### **VITEEE 2007 Question Paper**

Vellore Institute of Technology Engineering Entrance Examination

# **SOLVED PAPER**

## 2007

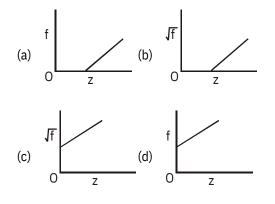
#### PART - I (PHYSICS)

- 1. The magnetic moment of the ground state of an atom whose open sub shell is half filled with five electrons is
  - (a)  $\sqrt{35} \sqrt{\mu B}$  (b)  $35 \mu_B$
  - (c)  $35\sqrt{\mu B}$  (d)  $\mu_B\sqrt{35}$
- 2. Indicate which one of the following statements is NOT CORRECT ?
  - (a) Intensities of reflections from different crystallographic planes are equal
  - (b) According to Bragg's law higher order of reflections have high values for a given wavelength of radiation

(c)r a given wavelength of radiation there is a smallest distance between the crystallographic planes which can be determined

Aragg's law may predict a reflection from a crystallographic plane to be present but it may be absent due to the crystal symmetry

3. Identify the graph which correctly represents the Moseley's law



4. Assuming f to be the frequency of first line in Balmer series, the frequency of the immediate next (i.e. second) line is

(a)	0.50 f	(b)	1.35 f
(c)	2.05 f	(d)	2.70 f

5. The velocity of a particle at which the kinetic energy is equal to its rest energy is

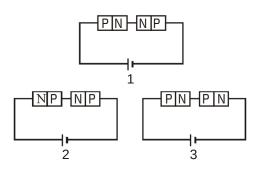
(a) 
$$\frac{3c}{2}$$
 (b)  $3\frac{c}{\sqrt{2}}$   
(c)  $\frac{3c}{2}^{\frac{1}{2}}$  (d)  $\frac{c\sqrt{3}}{2}$ 

6. One electron and one proton is accelerated by equal potential. Ratio in their deBroglie wavelength is

(a) 1 (b) 
$$\frac{m}{e}$$
  
m  
(c)  $\frac{mp}{m_e}$  (d)  $\sqrt{\frac{m}{p}}$ 

- 7. Two electrons one moving in opposite direction with speeds 0.8c and 0.4c where c is the speed of light in vacuum. Then the relative speed is about
  - (a) 0.4c (b) 0.8c (c) 0.9c (d) 1.2 c
- 8. A photo-sensitive material would emit electrons if excited by photons beyond a threshold. To overcome the threshold, one would increase
  - (a) the voltage applied to the light source
  - (b) the intensity of light
  - (c) the wavelength of light
  - (d) the frequency of light

- 9. The radius of nucleus is
  - (a) proportional to its mass number
  - (b) inversely proportional to its mass number
  - (c) proportional to the cube root of its mass number
  - (d) not related to its mass number
- 10. Radio carbon dating is done by estimating in specimen
  - (a) the amount of ordinary carbon still present
  - (b) the amount of radio carbon still present
  - (c) the ratio of amount of 14C to 12Cstill pr esen t
  - (d) the ratio of amount of 12C to 14C still pr esen t
- 11. Ionization power and penetration range of radioactive radiation increases in the order
  - (a) and respectively
  - (b) and respectively
  - (c) and respectively
  - (d) and respectively
- 12. The half life of a radioactive element is 3.8 days. The fraction left after 19 days will be
  - (a) 0.124 (b) 0.062
  - (c) 0.093 (d) 0.031
- 13. Two identical P-N junctions are connected in 1 series in three different ways as shown below to a battery. The potential drop across the P-N junctions are equal in



- (a) in circuits 2 and 3 in
- (b) circuits 1 and 2 in
- (c) circuits 1 and 3 in
- (d) none of the circuit
- 14. The temperature coefficient of a zener mechanism is
  - (a) negative (b) positive
  - (c) infinity (d) zero

