5itt oscillator the fee0d.5back network consVists of V
  - (a) two inductors and a capacitor
  - (b) two capacitors and an inductor
  - (c) three pairs of RC circuit three
  - (d) pairs of RL circuit

3. The reverse saturation of p-n diode

- (a) depends on doping concentrations
- (b depends on diffusion lengths of carriers
- ) depends on the doping concentrations and
- (c) diffusion lengths
- (d) depends on the doping concentrations, diffusion length and device temperature
- A radio station has two channels. One is AM at 1020 kHz and the other FM at 89.5 MHz. For good results you will use
  - (a) longer antenna for the AM channel and shorter for the FM
  - (b)shorter antenna for the AM channel and longer for the FM
  - (c) same length antenna will work for both
  - (d) information given is not enough to say which one to use for which
- 20. The communication using optical fibers is based on the principle of
  - (a) total internal reflection
  - (b) Brewster angle
  - (c) polarization
  - (d) resonance
- 21. In nature, the electric charge of any system is always equal to
  - (a) half integral multiple of the least amount of ch ar ge
  - (b) zero
  - (c) square of the least amount of charge
  - (d) integral multiple of the least amount of ch ar ge
- 22. The energy stored in the capacitor as shown in Fig. (a) is 4.5×10–6 J. If the battery is replaced by another capacitor of 900 pF as shown in Fig. (b), then the total energy of system is



- 23. Equal amounts of a metal are converted into 28. cylindrical wires of different lengths (L) and cross-sectional area (A). The wire with the maximum resistance is the one, which has
  - length = L and area = A
  - length =  $\frac{L}{2}$  and area = 2A
  - (c) length = 2L and area =  $\frac{A}{2}$
  - all have the same resistance, as the amount of the metal is the same
- 24. If the force exerted by an electric dipole on a charge q at a distance of 1m is F, the force at a point 2m away in the same direction will be
  - (a) 2
- F

R

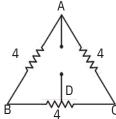
2

R

8 (d)

point D divides the resistance into two equal halves, the resistance between point A and D will be

T eharcehe areres isctoannnceecst eodf 4as shown in figure. If the



- (a) 12
- (b) 6
- (c)
- The resistance of a metal increases with

- increasing temperature because
  (a) the collisions of the conducting electrons

  25. A solid sphere ofisa deinucsl oRse1d abnyd a v hoolullmowe scphhaergree with the electrons increase the collisions of the conducting electrons density with the lattice consisting of the ions of the of radius R with negative surface charge density , such that the total charge in the system is 0 is a positive constant and r is the zdeisrota. nce from the centre of the sphere. The ratio metal increase
  - (dc)) the crease of conduction electrons

the number of conduction electrons in cr eas es

- 30. In the absence of applied potential, the electric current flowing through a metallic wire is zero because
  - (a) the electrons remain stationary
  - the electrons are drifted in random direction with a speed of the order of 10-2 cm/s
  - the electrons move in random direction with (c) a speed of the order close to that of velocity of light
  - electrons and ions move in opposite (d) direction
- (b) -Q, +Q, 0 (d) +Q, 0, 0 (c) 0, -Q, 027. A cylindrical capacitor has charge Q and length L. If both the charge and length of the capacitor are doubled, by keeping other parameters fixed, the energy stored in the capacitor

 $\sqrt{0/2}$  (d)  $\frac{0}{}$ 

26. A solid spherical conductor of radius R has a

spherical cavity of radius a (a < R) at its centre. A

the inner surface, outer surface and at a position

charge + Q is kept at the centre. The charge at

(a) remains same

(a) + Q, - Q, 0

(b) increases two times

r (a < r < R) are respectively

- (c) decreases two times
- (d) increases four times

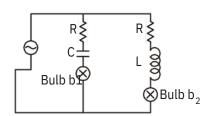
- 31. A meter bridge is used to determine the resistance of an unknown wire by measuring the balance point length I. If the wire is replaced by another wire of same material but with double the length and half the thickness, the balancing point is expected to be

- 32. Identify the INCORRECT statement regarding a superconducting wire
  - (a) transport current flows through its surface
  - (b) transport current flows through the entire
  - (c) area of cross-section of the wire
  - (d) it exhibits zero electrical resistivity and expels applied magnetic field

A sample of HCl gas is placed in an electric field 3×104 NC-1. The dipole moment of each HCl

- 33. molecule is 6×10–30cm. The maximum torque that can act on a molecule is
  - (a)  $2 \times 10-34 \text{ C2Nm}-1(b)2 \times 10-34 \text{ Nm}$
  - (c)  $18 \times 10-26 \text{ Nm}$  (d)  $0.5 \times 1034 \text{ C}-2 \text{ Nm}-1$
- 34. When a metallic plate swings between the poles of a magnet
  - (a) no effect on the plate
  - eddy currents are set up inside the plate and the direction of the current is along the motion of the plate
  - (c) eddy currents are set up inside the plate and the direction of the current oppose the motion of the plate
- (d) eddy currents are set up inside the plate35. When an electrical appliance is switched on, it responds almost immediately, because
  - (a) the electrons in the connecting wires move with the speed of light
  - the electrical signal is carried by electromagnetic waves moving with the speed of light
  - (c) the electrons move with the speed which is
  - (d) close to but less than speed of light

Two thereleatingardestegright bulbs are connected as shown in the Figure. When the circuit is an AC voltage source of frequency f, which of the following observations will be correct?



- (a) both bulbs will glow alternatively
- (b both bulbs will glow with same brightness

provided frequency f  $\frac{1}{2\sqrt{1/LC}}$ 

- (c) bulb b1 will light up initially and goes off,
- (d bulb b2 wwiilll bbelin OkN a ncodn bsutalbn btl2y will be ON
- ) bulb b

)

constantly

- 37. A transformer rated at 10 kW is used to connect a 5kV transmission line to a 240V circuit. The ratio of turns in the windings of the transformer is
  - (a) 5
- (b) 20.8
- (c) 104
- (d) 40
- 38. Three solenoid coils of same dimension, same number of turns and same number of layers of winding are taken. Coil 1 with inductance L1 was

Mound using a Mn wire of resistance 11
2 was wound using the
Coisl i2m wiliatrh winidreu chtuatn tchee L direction of winding was
reversed in each layer; Coil 3 with inductance L

was wound using a superconducting wire. The self inductance of the coils L1, L2, L3 are

- (a) L11 == LL23;= L 2L(8bel))L11 => LL22;> L 3L3 = 0
- (c) L
- 39. Light travels with a speed of 2 × 108 m/s in crown glass of refractive index 1.5. What is the speed of light in dense flint glass of refractive index 1.8.2 (a)
- 40. A parallel beam of fast moving electrons is incident normally on a narrow slit. A screen is placed at a large distance from the slit. If the speed of the electrons is increased, which of the following statement is correct?
  - (a) diffraction pattern is not observed on the screen in the case of electrons
  - (b) the angular width of the central maximum of the diffraction pattern will increase
  - (c) the angular width of the central maximum will decrease
  - the angular width of the central maximum will remain the same

### PART - II (CHEMISTRY)

41.	CH <sub>C</sub> H <sub>3</sub>	HNO <sub>3</sub>	675K
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- (a) CH **3**CCHH22NNOO22 + CH3NO2 (b) CH 23 = N COH22
- (c) 2CH
- (d) CH
- When acetamide is hydrolysed by boiling with acid, the product obtained is:
  - (a) acetic acid
- (b) ethyl amine
- (c) ethanol
- (d) acetamide
- 43. Which will not go for diazotization?
  - (a) C6H5NH2
- (b) C6H5CH2NH2
- (c) H  $HIG2 > C_6H_4$
- ON2
- 44. Secondary nitroalkanes can be converted into ketones by using Y. Identify the Y from the following

$$R$$
 CHNO2+Y  $R$  C=0

- (a) Aqueous HCl
- (b) Aqueous NaOH
- (c) KMnO 4
- (d) CO
- 45. Alkyl cyanides undergo Stephen reduction to produce
  - (a) aldehyde
- (b) secondary amine
- primary amine (d) amide
- 46. The continuous phase contains the dispersed phase throughout, Example is (a)Water in milk
  - (b) Fat in milk
  - (c)Water droplets in mist
  - (d) Oil in water
- 47. The number of hydrogen atoms present in 25.6 g of sucrose1 (C2H22O11) which has a molar mass of 342.3 g is
  - (a) 22
- (b) 9.91 × 1023
- (c) 1023 11
- (d)  $44 \times 1023$
- Milk c×h 1a0ng2e3s after digestion into:
  - (a) cellulose
- (b) fructose
- (c) glucose
- (d) lactose
- 49. Which of the following sets consists only of essential amino acids?
  - Alanine, tyrosine, cystine
  - (b) Leucine, lysine, tryptophane
  - Alanine, glutamine, lycine (c)
  - Leucine, proline, glycine

- 50. Which of the following is ketohexose?
  - (a) Glucose
- (b) Sucrose
- (c) Fructose
- (d) Ribose
- The oxidation number of oxygen in KO3, Na2O2 is
  - (a) 3.
- (b) 1, 0
- (c) 2
- (d) -0.33, -1
- ReactOio,n of PCl3 and PhMgBr would give 52. (a) br1omobenzene
  - c(bh)lorobenzene
  - t(cri)phenylphosphine
  - d(dic) hlorobenzene
- Which of the following is not a characteristic of transition elements?
  - (a) Variable oxidation states
  - (b) Formation of colored compounds
  - (c) Formation of interstitial compounds
  - (d) Natural radioactivity
- Cl P Cl bond angles in PCl5 molecule are 54.
  - (a) 120° and 90°
- (b) 60° and 90°
- (c) 60° and 120°
- (d) 120° and 30°
- The magnetic moment of a salt containing Zn2+ ion is
  - (a) 0

57.