15. Identify the logic gate from the following TRUTH table

	Input	ts	Output	
А		В	Υ	
0	0	0 1	11	
( a	ı )	(L C )	0	
In E	Boolea	n algebr 1	a, AB	
	NOR	gate	(b)	NOT gate
	AND	gate	(d)	NAND gate
				is equal to
(a)	ΑB		(b)7	₹ B <sup>_</sup>
(c)	A.B		(d)	A + B

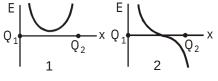
- 17. Radar waves are sent towards a moving airplane and the reflected waves are received. When the airplane is moving towards the radar, the wavelength of the wave
  - (a) decrease

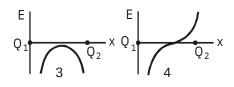
16.

- (b) increase
- (c) remains the same
- (d) sometimes increase or decrease
- 18. The transmission of high frequencies in a coaxial cable is determined by
  - (a)  $\frac{1}{(LC)}$  1/2 where L and C are inductance and
    - capacitance
  - (b) (LC)2(c) the impedance L alone
  - (d) the dielectric and skin effiect
- 19. The output stage of a television transmitter is most likely to be a
  - (a) plate-modulated class C amplifier
  - (b) grid-modulated class C amplifier
  - (c) screen-modulated class C amplifier
  - (d) grid-modulated class A amplifier
- 20. The antenna current of an AM transmitter is 8A when only the carrier is sent, but it increases to 8.93A when the carrier is modulated by a single sine wave. Find the percentage modulation.

(a) 60.1 %	(b) 70.1%
(c) 80.1%	(d) 50.1%

21. Two point like charges Q1 and Q2 of whose strength are equal in absolute value are placed at a certain distance from each other. Assuming the field strength to be posiive in the positive direction of x-axis the signs of the charges Q1 and Q2 for the graphs (field strength versus distance) shown in Figures 1,2,3 and 4 are



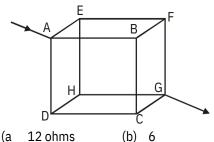


- Q1 positive, Q2 negative; both positive;
   Q1 negative, Q2 positive; both negative
- (b) Q1 negative, Q2 positive;Q1 positive, Q2 negative; both positive; both negative
- (c) Q1 positive, Q2 negative; both negative;Q1 negative, Q2 positive; both positive
- (d) Both positive; Q1 positive, Q2 negative; Q1 negative, Q2 positive; both negative
- 22. ABCD is a rectangle. At corners B, C and D of the rectangle are placed charges + 10 × 10–12C, -20×10–12C and 10 × 10–12C respectively. Calculate the potential at the fourth corner. The side AB = 4cm and BC = 3cm
  - (a) 1.65 V (b) 0.165 V
  - (c) 16.5 V (d) 2.65 V
- 23. A parallel plate capacitor of capacitance 100 pF is to be constructed by using paper sheets of 1 mm thickness as dielectric. If the dielectric constant of paper is 4, the number of circular metal foils of diameter 2 cm each required for the purpose is
  - (a) 40 (b) 20
  - (c) 30 (d) 10

24. Thee lectric field intensity E, due to an electric

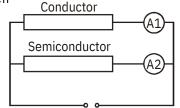
dipole of moment p, at a point on the equaparialleihetois the axis of the dipole and opposite to the direction of the dipole moment p

- (b) perpendicular to the axis of the dipole (c) and
- (c) and
   (d) is directed away from it parallel to the dipole moment perpendicular to the axis of the dipole
- 25. Twelve wires of each of resistance 6 ohms are connected to form a clube as shown in the figure. The current enters at a corner A and leaves at the diagonally opposite corner G. The joint resistance across the corners A and G are



) 3 ohms (d) ohms

26. (c) conductor and a semi-conductor are connected in parallel astroshown in the figure. At a certain voltage both ammeters registers the same current. If the voltage of the DC source is increased then