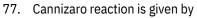
- (b) 1.87
- (c) 5.92
- (d) 2
- The number of formula units of calcium flouride CaF2 present in 146.4 g of CaF2 are (molar mass of CaF2 is 78.08 g/mol)
  - (a) 1.129 1024CaF (2b) 1.146 1024 CaF
  - 7.808 1024CaF (d) 1.877 1024 2aF (c) The IUPAC name of th2 e given compound

### CoNH 3 5ClCl 2 is

- (a) pentaamino cobalt chloride chlorate
- (b) cobalt pentaamine chloro chloride
- (c) pentaamine chloro cobalt (III) chloride
- (d) pentaamino cobalt (III) chlorate
- When SCN- is added to an aqueous solution containing Fe(NO3)3, the complex ion produced is

- FeOH <sub>2 5</sub> SCN-(b)
- FeOH 28 SCN-(c)
- (d) FeOH 2 SCN

59.	Hair dyes contaion (a) e(c) itrate (b gold chloride	68.	sometime because :	
60.	silver nitrate ) copper sulphate Schottky defects occu <b>(s</b> mainly in electrovalent compounds where )  (a) positive ions and negative ions are of (b) different size (c) positive ions and negative ions are of same		<ul> <li>(a) electrode potential of both the electrodes</li> <li>(b) becomes zero</li> <li>(c) electrode potential of both the electrodes</li> <li>(d) becomes equal <ul> <li>one of the electrodes is eaten away</li> <li>the cell reaction gets reversed</li> </ul> </li> </ul>	
	(d) size     positive ions are small and negative ions     are big     positive ions are big and negative ions are     small	69.	The amount of electricity required to produce one mole of copper from copper sulphate solution will be  (b) 2.33 Faraday	
61.	The number of unpaired electrons calculated in	70.	©Faraday (d) 1.33 Faraday Dipping iron article into a strongly alkaline	
	CoNH3 $_6$ and CoF $_6$ $^3$ are		solution of sodium phosphate (a) does not affect the article	
62.	(a) 4 and 4 (b) 0 and 2 (c) 2 and 4 (d) 0 and 4 The standard free energy change of a reaction		(b forms Fe2O3. xH2O on the surface ) forms iron phosphate film (c) forms ferric hydroxide	
	is G 115kJ at 298 K. Calculate the equilibrium constant k P in log kp	71.	flydroboration oxidation of 4-methyl-octene would give  (a) 4-methyl octanol  (b) 2-methyl decane	
	R 8.314 Jk <sup>1</sup> mol <sup>1</sup> (a) 20.16 (b) 2.303 (c) 2.016 (d) 13.83	72.	(c) 4-methyl heptanol (d) 4-methyl-2-octanone When ethyl alcohol is heated with conc. H2SO4,	
63.	If an endothermic reaction occurs spontaneously at constant temperature T and P, then which of the following is true?	/	the product obtained is: (a) CH 3COOC2H5 (bd)) C2CH2H42 (c) C2H6	
	(a) G > 0 (b) H < 0 (c) S > 0 (d) S < 0	73.	Anisole is the product obtained from phenol by the reaction known as	
64.	If a plot of log10C versus t gives a straight line for a given reaction, then the reaction is  (a) zero order (b) first order  (c) second order (d) third order	74.	(a) coupling (b) etherification (c) oxidation (d) esterification Ethylene glycol gives oxalic acid on oxidation	
65.	A spontaneous process is one in which the system suffers:  (a) no energy change (b) a lowering of free energy (c) a lowering of entropy		with (a) acidified K2Cr 2O7 (b)acidified KMnO <sub>4</sub> (c) alkaline KMnO4 (d periodic acid	
44	(d) an increase in internal energy  The half life period of a first order reaction is 1	75.	Diamond is hard becaस्रास्त्र(a)four valence electrons are bonded to	
66.	min 40 secs. Calculate its rate constant. (a) $6.93 \times 10-3 \text{ min}-1(\text{b})6.93 \times 10-3 \text{ sec}-1$ (c) $6.93 \times 10-3 \text{ sec}$ (d) $6.93 \times 103 \text{ sec}$		<ul> <li>(b) each carbon atoms by covalent bonds</li> <li>(c) it is a giant molecule</li> <li>(d) it is made up of carbon atoms it cannot be burnt</li> </ul>	
67.	The molar conductivities of KCl, NaCl and KNO are 152, 128 and 111 S cm2 mol-1 respectively.	76.	A wittig reaction with an aldehyde gives	
	What is the molar conductivity of NaNO3?  (a) 101 S cm2 mol-1(b)87 S cm2 mol-1  (c) -101 S cm2 mol-1(d)-391 S cm2 mol-1		<ul><li>(a) ketone compound</li><li>(b) a long chain fatty acid</li><li>(c) olefin compound</li><li>(d) epoxide</li></ul>	



- (a) HCHO
- (b) CH 3COCH3
- (c) CH 3CHO
- (d) CH3CH2OH

# CHO

Identify the reactant

- (a) H2O
- (b) HCHO
- (c) CO
- (d) CH 3CHO

### Maleic acid and Fumaric acids are G(ae)omePtorisci tIisoonm Iseorsmers(b) (d)cu)nctEionneanlt iIosmomeresrs

- The gas evolved on heating alkali formate with soda-lime is
  - (a) CO
- (b) CO 2
- (c) Hydrogen
- (d) water vapor

### 81. If a,b,c be three unit vectors such that

1b,b and c being non-parallel. If a (b c)

1 is the angle between a and b and 2 is the angle between a and c, then

- $\frac{1}{6}$ ,  $\frac{2}{3}$  (b)  $\frac{1}{3}$ ,  $\frac{3}{2}$
- (c)  $^{1}$   $^{2}$   $^{2}$   $^{2}$   $^{3}$   $^{(d)}$   $^{1}$   $^{3}$   $^{0}$ ,  $^{2}$   $^{2}$  equation  $^{r2}$  2r.c  $^{h}$   $^{|}$   $^{|}$   $\sqrt{h}$ ,

### 82.

- represents
- (a) circle (c) cone
- (b) ellipse (d) sphere

### 83. The simplified expression of $\sin(\tan(1 x))$ , for any 90. real number x is given by

- $\frac{1}{\sqrt{1 \times 2}} \qquad \text{(d)} \qquad \frac{x}{\sqrt{1 \times 2}}$

84. If 
$$\left| \frac{z + 25}{z + 1} \right|^{-5}$$
, the value of  $|z|$ 

- (a

- (d) 6
- (c)

- 85. Argument of the complex number  $\frac{1}{2}$  i
  - (a) 45°
- (b) 135°
- (c) 225°
- (d) 240°
- 86. In a triangle ABC, the sides b and c are the roots of the equation x2 - 61x + 820 = 0 and

$$A = \tan - 1 \frac{4}{3}$$
 , then a2 is equal to

- (a) 1098
- (b) 1096
- (c) 1097
- (d) 1095
- The shortest distance between the straight lines through the points A1 = (6, 2, 2) and A 2 = (-4, 0, -1), in the directions of (1, -2, 2) and (3, -2, -2) is
- 88. The center and radius of the sphere x2 + y2 + z2 + 3x - 4z + 1 = 0 are
  - $\frac{3}{2}$ ,0, 2;  $\frac{\sqrt{21}}{2}$ (a)
  - (b)  $\frac{3}{2}$ ,0,2;  $\sqrt{21}$
  - $\frac{3}{2}$ ,0,2;  $\frac{\sqrt{21}}{2}$ (c)
  - 3,2,0;221 (d)
- Let A and B are two fixed points in a plane then locus of another point C on the same plane such that CA + CB = constant, (> AB) is
  - (a) circle
- (b) ellipse
- (c) parabola
- (d) hyperbola

The directrix of the parabola y2 + 4x + 3 = 0 is

- 91. If g(x) is a polynomial satisfying g(x) g(y) = g(x) + g(y) + g(xy) - 2
  - for all real x and y and g (2) = 5 thenLt g(x) is
  - (a) 9
- (b) 10
- (c) 25
- (d) 20

- 92. The value of f(0) so that  $\frac{(ex 2x)}{x}$  may be continuous at x = 0 is
  - (a)  $\log \frac{12}{-}$
- (b) 0
- (c)
- (d)  $-1 + \log 2$
- 93. Let [] denote the greatest integer function and  $f(x) = [\tan 2 x]$ . Then
  - (a)  $\lim_{x \to 0} f(x)$  does not exist
  - (b) f(x) is continuous at x = 0
  - (c) f(x) is not differentiable at x = 0
  - d f(x) = 1
- 94. A spherical balloon is expanding. If the radius is increasing at the rate of 2 centimeters per minute, the rate at which the volume increases (in cubic centimeters per minute) when the radius is 5 centimetres is
  - (a) 10
- (b) 100
- (c) 200
- (d) 50
- 95. The length of the parabola y2 = 12x cut off by the latus-rectum is
  - (a)  $\frac{5}{2} \sqrt{2} |88| (\frac{1}{4} \sqrt{2})$
  - (d)  $3 \sqrt{\log(1 \sqrt{2})}$
- 96. If I  $\frac{x5}{\sqrt{1-x3}}$ dx, then I is equal to
  - (a)  $9(1 x^3)^{\frac{5}{2}} 3(1 x^3)^{\frac{3}{2}} C$
  - (b)  $\log \left| \sqrt{x} \quad \sqrt{1 \quad x^3} \right|$
  - (c)  $\log \left| \sqrt{x} \sqrt{1 + x^3} \right|$  C
  - (d)  $9(1 x^3)^2 3(1 x^3)^2 C$

97. Area enclosed by the curve

$$4x \sqrt{2}^{2} y^{2} 8 is$$

- (a)
- (b) 2
- (c) 3
- (d) 4
- 98. The value of  $\int_{0}^{a} \sqrt{\frac{a \times x}{x}} dx$  is
  - (a)
- (b) a 4
- (c)
- (d)
- Let y be the number of people in a village at time t. Assume that the rate of change of the population is proportional to the number of people in the village at any time and further assume that the population never increases in time. Then the population of the village at any fixed time t is given by
  - (a) y = ekt + c, for some constants c < 0 and k > 0
  - (b) y = cekt, for some constants c > 0 and k < 0

  - (c) y = ect + k, for some constants c < 0 and k > 0(d) y = kect, for some constants c > 0 and k < 0
- 100. The differential equation of all straight lines touching the circle x2 + y2 = a2 is

(a) 
$$y$$
  $\frac{dy}{dy}^2$   $\frac{a^2}{1}$   $\frac{dy}{dy}^2$ 

(b) 
$$y \xrightarrow{xddyx^2} a_2 1 \xrightarrow{dy} a_1^2$$

(d) 
$$y \frac{dy}{dx} = a^2 1 \frac{dy}{dx}$$

- 101. The differential equation

admits

- (a) infinite number of solutions
- (b) no solution
- (c) a unique solution
- (d) many solutions

### 102. Solution of the differential equation

$$xdy ydx \sqrt{x2 y2}dx 0 is$$

(a) 
$$\sqrt{x2}$$
  $\sqrt{x2}$   $\sqrt{2}$   $\sqrt{2}$ 

(a) 
$$y = \sqrt{x2} = y2$$
 Cx2  
(b)  $y = \sqrt{x2} = y2$  Cx2  
(c)  $x = \sqrt{x2} = y2$  Cy2

(c) 
$$\chi \sqrt{x^2 y^2}$$
 Cy2

(d) 
$$\chi \sqrt{x2-y2}$$
 Cy2

### 103.Let P, Q, R and S be statements and suppose

that P Q R

P. if ~ S R, then

(a)  $S \sim Q$ 

(b)  $\sim 0$ S

(c) ~S ~ Q

(d) O ~S

104.In how many number of ways can 10 students be divided into three teams, one containing four students and the other three?