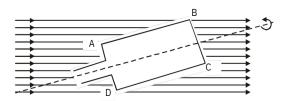


- (a) the ammeter connected to the semiconductor will register higher current than the ammeter connected to the conductor
- (b) the ammeter connected to the conductor will register higher current than the ammeter connected to the semiconductor
- (c) the ammeters connected to both semiconductor and conductor will register the same current
- (d) the ammeter connected to both semiconductor and conductor will register no change in the current

27. A uniform copper wire of length 1m and cross-sectional area 5×10-7m2 carries a current of 1A . Assuming that there are 8×1028 free electrons/ m3 in copper, how long will an electron take to drift from one end of the wire to the other action of the wire to the other action

(a)-	0.0.4.1022	(a)	1.0×1035
(c)	3.2×103s	(d)	6.4×103s

- 28. The temperature coefficient of resistance of a wire is 0.00125/K. At 300K its resistance is
  - 1 .The resistance of the wire will be 2 at
  - (a) 1154 K (b) 1100 K
  - (c) 1400 K (d) 1127 K
- 29. A rectangular coil ABCD which is rotated at a constant angular velocity about an horizontal as shown in the figure. The axis of rotation of the coil as well as the magnetic field B are horizontal. Maximum current will flow in the circuit when the plane of the coil is



- (a) inclined at 30 degrees to the magnetic field
- (b) perpendicular to the magnetic field
- (c) inclined at 45 degrees to the magnetic field
- (d) parallel to the magnetic field
- 30. If the total emf in a thermocouple is a parabolic

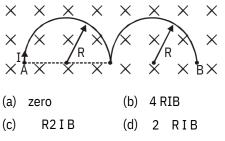
function expressed as E = at +  $\frac{1}{2}$  bt2, which of

the following relations does not hold good

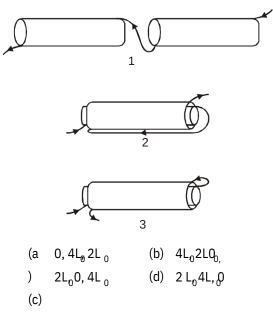
- (a) neutral temperature t = -a/b
- (b) temperature of inversion t = -2a/b
- (c) thermo-electric power p = a + bt
- (d)  $t_n = a/b$
- 31. The proton of energy 1 MeV describes a circular path in plane at right angles to a uniform magnetic field of 6.28 ×10–4T. The mass of the proton is 1.7 × 10–27 Kg.The cyclotron frequency of the proton is very nearly equal to

(a	107	(b)	105
)	Hz	(d)	Hz
(c)	106		104
	Hz		Hz

32. A wire AB, in the shape of two semicircular segments of radius R each and carrying a current I, is placed in a uniform magnetic field B directed into the page (see figure). The magnitude of the force due to the field B on the wire AB is

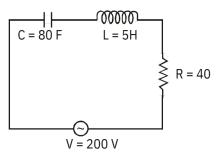


33. There are two solenoids of same length and inductance L but their diameters differ to the extent that one can just fit into the other. They are connected in three different ways in series.
1) They are connected in series but separated by large distance 2) they connected in series with one inside the other and senses of the turns coinciding 3) both are connected in series with one inside the other with senses of the turns opposite as depicted in figures 1,2 and 3 respectively. The total inductance of the solenoids in each of the case 1, 2 and 3 are respectively



34. From figure shown below a series LCR circuit connected to a variable frequency 200V source.

L = 5H, C = 80 F and R = 40. Then the source frequency which drive the circuit at resonance is







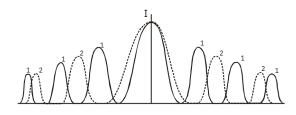
35. If the coefficient of mutual induction of the primary and secondary coils of an induction coil is 5H and a current of 10A is cut off in 5×10−4 second, the *emf* induced(in volt) in the secondary coil is