- (a) 400
- (b) 700
- (c) 1050
- (d) 2100

105. If R be a relation defined as a R b iff |a - b| > 0, then the relation is

- (a) reflexive
- (b) symmetric
- transitive
- symmetric and transitive

106.Let S be a finite set containing n elements. Then the total number of commutative binary operation on S is

### 107.A manufacturer of cotter pins knows that 5% of

his product is defective. He sells pins in boxes of 100 and guarantees that not more than one pin will be defective in a box. In order to find the probability that a box will fail to meet the guaranteed quality, the probability distribution one has to employ is

- (a) Binomial
- (b) Poisson
- (d) Exponential
- (c) Normal 108.The probability that a certain kind of component

will survive a given shock test is probability that exactly 2 of the next 4 components tested survive is

- 25  $\overline{128}$
- (c)
- 27 128

109. Mean and standard deviation of marks obtained in some particular subject by four classes are given below. Report the class with best performance

- (a) 80.
- (b) 75,5
- (c) 18 (d) 76, 7 110.A rand800m, variable X follows binomial distri2bu1tion with mean and variance. Then
  - (a) 0 < <
- (b) 0 < <
- (c) < 0 <
- (d) < 0 <
- 111. The system of equations

$$x + y + z = 0$$
  
 $2x + 3y + z = 0$ 

x + 2y = 0

ha a unique solution; x = 0, y = 0, z = 0

- infinite solutions s
- no solution (a)
- finite number of non-zero solutions (b)
- (c)
- (d) 112. (a)
  - (c) a = b2
- (b) a = b
- (d) ab = 1

113.If D = diag (d 1, d2, ..., dn) where d1 0, for i = 1, 2, ..., n, then D-1 is equal to

- (a) DT
- (b) D
- (c) Adj (D)
- (d) diag (d<sub>1</sub>1, d2<sup>-1</sup>, ...dn<sup>-1</sup>)
- 114.If x, y, z are different from zero and

$$\begin{vmatrix} a & b & y & c \\ a & x & b & z \\ a & x & b & y & \infty \end{vmatrix} = 0 \text{ then the value of}$$

the expression ,

- (a) 0
- (b) -1
- (c) 1
- (d) 2

115. Probability of getting positive integral roots of the equation  $x^2 - n = 0$  for the integer n, 1 < n < 40is

- (a) 5
- 1 (b) 10
- 3 (c) 20
- 1 (d) 20

116. The number of real roots of the equation

$$x4 \sqrt{x4 \ 20} \ 22 is$$

- 4 (a)
- (b) 2 (d) 1

0 117.L₩

, be the roots of the equation

 $x^2 - ax + b = 0$  and An = n + n.

Then An+1 - aAn + bAn-1 is equal to

- (a) –a (c) 0
- (b) b
- (d) a b118.If the sides of a right-angle triangle form an A.P.,

the 'Sin' of the acute angles are
(a) 
$$\frac{8,45}{-}$$

(b) 
$$\sqrt{3,1}$$

(c) 
$$\sqrt{\frac{\sqrt{5}}{2}}, \sqrt{\frac{\sqrt{5}}{2}}$$

(d) 
$$\sqrt{\frac{\sqrt{3}}{2}}, \sqrt{\frac{\sqrt{3}}{2}}$$

119. The plane through the point (-1, -1, -1) and containing the line of intersection of the planes

r.(i^3j^k^) 0 and r.(j^

2k^) 0 is

120. a  $\hat{j}^{\hat{j}} = \hat{k} \hat{j}^{\hat{j}}$  and b  $\hat{j}^{\hat{j}} = \hat{k} \hat{j}^{\hat{j}} \hat{j}^{\hat{j}} \hat{k}$  are one of the

sides and m^edians respectively, of a triangle through the same vertex, then area of the triangle is

- (a)  $\frac{1}{2}\sqrt{83}$
- (b)  $\sqrt{83}$
- (c)  $2\sqrt{85}$
- √86

### SOLUTIONS

### PART - I (PHYSICS)

- (d) I wo beams of light give rise to an interference pattern if they are coherent, they have same wavelength/frequency in same phase or having a constant phase difference and same state of polarisation.

  Interference pattern can not be obtained if the two beams are not mono chromatic.
  (b)By the theory of diffraction at a single slit, the width of the central maximum is given by
  - W  $\frac{2D}{a}$  W D,

2.

Therefore, to increase the width of the central maximum a should be decreased

maximum a should be decreased.

Work
identification of the should be decreased.

Mork
identification of the should be decreased.

Work
identification of the should be decreased.

Mork
identification of the should be decreased.

Identification of the should be decrease

path difference of

- Ray R2originates after

reflection at narer medium.

Net path difference = 2t+

where t is the thickness of the soap solution. For constructive interference,

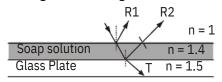
$$2t+$$
 2 = m, where m = 0, 1, 2.....

Let the two adjacent reflection maxima be observed at m and m-1. Then

2 t 
$$\frac{1}{2}$$
 m  $_1$   
or 2 t m  $\frac{12}{1}$  ... (1)

Similarly, 2t m 
$$\begin{pmatrix} 3 \\ 2 \end{pmatrix}$$
 ...(2)

Solving (1) & (2), we get



$$\begin{array}{cccc} & & \frac{2}{2} & \\ & & 1 \\ & & 1 \end{array}$$

Putting, 1 = 420 nm, 2 = 630 nm, = 1.4 We get,t = 450 nm

4. (c)We have,

speed = frequency × wavelength Also, when a wave passes from one medium to the other, its frequency remains consider. wavelength

Therefore, when the speed of a wave doubles, its wavelength also doubles.

5. (c) Here,

Frequency, =  $6 \times 1014 \text{ Hz}$ Work-function, =  $2\text{eV} = 2 \times 1.6 \times 10-19 \text{ J}$ 

corfrnsi = 3.2 × 10-19 Maximum energy Tmax = 2 Ry I

Maximum energy, Tmax = ? By Einstein's photo electric equation, we have

$$h = +T_{max}$$

$$Tmax = h -$$
= (6.63 × 10-34 × 6 × 1014)- (3.2 × 10-19)
= (3.97 × 10-19) - (3.2 × 10-19)
= 0.77 × 10-19 J
$$= \frac{0.77 \cdot 10 \cdot 19}{1.6 \cdot 10 \cdot 19} \text{ eV} = 0.49 \text{ eV}$$

(b)We have, dsin

For  $= 90^{\circ}$  and n = 1, we get d =

But 
$$\frac{h}{p} = \frac{h}{\sqrt{2meV}} = \sqrt{\frac{h^2}{2meV}}$$
  
=  $\sqrt{\frac{(6.63\ 10\ 34)2}{2\ 9.1\ 10\ 31\ 1.6\ 10^{-19}\ V}}$   
=  $\sqrt{\frac{1}{2}\ 109m}$   $d = \sqrt{\frac{10.5}{2meV}}$  109

or 5 10 10 
$$\sqrt{\frac{1.5}{V}}$$
 10 9 or 0.5  $\sqrt{\frac{1.5}{V}}$   
or 0.5 0.5  $\sqrt{\frac{1.5}{V}}$  V  $\sqrt{\frac{1.5}{0.5}} = 6V$ 

answer. But 5V is approximately equal to the exact potential. Therefore, option (b) should be the correct option.

- 7. (b)Davison and Germer performed an experiment to prove that matter has a wave nature. The experiment was based on electron diffraction.
- (c)We have,  $N = {}_{t} N_{0} \frac{12T1/2}{}$

NNt = number of atoms present after time t 0 = initial number of atoms

T1/2 = half life of the nuclide

$$\frac{N_{0t}}{N}$$
  $\frac{1}{2}$   $\frac{1}{T_{1/2}}$  or  $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{T_{1/2}}$  or  $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{T_{1/2}}$   $\frac{2}{T_{1/2}}$   $\frac{1}{T_{1/2}}$   $\frac{2}{T_{1/2}}$   $\frac{1}{T_{1/2}}$   $\frac{2}{T_{1/2}}$   $\frac{2$ 

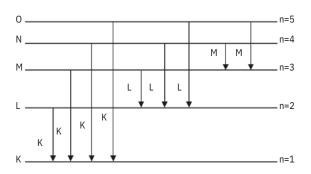
9. (c)Due to time dilation the interval between two events at the same point in a moving frame appears to be longer by a factor

$$\frac{1}{\sqrt{1 + \frac{v^2}{c^2}}}$$
 to an observer in a stationary

frame. Time dilation is independent of the direction of velocity and depends only on its magnitude.

10. (c) The - decay in the case of 234U takes place as follows:

11. (a) When electron jumps from the level n = 2 to of electron from the level n = 3 to the level n = shown in the figure. 1. X- ray spectra has been shown below.



No option is matching with the exact 12. (b)Let the number of and particles emitted

$$A - 4m = A - 8$$
  $m = 2$ 

the mass number of a radioactive nuclide decreases by 4 due to emission of one particle] Aga in , (Z - 2m) + n = Z - 3

[the atomic number decreases by 2 due

emission of 1 -particle but increases by 1 due to emission of 1 - particle

or or 
$$-2m + n = -3$$
  
 $2m - n = 3$   
 $(2 \times 2) - n = 3$  (  $m=2$ )  
 $n = 1$ 

13. (b) Rf RΙ - Op – amp

For the Op-amp shown above, we have

$$\frac{\text{Vo}}{\text{VI}} \qquad \frac{\text{Rf}}{\text{RI}}$$

Comparing this circuit with the given one, We get V **₹¼**,Rf = 10k  $= 10 \times 10^{\circ}$  $RI = 1k = 1 \times 103$ 

14.(d)The solid is an n-type semiconductor. In an ntype semiconductor, the impurity is pentavalent which is also called the Donar impurity because one impurity atom generate one electron. The Donor the level n = 1, Kx - rays are emitted. Similarly, Kx-rays are emitted when there is atransition energy level lies just below the conduction band as

Conduction band	
Donor levels	
Valence band	

15. (a)We have, I 
$$D = IS(eV_D/V^T 1)$$

where, VT 
$$\frac{k^{7}}{e}$$

$$\begin{split} \frac{I_D}{I_S} & 1 & e^{VO} & \text{or ln 1} & \frac{I_D}{I_S} & \frac{V_D}{nV_T} \\ V_D & \text{nVT ln 1} & \frac{I_D}{I_S} & = \text{VT ln 1} & \frac{I_D}{I_S} \\ & = \text{VT ln} & \frac{I_{majority}}{IS} \end{split}$$

Here,  $n_{\underline{e}}$  (101 7 1016)cm 3 101 (610 1)cm 3 9 10  $^{16}$ cm3

We know that, ne  $n_h n_i^2$   $n_h n_i^2 = \frac{(1.4 \cdot 10^{-10})2}{0.10^{16}}$  cm<sup>3</sup>

Also,  $\frac{\text{I maj ori tyn}^{\text{e h}}}{\text{IS}} \frac{\text{Tyn}^{\text{e h}}}{\text{n}}$ 

$$V_D = \frac{kT}{eln} = \frac{9 \cdot 10^{16}}{(1.4 \cdot 10^{-10})^2}$$
  
9 \quad 10^{16}

$$=\frac{\text{keTln}(4)}{10^{12}}$$

16. (c)Here, electric field, E = 106 V/m width of depletion region, d =  $2.5 \text{ m} = 2.5 \times 10\text{--}6\text{m}$  Potential required for breakdown (V) = Ed =  $(106 \times 2.5 \times 10\text{--}6) \text{ V} = 2.5 \text{ V}$  Contact Potential = 1.0 V

Reverse biased potential for zener breakdown = (2.5 – 1.0) V = 1.5 V

17 (b)In a colpitt oscillator, the feed-back network consists of two capacitors and one inductor.
(d)The reverse saturation of p-n diode depends on the doping concentrations, diffusion

18 length and device temperature.

1.9. (a)Antenna length =

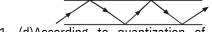
for cosntant velocity,

1

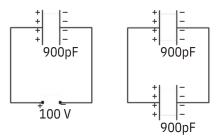
Antenna length

Here, AM FM Antenna length for AM should be longer than that of FM.

20. (a)The principle of communication using optical fibers is based on the principle of total internal reflection.



- 21. (d)According to quantization of charge, the charge of any system is an integral multiple of the charge of electron which is the least amount of charge on any system.
- 22. (b) The charge on the capacitor when connected to the battery is given by



Q = CV =  $(900 \times 10-12 \text{ F}) \times 100 \text{ V} = 9 \times 10-8 \text{ C}$ When the battery is replaced by another capacitor of 900 pF capacitance, the charge of 9  $\times$  10-8 C is distributed on both. Let Q and  $\times$  20 be the charge on each of them.

$$Q = Q1 + Q2$$
  
= C1V + C2V, where V is the common potential.

or V = 
$$\frac{Q}{C1 \quad C2}$$

As the two capacitors are in parallel, the equivalent capacitance is given by C = C1 + C2

Total energy of the capacitors =  $\frac{1}{Q^2 \text{CV2}}$ 

$$= \frac{1}{2} \quad C_1 \quad C_2 \quad \frac{Q2}{C1 \quad C_2} = 2(C1 \quad C2)$$

$$= \frac{9 \quad 10^{-8} \quad 2}{2(900 \quad 10 \quad 12 \quad 900 \quad 10^{-12})}$$

$$= \frac{(9)2 \quad 10^{-16}}{2 \quad 2 \quad 9 \quad 10^{-10}} = 2.25 \times 10 - 6 \text{ J}$$

For 
$$l = L$$
 and  $A = A$ ; R1  $A$ 

For 
$$l = \frac{L}{2}$$
 and  $A = 2A$ ;

$$R2 = \frac{\frac{L}{2}}{2A} \frac{1}{4} \frac{L}{A} = \frac{1}{4}R1$$

For l = 2L and  $A = \frac{A}{2}$ 

$$R_3 \qquad \frac{2L}{A} \qquad \qquad \frac{L}{A} = 4 R_1$$

Thus R3 > R1 > R2

Therefore, the wire having length 2L and area

$$\frac{\mathsf{A}}{\mathsf{2}}$$
 has the maximum resistance.

24. (d)We know that the electric field at any point due to an electric dipole varies inversely with the cube of the distance of the point from the centre of the dipole, that is,



Also, force on a charge (q) is given by

$$F = qE$$
  $F = \frac{1}{r^3}$ 

When the distance of the charge becomes 2m, i.e. double of its initial value, then new force (F  $\dot{}$  ) will become

$$F' = (2)3.F$$
  $F = 8$ 

25. (c) Let us first calculate the total charge on the soild sphere.

Let us consider a concentric sphere of radius r and thickness dr. Then volume of the sphere, dV = 4r2dr

Given, the volume charge density of the sphere =



Charge on this sphere,

$$dQ = .dV = \frac{0.4r2}{r} dr = 4$$
 .rdr.

Total charge on the whole solid sphere,

$$Q_s = {R1 \choose 0} dQ = 4 = {R1 \choose 0} r dr$$

$$= 4 = {R21 \choose 0} = 2 = 0 R21$$

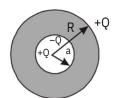
$$QS = 2 = {0R2 \choose 0} = ...(1)$$

Now, the total charge on the hollow sphere, Qh = -(4R22)By question, Qs + Qh = 0

2 R2 = 4R2 <sub>2</sub>

$$\frac{0}{2}$$
  $\frac{R12}{2}$   $\sqrt{\frac{0}{2}}$ 

26. (b)A charge Q will be induced on the inner surface of the solid spherical conductor. An equal but opposite charge will be induced on the outer surface of the conductor. There will be no charge at a position between the inner and outer surface.



27. (b) The energy stored in a capacitor is given by

$$E = \frac{Q^2}{2C}$$

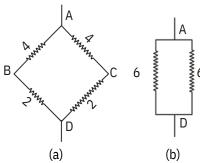
L = length of the cylindrical conductor R R2 == oinunteerr rraaddiiuuss

When both Q and L are doubled, by keeping other parameters fixed, the energy stored (E') becomes

 $E'(2Q)^{\frac{3}{2}}L$ 

2Q2

### 28. (c)Redrawing the figure, we get



and 2 resistors are in series and the same is the case with another 4 and 2 resistors. So, the four resistors are equivalent to following two resistors.

Now, in fig (b) these two 6 resistors are in parallel.

Equivalent resistance, R 
$$\begin{pmatrix} 6 & 6 & 36 \\ 6 & 6 & 12 \end{pmatrix}$$

- = 3 29. (b) In a conductor, the charge carriers are electrons. As the temperature is increased. the collisions of these conduction electrons with the fixed ions of the lattice of the metal increases and hence the resistance of the conductor also increases.
- If there is no potential difference through a 30. (b) metallic wire, the current is zero because the electrons drift in a random direction with a speed of the order of 10-2 cm/s so that the net charge crossing a particular cross-section 34.(c) When a metallic plate swings between the in a given time is zero.
- If the wire is replaced by another wire of same material but with double the length and half 31. the thickness, the resistance of the wire as a whole will change. Let us calculate this ch a n ge.

Initial resistance, 
$$R = A \frac{L}{r^2}$$

Fubak resistance, R'

Therefore, the resistance will increase by eight times.

In a meter-bridge, we have

wh er eR = unknown resistor S = known resistor *l* = balancing length

When the resistance of the new wire is 8R then the new balancing length will be

$$\frac{1008R}{S8R} = \frac{1008R}{(SR) 7R}$$

$$= \frac{1008R}{100R} 7R$$

No option is correct.

32.(b)The transport current flows through the surface of the subgreen ducting wire and not

33.(c)Here, 
$$E = 3 \times 104 \text{ NC} - 1$$
  
p = 6 × 10-30 Cm

$$max = ?$$

We have. torque acting on a dipole

, i.e. 
$$\max = pE$$
  
 $\max = (3 \times 104 \times 6 \times 10-30)$  Nm  
 $= 18 \times 10-26$  Nm

- poles of a magnet, eddy currents are set up inside the plate. These currents set up their own magnetic field which opposes the magnetic field of the poles. Thus, the direction of the current opposes the motion of the plate.
- 35.(b)When an electrical appliance is switched on, the electrons in the conducting wires move with their drift speed which is very less than the speed of light. But as soon as the switch is on, an electromagnetic wave is set up

inside the conductor and the electrical signal is carried by them. The speed of electromagnetic wave is, of course, equal to the speed of light and hence the appliance responds almost immediately after the

switch 36.(b) Imade cuit shown is a parallel resonant

circuit. The frequency is 
$$f = \frac{1}{2 \sqrt{LC}}$$
 at

resonance. Also, at resonance, the capacitative reactance is equal to the inductive reactance. Therefore, equal current will flow through both the bulbs b1 and b2.

So, both will glow with same brightness.