(a)	5×104	(b)	1×105
(c)	25×105	(d)	5×106

- 36. A voltage of peak value 283 V and varying frequency is applied to a series L, C, R combination in which R = 3 ohm, L=25 mH and C= 400F. The frequency (in Hz) of the source at which maximum power is dissipated in the above is
  - (a) 51.5 (b) 50.7
  - (c) 51.1 (d) 50.3
- 37. Four independent waves are represented by equ at i on s
  - (1)  $X_{\overline{1}}$  asint (3)  $X_{\overline{2}}$  = asin2t (2)  $X_{\overline{3}}$  asin t (4)  $X_{\overline{4}}$  asin(t+)

(2)  $X_{\overline{s}} \operatorname{asin} t$  (4)  $X_{\overline{s}} \operatorname{asin}(t+)$ Interference is possible between waves represented by equations

- (a) 3 and 4 (b) 1 and 2
- (c) 2 and 3 (d) 1 and 4



- (a) is longer than and the ratio of the
- (b) longer to the shorter wavelength is 1.5
- (c) is longer than and the ratio of the
- (d) longer to the shorter wavelength is 1.5 and are equal and their ratio is 1.0 is longer than and the ratio of the longer to the shorter wavelength is 2.5
- 39. In Young's double slit experiment, the interference pattern is found to have an intensity ratio between bright and dark fringes is 9. This implies the (a) (b) (c) (d)
  - the intensities at the screen due to two slits are 5 units and 4 units respectively the intensities at the screen due to the two slits are 4 units and 1 units respectively the amplitude ratio is 7 the amplitude ratio is 6
- 40. Rising and setting sun appears to be reddish because
  - (a) Diffraction sends red rays to earth at these
  - (b) times
  - (c) Scattering due to dust particles and air
  - (d) molecules are responsible Refraction is responsible Polarization is responsible

#### PART - II (CHEMISTRY)

41. The catalyst used in Rosenmund reaction is

(a)	Zn/Hg	(b)	Pd/BaSO4
(c)	Raney Ni	(d)	भ्रुव in Ethanol

- 42. CH<sub>2</sub>CO<sub>2</sub> RM/g<sup>H</sup> ?
  - (a) ROOC(CH),COOR
  - (b) RCOCH CH COOH
  - (c) RCO OR
  - (d) RC OO H

- 43. Identify, which of the below does not possess any element of symmetry?
  - (a) (+)- Tartaric acid
  - (b) Carbon tetrachloride
  - (c) Methane
  - (d)Mesotartatric acid
- 44. The weakest acid amongst the following is (a) CICHCQOH (b) HCOOH (c) FCH CH CQOH (d) CH (I)COQH
- 45. HOOC CH2 , COOH 2C H QH<sub>5</sub>

H2SO4 C2H5OOC CH2 COOC2H5 Toluene

The purpose of using toluene here is

- (a) to make both substances (acid & alcohol) miscible
- (b) that the product is insoluble in toluene
- (c) that the reactants are insoluble in water
- (d) because of the formation of low boiling azotrope
- 46. Trans esterification is the process of
  - (a) conversion of an aliphatic acid to ester
  - (b) conversion of an aromatic acid to ester
  - (c) conversion of one ester to another ester
  - (d) conversion of an ester into its components namely acid and alcohol
- 47. The correct sequence of base strengths in aqueous solution is
  - (a) (CH),  $NH \ge CHNH \ge (CH) N$ 3 3
  - (b)  $(CH)_{N} > (CH) N_{H} > CHNH _{3}$
  - 2  $(CH)_{N} > CH NH_{=} (CH) NH_{32}$ (c)
  - (d) (CH), H > (CH),  $N \ge CH$   $NH_3$
- diazoniumchloride is boiled, the product formed is (a) C H CH OH

2

- (с) С Ӊ С<sub>5</sub>ООН (d) C H QH 49. Carbylamine reaction is given by aliphatic
  - (a) primary amine
  - (b) secondary amine
  - (c) tertiary amine
  - (d) quaternary ammonium salt
- NH 3 2, Ni 50. C6H5CHO ?

- 51. In TeClthe central atom tellurium involves
  - (a) sp3 hybridization
  - (b) sp3d hybridization
  - (c) sp3d2 hybridization
  - (d) dsp2 hybridization
- 52. The purple colour of KMnO is due to the transition L)

Anuclear reaction of 23592Uwith a neutron 53.