37. (b)In a transformer, the ratio of turns in the windings is given by

N 5kV 
$$= \frac{5000V}{240V} = 20.8$$

38. (a) Self - inductance (L) of a solenoid =  $\frac{ON}{I}$ 

where o = absolute permittivily of space/

N = number of turns in the coil A = area of cross-section of the solenoid

l = length of solenoid.

This expression shows that for all three solenoids, the self-inductances will be equal. 43.

(b) We know that the refractive index of a medium is given by

 $\frac{co}{c}$ 

Where c = velocity of light in the medium co = velocity of light in vacuum For crown glass,

1.5 
$$\frac{c_0}{2 \cdot 108}$$
 ... (1)

For flint glass, 1.8 
$$\frac{c_0}{c}$$
 ...(2)

Dividing (2) by (1), we get 
$$\begin{pmatrix} 2 & 108 & 1. \\ c & 8 & \\ c & 1. \end{pmatrix}$$
  
or c =  $\begin{pmatrix} 1.5 & 2.8 & 10^8 & m/s \\ 1.8 & 1.67 \times 108 & m/s \\ 1.67 \times 108 & m/s \\$ 

40.(c)Fast moving electrons create electromagnetic

waves. So, the diffraction pattern will be observed. Also, the angular width of the central maximum is given by

$$W = \frac{2}{a}$$
, where a = width of the slit

= wavelength of the light. When the speed of electrons will increase, the frequency will increase which will result in decreasing the wavelength as the speed of light is a constant. Therefore, the angular width will decrease.

### PART - II (CHEMISTRY)

(b)Aliphatic nitro compounds are prepared by vapour phase nitration of alkanes at 693-793K, under pressure. Alkanes though less reactive do undergo nitration to give a mixture of nitro alkanes resulting through cleavage of carbon-carbon bond alongwith oxidation product like CO2, NO2, H2O etc.

3 NO <sub>2</sub> (20%)

42. (a)Amides are hydrolysed rapidly by acids to produce carboxylic acid and ammonium salt;

RCONH  $_2$   $^{\rm H3O}$  RCOOH NH  $_4$  Hence acetamide will give acetic acid on hydrolysis.

(b)Diazotisation reactions are shown by primary aromatic amine only as the arene diazonium salt formed is stable at 273-278 K. Compound GH5CH2NH2 is not an aromatic amine, hence

will not give the test/reaction.

 (aS)econdary nitro alkanes upon hydrolysis with boiling HCl gives a ketone & nitrous oxid e. 2R2CHNO2

45. (a) Stephen reduction is partial reduction of alkyl or aryl cyanides to give corresponding aldehydes with a suspension of anhydrous stannous chloride in ether.

h yd rolysis boiling HQ CH GHO NH GI

46. (a)In a colloidal system, the substance present in large amount in the mixture is called the dispersed medium & the solute is called dispersed phase. In case of milk and water solution the dispersed phase is milk protein & fat and water is dispersed medium. 47. (b)No. of moles of a compound

given mass (gm) Molar mass (gm)

i.e.  $\frac{25.6}{342.3}$  = 0.0748 moles.

× 1023 molecules of it.

Hence 0.0748 moles contains = 6.022 × 1023 × 0.0748

 $= 0.4504 \times 1023$  molecules.

1 molecule of sucrose by formula is having 22 atoms of hydrogen.

 $0.4504 \times 1023 \times 1023 \times 22 = 9.91 \times 1023$ atoms of hydrogen.

48.(c)Milk contains lactose as milk sugar. After digestion of milk lactose is broken down by enzymes lactase to form glucose and galactose before it enter the blood stream.

- 49.(b)Out of 20 amino acids, the 10 amino acids which human body cannot synthesize are called essential amino acids. The ten essential amino acids are:
  - 1) Valine 2) Leucine 3) Isolucine 4) Histidine
  - 5) Phenylanaline 6) Methionine 7)

Tryptophan 8) Lysine 9) Arginine 10)

Th reon in e.

- 50.(c)Among the given examples, glucose is an alcohexose, sucrose is a disaccharide, fructose is a ketohexose while ribose is a aldopentose.
- 51.(d)To find the oxidation number of a given compound we have to equate the charge on the overall compound with the charge on individual atom of which the compound is made of.

In KO 3. K is an alkali metal. hence its oxidation number is +1. In KO

$$(+1) + 3 \times (x) = 0 \text{ or } x =$$
  $\frac{1}{3}$  0.33

hence oxidation number of oxygen i.e. x = -0.33.

In Na2 O2, again Na is an alkali metal.

Hence 
$$2 \times (+1) + 2 \times x = 0$$

52.(c)In a reaction the alkyl part of grignard reagent

acts as a nucleophile as carbon is more electronegative than magnesium. Hence the alkyl part will get attached to the electron

deficie3n,t cshpleocriinees. is more electronegative than i.e. Pentaamine chloro cobalt (III) chloride. In PCl phosphorous.

Hence the Ph- will attack the phosphorous in PCl 3 to form organic phosphine with formula Ph3P.

3PhMgBr PCl<sub>3</sub>

3MgBrCl

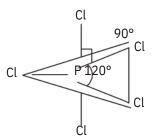
Triphenylphosphine

53.(d)Transition elements or d-block elements have 1 mole of sucrose (C12 H22O11) contains 6.0 22 riable oxidation states, they form coloured

> compounds because of partially filled d- orbitals and also because of small size they form interstitial compounds. They are stable elements and does not show radio activity.

(a)In PCl, ph s undergoes spd <sup>3</sup> 5osphorou hybridization and has trigonal bipyramidal géometry. It has two axial chlorine atoms & three equatorial chlorine atoms bonded to the central P.

Hence bond angles for axial are 90°, Cl-P-Cl & for equatorial Cl-P-Cl it is 120°.



55.(a) Magnetic moment of a salt depends upon the number of unpaired d-electrons. In Zn2+ salt configuration of cation is 4s03d10. Hence total no. of unpaired electron, n is zero. So magnetic moment i.e.

B.M.  $\sqrt{n(n 2)} 0.$ 

56.(a)Formula unit = no. of molecules of CaF 2.

massingm 146.4gm 1.875 Moles = molarmass 78.08gm

Molecules = Mole × 6.022 × 1023

 $= 1.875 \times 6.022 \times 1023$ 

= 1.129 × 1024 units of CaF<sub>3</sub>

57.(c)For writing IUPAC name of a co-ordination compound we first write the name of (+) ive

complex here. [Co(NH)Cl]2+35
The names of ligands will come first in alphabatical order, followed by metal ion with its oxidation state written in bracket or parentheis in Roman number i.e. Co (III) here.

IUPAC name for cationic complex Pentaamine chloro cobalt (III).

This will follow the name of anion with a gap.

- 58. thiocyanate, SCN- ion to form a blood red complex i.e. FeSCN2+. But in presence of water it forms a complex containing five water molecules. i.e. [Fe (H2 SOi)] lv5e (rS nCiNtr-)a]2.t+e has been findency for maximum randomness. i.e.
- 59. (c) used since the begining of nineteenth maximum entropy century to dye hair. Silver salts darken when 66. (b) For 1st order reaction. exposed to light and silver combines with protein yeilding a dark coloured proteinate.
- 60. (b)Schottky defect is generally shown by compounds which have ionic nature and small difference in the size of cations & anions.

In this defect equal no. of cations & anions is found missing from their lattice sites.

- and {CoF6} 3- both the 61. (d)In  $[Co(NH)]3_{\frac{1}{2}6}$  and  $\{CoF6\}$  <sup>3-</sup> both the oxidation state of cobalt ion is +3. In first case NH striosnightefinetedut rlaig aling aun chrevinionen itshe electrons in Co (+III) i.e. 4s03d6 get paired to form inner unpaired electron. On the otherahand implex wettenfield ligand hence it forms an outer orbital complex with 4 68. (c) As we know that unpaired electrons.
- 62. (a)  $G^{\circ} = -115 \text{ kJ at } 298 \text{K}.$ Now,  $G^{\circ} = -2.303 \text{ RT log kP}$ R = 8.314 JK-1 mol -1 & I = 298K.  $G^{\circ} = -2.303 \times 8.314 \times 298 \times \log Pk$ 115 103 = 20.155 298 log kP =2.303 8.314 = 20.16
- Now, G = H TS. As the reaction is endothermic, so value of H must be positive, i.e. H > 0. Hence to have a negative G. H < TS. As T & P are constant. TS must be positive to give the total value a negative sign. Hence S> 0.

63. (c) For a reaction to take place spontaneously

the value of G must be negative i.e. G< 0.

64. (b) Any first order reaction follows the equation

hence the plot is for a 1st order reaction.

- (b)Fe (III) ion from ferric nitrate will react with 65. (b)The driving forces which are responsible for a process to be spontaneous are: i)Tendency for minimizing energy

$$t\frac{1}{2}$$
 (half life time) =  $\frac{0.693}{\kappa}$ 

maximum entropy

Hence K = 
$$\frac{0.693}{t_{1/2}^{1/2}} = \frac{0.693}{(60 - 40)\text{sec}} = 0.693 \times$$

 $10-2 \sec -1 = 6.93 \times 10-3 \sec -1$ 

67. (b) Since NaNO 3 is formed by the reaction

Nacl KNO3 NaNO3 KCl

hence, using Kohlrausch's law

Ecell = Ecathode - Eanode when Ecathode = Eanode

Ecell = 0

If Ecell = 0 no net reaction occurs. The reactants and products are at equilibrium and no current will flow.

Note that it is only possible to obtain electrical work from a system that is not at equilibrium. In order for current to flow, there must be a net reaction occurring. As the oxidation- reduction reaction proceeds toward equilibrium, and the concentrations of the reacting species approach their equilibrium values, the EMF of the cell decreases to zero. When the system is at equilibrium, the cell potential is zero and we have a dead battery.

- 69. (c)In4 C suoSluOtion, oxidation state of Cu is +2. Hence one mole of copper sulphate will require charge equal to two moles of electrons to form metallic Cu. Mole charge = IF. Hence 2 Faraday is required.
- 70. (c)Rusting of iron is generally promoted in an acidic aqueous medium. Alkaline medium prevents availability of H+ ions. Sodium phosphate will cause formation of a protective film of iron phosphate on the iron preventing rusting. These solutions are used in car radiators to prevent rusting of iron parts.

71. alcohols containing same number of carbon atoms. The addition follow anti-Markowi Koff's rule. Boron atom act as an electrophile. Main two steps re involved. Reagent used BH3 & NaOH/H2O2.

4 - methyl octene

R<sub>3</sub>B where R=4-methyl octyl

72. (d)Et2hSyOl a4lcohol on treating with conc. H undergoes dehydration to form alkene i.e. ethylene

73. (b)An, Pishoelen yişl mOethyl ether. It

can be prepared by treating phenol first with a base like NaOH to form phenoxide ion. The phenoxide ion will then substitute the halide of an R-X molecule, to form methyl phenyl

C 6H5ONa CH 
$$_3$$
 Cl CH  $_3$  O C  $_6$ H  $_5$ 

74. (c) Alkaline Potassium permanganate is a strong oxidising agent. It oxidises ethylene glycol to oxalic acid.

$$\begin{array}{c} \text{CHI2} \text{y2OleOHnHe} \\ \text{CH} & \xrightarrow{\text{KMnO 4}} & \text{COOH} \\ & & \text{glycol} & & \text{oxalic} \\ \end{array}$$

75. (a)In the structure of diamond each carbon atom in sp3 hybridised & is covalently bonded with four other carbon atom held at the corners of a regular tetrahedron by covalent bonds. This results in a very big three dimensional polymeric structure in which C - C distance is 154 pm and bond angle is 109.5°. Owing to very strong covalent bonds by which atoms are held to gether diamond is the hardest substance known.

(a)Hydroboration-oxidation of alkenes give 76. (c)The witting reaction is a chemical reaction of aldehyde or ketone with triphenyl phosphonium ylide to give an alkene and triphenyl phosphine oxide.

C = O + (C6 H5)3 P = C

OR

$$C = C + (C6 H5)3 P = C$$
 $C = C + (C6 H5)3 P = C$ 
 $C = C + (C6 H5)3 P = C$ 
 $C = C + (C6 H5)3 P = C$ 
 $C = C + (C6 H5)3 P = C$ 
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 $C = C + (C6 H5)3 P = C$ 
 $C = C + (C6 H5)3 P = C$ 
 $C = C + (C6 H5)3 P = C$ 

Triphenyl phosphine oxide

77. (a)Cannizaro's reaction is for those aldehydes which does not contain - hydrogen atom. This is also called self oxidation - reduction reaction. Among the given carbonyl compounds only HCHO does not have - h ydr ogen.

78. (c) 
$$0 + CO$$
 AlCl  $3$  O

When a mixture of CO and HCl gas is passed through benzehennpatisheaethaylydset consisting anhydrous AlCl

is formed.

CO HCl HOCL formyl chloride

79.(b) Maleic acid & fumaric acid are both the isomers of butene dioic acid. Maleic acid is the cis isomer & fumaric is the trans-isomer.

80. (c)Alkali formate i.e. HCOONa with soda-lime i.e. NaOH + CaO will react to give Na 2CO3 and hydrogen gas is liberated.

### PART - III (MATHS)

81. (c) a (b c) 
$$\frac{1}{2}b$$

(a.b)c
(a.c)b

 $\frac{1}{2}b$  [Vector triple product]
(a.bcos
(a|.|c|cos 2)b | | | | 1)c  $\frac{1}{2}b$ 

Equating the coefficients of b and c both sides, we get

$$\cos 2 \quad \frac{12 \text{and } \cos 1}{0}$$

$$\cos 2 \quad \cos \frac{\pi}{3} \text{and } \cos \frac{\pi}{2}$$

$$2 \quad \frac{\pi}{3} \text{and } \frac{\pi}{2}$$

82.(d) Vector equation of a sphere in central form with centre having position vector c and radius R is

Hence, the given equation represents a sphere.

83. (b)Let 
$$tan-1 x =$$

$$x an \frac{\sin}{\cos} \frac{\sin}{\sqrt{1 \sin 2}}$$

$$x \sqrt{1 \sin 2} \sin x^2 (1 x^2)$$

$$x^2 \sin^2 (1 x^2)$$

$$\sin^2 x^2 \sin x^2 \sin x^2 (1 x^2)$$

$$\sin^{1}\frac{x}{\sqrt{1 \times 2}}$$

$$\tan^{1}x \quad \frac{x}{\sqrt{1 \times 2}}$$

Now,  $\sin (\tan -1x) = \sin \sin \frac{1}{\sqrt{1 \times 2}}$ 

$$= \frac{x}{\sqrt{1 \times 2}}$$

84. (c)Given that

$$\begin{vmatrix} z & 25 \\ \hline z & 1 \end{vmatrix} = 5 \qquad |Z = 25| \qquad 5|Z = 1|$$
Let  $Z = x + iy$ , then
$$\begin{vmatrix} x & iy & 25 \\ \hline & 5|x & iy = 1 \end{vmatrix}$$

$$\begin{vmatrix} (x & 25) & iy \\ \hline & 5(x = 1 & iy) \end{vmatrix}$$
Squaring both sides, we get

 $(x-25)^2 + y^2 = 25\{(x-1)^2 + y^2\}$ 

$$25x^2$$
  $50x$   $25$   $25y2$   $24x2 + 24$   $y2 - 600 = 0$   $x2 + y2 - 25 = 0$   $|x + iy|2 = 25$   $|Z| = 52$ 

85. (c)We

have, 1 1 3i 2 i 2 5i 3i2  
3i i 2 2 i 2 i 4 i2  
= -1 - i  
Now, let us put -1 = r cos, -1 = r sin  
Squaring and adding, r2 = 2 i.e., 
$$r = \sqrt{2}$$
  
So that cos =  $\frac{1}{\sqrt{2}}$ , sin =  $\frac{1}{\sqrt{2}}$ 

Thus, argument is 225°.

86. (c)Since b and C are the roots of x2 - 61x + 820 = 0, so b + c = 61, bc = 820

A 
$$\tan^{1}\frac{4}{3}$$
  $\tan^{4}\frac{4}{3}$   $\cos^{4}\frac{3}{5}$ 

Now, using the formula,

$$\cos A = \begin{array}{cc} b2 & c^2 & a^2 \\ & 2bc \end{array}$$

a2 = 
$$b2 + c2 - 2bc \cos A$$
  
=  $(b + c)2 - 2bc - 2bc \cos A$   
=  $(b + c)2 - 2bc (1 + \cos A)$   
=  $(61)2 - 2 \times 820 \ 1 \frac{3}{5}$   
=  $3721 - 2624 = 1097$ 

87. (d)Equation of first line,

$$\frac{x-6}{1}$$
  $\frac{y-2}{2}$   $\frac{z-2}{2}$  k (s ay)

x = k + 6, y = -2k + 2, z = 2k + 2Hence, general point on the first line, P = (k + 6, -2k + 2, 2k + 2)Equation of second line,

$$\frac{x}{3} = \frac{4}{2} = \frac{y}{2} = \frac{z}{2} = 1$$
 (say)  
  $x = 3l - 4, y = -2l, z = -2l - 1$ 

Hence, general point on the second line, Q (3l-4,-2l,-2l-1)Direction ratios of PQ are 3l-4-k-6,-2l+2k-2,-2l-1-2k-2 i.e. 3l-k-10,-2l+2k-2,-2l-2k-3 Now |PQ| will be the shortest distance between the two lines if PQ is perpendicular to both the lines. Hence,

Subtracting equation (i) from (ii), we get 16l = 16 l = 1

Putting this value of l in equation (i), we get -3k-3

$$-3k = 3$$
,  $k = -1$   
P  $(-1 + 6, -2 (-1) + 2, 2 (-1) + 2)$   
 $(5, 4, 0)$ 

Similarly, Q = (-1, -2, -3)Hence, shortest distance, PQ,

= 
$$\sqrt{(1 \ 5)^2 \ (2 \ 4)^2 \ (3 \ 0)^2}$$
  
=  $\sqrt{(6)^2 \ (6)^2 \ (3)^2}$  =  $\sqrt{36 \ 36 \ 9}$   
= 9 units

88. (c) Since the centre and radius of the sphere x2 + y2 + z2 + 2 ux + 2vy + 2wz + d = 0 are

$$(-u, -v, -w)$$
 and  $\sqrt{u2 \ v2 \ w2}$  d respectively. So, for the sphere

$$x2 + y2 + z2 + 3x - 4z + 1 = 0,$$
Centre  $\frac{3}{2}$ ,0,2 , and

Radius =  $\sqrt{\frac{3}{2}}^2$  02 (2)2 1

$$\sqrt{\frac{9}{4}} \ 4 \ 1 \ \frac{\sqrt{21}}{2}$$

89. (b)Let two fixed points be A (ae, 0) and B (-ae, 0). Let C (x, y) be a moving point such that AC + CB = constant = 2a (say)

i.e. , 
$$\sqrt{(x-ae)2-(y-0)2}$$
 
$$\sqrt{(x-ae)2-(y-0)2} = 2a$$

Or 
$$\sqrt{x2}$$
 y2 a2e2 2ae

$$\sqrt{x2 \quad y2 \quad a2e2x \quad 2aex} \quad 2a \quad ...(1)$$
  
Or  $l + m = 2a \quad ...(2)$   
Where,  $l2 = x2 + y2 + a2e2 - 2aex \quad ...(3)$   
and  $m2 = x2 + y2 + a2e2 + 2aex \quad ...(4)$   
From, (3) and (4)

or 
$$m2 - l2 = 4aex$$
  
 $(m - l) (l + m) = 4 aex$   
 $2a (m - l) = 4aex[From (2)]$   
 $m - l = 2ex$ 

Adding (2) and (5), we get (5) m = a + ex From (4) and (6), ()6a)ex a2 +e2 x2 + 2aex = x2 +y2 + a2e2 + 2

x2(1-e2) + y2 = a2(1-e2)Dividing both sides by a2(1-e2), we get

$$\frac{x^2}{a^2} = \frac{y^2}{a^2(1 e^2)} = 1$$

Or 
$$\begin{cases} x^2 & y^2 \\ a^2 & b^2 \end{cases}$$
 1, where b2 = a2 (1 - e2)

This is the equation of ellipse.

90. (d) The equation of the parabola is

$$y^2$$
 4x 3 0  
or  $y^2$  4 x  $\frac{3}{4}$  ...(1)

The directrix of the parabola 
$$Y2 = -4aX$$
 ... (2) is  $X = a$ .

On comparing the equation (1) and (2), we

get 
$$4a = 4$$
 and  $X \times \frac{3}{4}$   
or  $a = 1$  and  $X \times \frac{3}{4}$ 

Hence the directrix of the parabola (1) is

$$x = \frac{3}{4} = 1 \text{ or } x = \frac{1}{4} = 0.$$

91. (b) 
$$g(x)$$
.  $g(y) = g(x) + g(y) + g(xy) - 2...(1)$   
Put  $x = 1$ ,  $y = 2$ , then  
 $g(1)$ .  $g(2) = g(1) + g(2) + g(2) - 2$   
 $5g(1) = g(1) + 5 + 5 - 2$ 

4g (1) = 8 
$$g(1) = 2$$
  
Put y  $\frac{1}{x}$  in equation (1), we get

$$g(x).g = \frac{1}{x}$$
  $g(x) = g = \frac{1}{x}$   $g(1) = 2$ 

$$g(x).g \xrightarrow{X} g(x) g \xrightarrow{X} 2 2$$

This is valid only for the polynomial

$$g(x) = 1 + xn$$
 ... (2)  
Now  $g(2) = 5$  (Given)  
 $1 + 2n = 5$  [Using equation (2)]  
 $+ 2n = 4$ ,  $2n = 4$ ,  $-4$ 

Since the value of 2n cannot be –Ve.

So, 2n = 4, n = 2

Now, put n = 2 in equation (2), we get g(x) = 1 + x2

92. (d) 
$$f(x)$$

$$= \begin{cases} 1 & (1 & x^{2} & x^{3} \\ x & 2! & 3! \end{cases}$$
..)  $1 = \begin{cases} \log 21! \\ x & x^{2} & 3! \end{cases}$ 

$$f(x) = log2$$
 1  $x \{ (log2)2 \ 2!$  1

Putting x = 0, we get 
$$f(0) = \log 2 - 1 + 0 + 0 + \dots = -1 + \log 2$$
.

93. (b) Check the continuity of the function f(x) = [tan2 x] at x = 0.

L.H.L. (at x = 0)

$$= \lim_{x \to 0} [\tan 2x] \qquad \lim_{h \to 0} [\tan 2(0 \quad h)]$$

$$= \lim_{h \to 0} [\tan 2 h] [\tan 2 \quad 0] \quad [0] \quad 0$$

R.H.L. (at 
$$x = 0$$
)

$$= \lim_{x \to 0} [\tan 2x] \qquad \lim_{h \to 0} [\tan 2(0 \quad h)]$$

$$= \lim_{h \to 0} [\tan 20] \qquad [0] \quad 0$$

Now, determine the value of f(x) at x = 0.

 $f(0) = [\tan 2 \ 0] = [0] = 0$ 

Hence, f(x) is continuous at x = 0.

94. (c)Let r and V be the respectively radius and volume of the balloon. Let t represents the time. The rate of increament in radius is

2 cm/minute. The volume of the

dt balloon is given by

$$V = \frac{4}{3} r^3$$

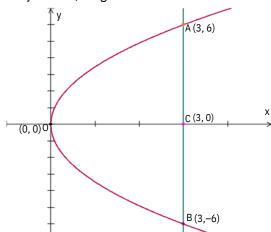
Differentiating w.r. to t, we get

$$\frac{dV}{dt} = \frac{4}{3} (3r2 \underline{ddrt})$$

Substituting the values of and  $\frac{dr}{dt}$ , we get

$$\frac{dV}{dt}$$
 4  $\frac{4}{3}$  (3 52 2) 200 cm3/minute

95. (a)On comparing the equation of the parabola  $y2 = 12 \times \text{ with the standard equation,}$ y2 = 4 ax, we get 4 a = 12 or a = 3.



Hence, the focus, point C will be at (3, 0) and the extremities of the latus-rectum AB will be at (a, 2a) and (a, -2a). So the coordinates of A and B are (3, 6) and (3, -6) respectively. Now we need to find the length ( curve AOB) of the parabola. As it is not a straight line so we cannot directly find the length of this curve as we cannot directly apply Pythagorous theorem. Let us consider a small length ds on the parabola. Using pythagorous theorem for this length,

ds = 
$$\sqrt{(dx)^2 + (dy)^2} = \sqrt{\frac{dx}{dy}^2 + 1dy}$$
  
s  $\frac{6}{6} \sqrt{\frac{dx}{dy}^2 + 1.dy} = ...(1)$ 

From y2 = 12 x 
$$x = \frac{y2}{1}$$
  
 $\frac{dx}{dy} = \frac{2y}{12} = \frac{y}{6}$  Putting in (1),  
 $\frac{6}{36} = \frac{\sqrt{\frac{y}{6}}}{1} = \frac{\sqrt{\frac{y^2}{36}}}{36} = \frac{\sqrt{\frac{y^2}{36}}}}{36} = \frac{\sqrt{\frac{y^2}{36}}}{36} =$ 

$$=\frac{26}{6}\sqrt{y^2+6^2} dy$$

Using 
$$\sqrt{x^2 + a^2} = \frac{x}{2} \sqrt{a^2 + x^2}$$

$$\frac{a^2}{2} \log x \sqrt{a^2 x^2}$$
 C

We get s 
$$\frac{1}{3} \frac{y}{2} \sqrt{62 + y^2} = \frac{62}{2}$$

$$\log y \sqrt{6^2 y^2} C_0^6$$

$$= \frac{1}{3} \frac{6}{2} \sqrt{62 62} 18 \log 6 \sqrt{6^2 6^2}$$

C 0 18log 0 
$$\sqrt{6^2 \ 0}$$
 C

$$= \frac{1}{3} 3.6\sqrt{2} 18\log 6 6\sqrt{2} 18\log 6$$

$$= 6\sqrt{2} 6\log \frac{6(1\sqrt{2})}{6}$$

$$= 6(\sqrt{2} \log(1\sqrt{2})$$

96. (d) I 
$$\frac{x5}{\sqrt{1 + x3}} dx = \frac{x3.x2}{\sqrt{1 + x3}} dx$$
  
Let 1 + x3 = t2, so that 3x2 dx = 2t dt

$$I = \frac{(t^2 - 1) 2tdt}{3} + \frac{2}{3} + t^2 + 1)dt$$

$$= \frac{2}{3} + \frac{t^3}{3} + \frac{2}{3} + \frac{(1 - \frac{x^3}{3})^{3/2}}{3} + \frac{(1 - \frac{x^3}{3})^{\frac{1}{2}}}{3} + \frac{1}{3} + \frac{1}{3$$

(d)The given curve is

$$[4(x \sqrt{2})^{2} \frac{2}{y}] = 8$$

$$4(x \sqrt{2})^{2} y^{2} = \frac{8}{2}$$

$$(x \sqrt{2})^{2} \frac{y}{2}^{2} = \frac{2}{2\sqrt{2}}$$

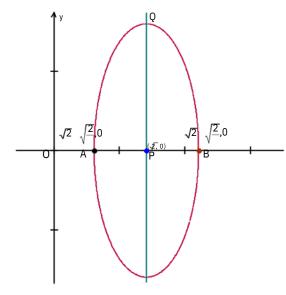
$$\frac{(x \sqrt{2})^{2}}{\sqrt{2}^{2}} = \frac{y^{2}}{2\sqrt{2}} = 1$$
...(1)

This is the equation of the ellipse having centre  $(\sqrt{2},0)$ .

Observe the figure of ellipse (1). The centre

P is 
$$(\sqrt{2},0)$$
. A and B are  $\sqrt{2}$ ,  $\sqrt{\frac{2}{2}}$ , 0 and

$$\sqrt{2}$$
  $\sqrt{\frac{2}{}}$ ,0 respectively.



The required area =  $4 \times$  area of figure PQB

$$= 4 \int_{\sqrt{2}}^{\sqrt{2}} \sqrt{\frac{2}{2}} y dx$$

$$= 4 \int_{\sqrt{2}}^{\sqrt{2}} \sqrt{\frac{8}{2}} \int_{-\frac{1}{2}}^{\frac{8}{2}} 4(x \sqrt{2})^2 dx$$

$$4 2 \int_{\sqrt{2}}^{\sqrt{2}} \sqrt{\frac{2}{2}} \int_{-\frac{1}{2}}^{\frac{2}{2}} (x \sqrt{2})^2 dx$$

$$= 8 \frac{x \sqrt{2}}{2} \sqrt{\frac{2}{2}} (x \sqrt{2})^2$$

$$(2/x) = 1 \times \sqrt{2} \sqrt{2}$$

$$\frac{(2/)}{2} \sin^{-1} \frac{x}{\sqrt{2/}} \sqrt{\frac{2}{2}} \sqrt{\frac{2}{2}}$$

$$\sqrt{a^{2} \times 2} dx \quad \frac{1}{2} x \sqrt{a^{2} \times x^{2}} \quad \frac{a^{2}}{2} \sin^{-1} x \quad C$$

$$= 8 \quad \frac{\sqrt{2} \quad \sqrt{\frac{2}{1}} \quad \sqrt{2}}{2} \sqrt{\frac{2}{1}} \quad (\sqrt{2} \quad \sqrt{\frac{2}{X}} \quad \sqrt{2})2$$

$$1_{\sin 1} \frac{\sqrt{2} \sqrt{\frac{2}{-}} \sqrt{2}}{\sqrt{\frac{2}{-}}} \frac{\sqrt{2} \sqrt{2}}{2}$$

$$\sqrt{\frac{2}{-}} (\sqrt{2} \sqrt{2})^2 \frac{1}{-\sin 1} \frac{\sqrt{2} \sqrt{2}}{\sqrt{2/-}}$$

$$= 8 \frac{1}{\sqrt{\phantom{a}}} (0) + \frac{1}{3} \sin_{-1}(1) - 0 - 0$$

$$8 \frac{1}{2} - 4$$
 square units.

98. (c) Let  $x = \cos 2$ , so that  $dx = -2a \sin \cos d$ 

Now 
$$\int_{0}^{a} \sqrt{\frac{x}{x}} dx$$
  $\int_{\overline{2}}^{a} \sqrt{\frac{a \cos^2}{a\cos^2}}$  (asin cos )d

$$[\frac{1}{2}atx \quad 0; \quad 0atx \quad a]$$

$$= a \int_{0}^{2} \sqrt{\frac{1 \cos^{2}}{\cos^{2}}} 2sin \quad cos \quad d$$

$$\int_{0}^{0} f(x)dx \quad \int_{0}^{t} f(x)dx$$

= 
$$a_0 / 2 \cos ions$$
.  $\cos = a_0 / 2 = a_0 / 2 = a_0 / 2 \cos 2 \sin 2$ 

$$= a \frac{\sin 2}{2} \int_{0}^{2} dx$$

$$= a \int_{2}^{2} \int_{2}^{2} (0 \ 0)$$

$$= a \int_{2}^{2} \int_{2}^{2} dx$$

Separating the variables, we get  $\frac{dy}{dt}$  kdt

Integrating both sides, we get  $\frac{dy}{y}$  kdt

 $\log y = kt + M$  (as y cannot be -ve)

y = ekt+M  $y = eM \cdot ekt$ 

y = C ekt, where C = eM Constant k cannot be positive

Constant k cannot be positive because the population never increases in time. And

another constant C cannot be negative because of eM > 0 always.

Hence y = Cekt, for some constants C > 0 and k < 0.

100.(b)The given circle is, x2 + y2 = a2Differentiating with respect to x, we get

$$2x \quad \begin{array}{cccc} 2y\underline{ddxy} & 0 & & x & y\underline{dd}xy \\ & & 2 & & \\ & x & \underline{yddxy} & 0 & \text{(Squaring both sides)} \end{array}$$

$$x^2$$
  $\frac{2xy}{dx} \frac{dy}{dx}$   $y^2$   $\frac{dy}{dx} \frac{d^2}{dx}$  0

$$2xy \frac{dy}{dx}$$
  $x2$   $y2$   $\frac{dd}{dx}x^{2}$ 

y2 x2 
$$\frac{dy}{y2}$$
 2xy $\frac{dy}{dy}$ x

$$x2$$
  $x2$   $\frac{dy}{x}$   $y2$   $\frac{dy}{x}$ 

(Adding y2 
$$x2 \frac{ddxy^2}{}$$
 both sides)

y 
$$x \frac{dd}{dx} x^2y$$
  $a^2 1 \frac{dy}{dx}^2$ 

$$x^2$$
  $y^2$   $a^2$ 

101. (b) 
$$\left| \frac{dx}{dy} \right| |y| = 3 = 0$$
 Since  $\left| \frac{dy}{dx} \right| = 0$ ,  $|y| = 0$   $\left| \frac{dy}{dx} \right| = |y| = 3 = 3$ 

Hence 
$$\left| \frac{dy}{dx} \right| |y| = 3$$
 0 is not possible.

Therefore, the given differential equation has no solution.

102.(b)The given differential equation is

This is the linear differential equation.

Put y= vx, so that  $\frac{dy}{dx}$  v  $\frac{xdv}{dx}$ . Then

Integrating both sides, we get

Integrating both sides, we get 
$$\frac{dv}{\sqrt{1-v^2}} = \frac{dx}{x}$$

$$\log(v - \sqrt{1-v^2}) - \log x - \log C$$

$$v - \sqrt{1-v^2} - Cx$$

$$y - \sqrt{1-\frac{y^2}{x^2}} - Cx - [-y - vx]$$

$$y - \sqrt{x^2 - y^2} - Cx^2$$

$$103. (b) \sim Q - S - \sim S - Q$$

$$But \sim S - R$$

$$Q - R, True [As P - Q - R - R]$$

Hence ~Q 104.(d)We know that the number of ways of dividing (m+n+p) things into three groups containing m, n and p things respectively

S is true

Further if any two groups out of the three have same number of things then number of ways

Hence number of ways to divide 10 students into three teams one containing four students and each remaining two ton three

105.(d)We observe the following properties:

Reflexivity - Let a be an arbitrary element. Th en,

$$|a \ a| \ 0|0 \ aR/a$$
  
This, R is not reflexive on R.

nCprnq r  ${}^4C2$   ${}^3$   ${}^2$   ${}^1$   ${}^2$ elements, then (a,b) R |a - b| > 0|b - a| > 0b |b a| 4 4 4 4 (b,a) R 109.(b)Performance of the class will be best if mean Thus, (a, b) (b, a) R. So, R is of the marks obtained is maximum but symmetric. standard deviation of the marks obtained is Transitivity – Let (a, b) minimum. R and (b, c) Hence the class which has mean and |a - b| > 0 and |b - c| > 0standard deviation of the marks obtained as |a - c| > 0(a, c) R So, R is transitive. 75 and 5 respectively performs best. 106.(a) Let  $S = \{ai\}$  where i = 1.2....n110.(b)Mean, np = ; and variance, npq = where n From commutative operations, = number of trials and p + q = 1. ai\*aj aj\*ai ... (i) i,j1,2,3....n (1 p)where \* represents a binary operation np Number of distinct elements in S × S p 1 i.e., {ai} {aj} subject to the condition (i) -1 < -p < 0 0 < 1 - p < 1i 1,2...n  $=n\{(a1,a1),(a1,a2),...,(a1,an),$ 0 - 10 < < (a2, a2), (a2,a3),....(a2,an), 111.(b) x + y + z = 02x + 3y + z = 0...(2) ...(an 1,an 1),(an 1,an),(an,an) x + 2y = 0From equation (3), we have n(n 1) n (n 1) (n 2) .... 2 1 x = -2yPutting this value of x in equations (1), we No. of commutative binary operations -2y + y + z = 0 y = z= No. of functions  $f: S \times S$  S subject to (i) = n.n.n....n(n 1) times Hence x = -2zn(n 1) Thus, the solution of the given system of equations is (-2z, z, z), where z is a parameter R). Hence the system has infinite 107.(b) Poisson distribution is a probability number of solutions including zero solution. distribution which is obtained when the probability (p) of the happening of an event is same in all the trials and there are only two 112.(d)Here,  $0 \, a \, 0 \, a^2$ h 0 events in each trials generally says successes and failures probability (p) of the 0 0 0 happening of the event in trial is very less ab but number of trials (n) is very large. O a b0 =1 is very less and Here, p = 5% = 1000 а ab Similarly, 0 ab n = 100, is very large. Hence, one has to employ the Poisson distribution in the given a2b2 qu est i on. 0 108.(d)The probability that a component survives Now. is  $p = \int_{1}^{\pi} . Then q = 1 - p = 1$ a 2<sup>2</sup> 1 0 0 a [pq1] 0 1 0 a 2b2 h 0 n takes the value 4 and r = 2. Hence the a2b2 = 1 ab = 1required probability is

Symmetry – Let a and b be two distinct

1

dn

0 0 0 0

0

 $d_1^1$ 

of x from 1 to 40, there are 40 positive roots, out of which only six roots 1, 2, 3, 4, 5 and 6 are positive integral roots. Hence, probability of getting positive integral roots =  $\frac{3}{40}$ 

20

116. (a) 
$$x4 \sqrt{x4} \sqrt{240} \sqrt{2}$$
  
or  $x4 - 22 = \sqrt{0}$   
Put  $x4 = y$  and square both the sides.  
 $(y - 22)2 = y + 20$   
 $y2 + 484 - 44y = y + 20$   
 $y2 - 45y + 464 = 0$   
 $y2 - 29y - 16y + 464 = 0$   
 $(y - 29)(y - 16) = 0$   
 $y = 16, 29$   
 $x4 = 16, 29$  or  $x = \pm 2, \pm 2.31$ 

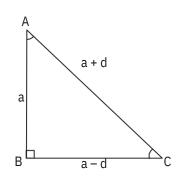
117.(c) Since , be the roots of the equation x2 - ax + b = 0, so each of them must satisfy the equation. Therefore

Now, 
$$\stackrel{2}{A}$$
 b 0...(1) and  $\stackrel{2}{}_{n+1}$  b 0 ...(2)

 $\stackrel{n+1}{} - a A n + b A n - 1 = + \stackrel{n+1}{}_{n+1}$ 
 $- a (\stackrel{n}{}_{n}) + b (n-1+n-1)$ 
 $= n-1(2-a+b) + n-1(2-a+b)$ 
 $= n-1(0) + n-1(0) = 0$  [From (1) & (2)]

118.(a) Let the sides of the triangle be a - d, a, a+d, where d is greater than zero. From the figure, it is clear that the angles A and C are acute angles. Now, by the theorem of Pythagorus, AC2 = AB2 + BC2 (a + d)2 = a2 + (a - d)2 a2 + d2 + 2ad = a2 + a2 + d2 - 2ad 4ad = a2

$$d = a/4$$

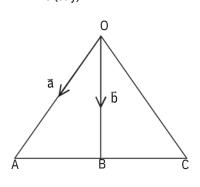


sinC a a 4 a d a 
$$\frac{a}{a}$$
  $\frac{a}{4}$ 

119.(a) The plane containing the line of intersection of the planes() and

Substituting this value for in (i), we get the required plane r.(i 2j 3k) 0

120.(d)In the figure, OAC is a triangle and OB is a median such that



OA OC 20B

Now, the area of the triangle,

$$\frac{1}{2}$$
 $\phi$ A OC  $\left| \begin{array}{cc} \frac{1}{2} \phi & c \\ \end{array} \right|$ 

Her e.

= 
$$\hat{i}(5 \ 9) \ \hat{j}(5 \ 3) \ k(93)$$
  
=  $14i^2 2j^12^k 2(7i^2) \hat{j}(6k^2)$ 

$$\begin{vmatrix} ac \\ = 2\sqrt{(7)2} & (1)2 & (6)2 \end{vmatrix}$$
  
=  $2\sqrt{49} + 1 = 36 + 2\sqrt{86}$ 

$$\frac{1}{2}$$
 2 $\sqrt{86}$   $\sqrt{86}$ .