> produces 30 Krand two neutrons. Other element produced in this reaction is

- (b) <sup>1</sup>55Cs (a) <sup>1</sup>37/<sub>2</sub>Te
- (c) 1376Ba <sup>144</sup>56Ba
- 54. AgCl dissolves in a solution of NH but not in water because
  - (a) NH is a better solvent than HQ
  - (b) Ag+ forms a complex ion with NH,
  - (c) NH is a stronger base than HQ
  - (d) the dipole moment of water is higher than NH,
- Which of the following is hexadenate ligand? 55.
  - (a) Ethylene diamine
  - (b) Ethylene diamine tetra acetic acid
  - (c) 1, 10- phenanthroline
  - (d) Acetyl acetonato
- A coordinate bond is a dative covalent bond. 56. Which of the below is true?
  - (a) Three atoms form bond by sharing their
  - (b) electrons
  - Two atoms form bond by sharing their (c) electrons Two atoms form bond and one of them provides both electrons
  - (d) Two atoms form bond by sharing electrons obtained from third atom
- 57. Which of the following complex has zero magnetic moment (spin only)?
  - (a) [Ni(NH3)6]Cl2 (b) Na3[FeF6]
  - (c) [Cr(H2O)6]SO4 (d) K4[Fe(CN)6]
- 58. The IUPAC name of [Ni(PPh)CJ]2; is
  - (a) bis dichloro (triphenylphosphine) nickel
  - (b) (II) dichloro bis (triphenylphosphine)
  - (c) nickel (II) dichloro triphenylphosphine
  - (d) nickel (II) triphenyl phosphine nickel (II) dichloride

- 59. Among the following the compound that is both 67. Given the equilibrium system: paramagnetic and coloured is
  - (a) K Cr, O , (b) (NH) [TiCl] 6

(c) VOSO 
$$_4$$
 (d) KGu (CN)  $_4$ 

- 60. On an X-ray diffraction photograph the intensity of the spots depends on
  - (a) neutron density of the atoms/ions
  - (b) electron density of the atoms/ions
  - (c) proton density of the atoms/ions
  - (d) photon density of the atoms/ions
- 61. An ion leaves its regular site occupy a position in the space between the lattice sites is called
  - (a) Frenkel defect (b) Schottky defect
  - (c) Impurity defect (d) Vacancy defect
- 62. The 8:8 type of packing is present in (a) MgF 2 (b) CsCl (d) NaCl (c) KCl
- 63. When a solid melts reversibly
  - (a H decreases (b) G
    - ) E decreases (d) increases S
- 64. (a) thalpy is equal to increases

(a) 
$$-T^2 - \frac{G}{T}_V$$
 (b)  $-T^2 - \frac{G/T}{T}_P$ 

(c) 
$$T^2 - \frac{G/T}{T} = (d) = 2T - \frac{G}{T}$$

65. Condition for spontaneity in an isothermal process is

66. Given:2C s 202 g 2CO2g;

Р

C2H2 g  $2\frac{1}{2}$ O2 g 2CO2 g H2O() ; H -1310kJ

The heat of formation of acetylene is (a)-1802 kJ(b)+1802 kJ (c)+237 kJ(d)-800 kJ

NHÇl (s)  $NH_{\frac{1}{2}}(aq) + Cl_{-}(aq)$ 

( H = +3.5kcal/mol).

What change will shift the equilibrium to the right?

- (a) Decreasing the temperature
- (b) Increasing the temperature
- (c) Dissolving NaCl crystals in the equilibrium mixture
- (d) Dissolving NHNO crystals in the equilibrium mixture
- 68. According to Arrhenius equation, the rate constant (k) is related to temperature (T) as

(a) 
$$In\frac{k_2}{k1} = \frac{E_a}{R} \frac{1}{T_1} - \frac{1}{T_2}$$

(b) 
$$\ln \frac{k}{k1} - \frac{E_a}{R} \frac{1}{T1} - \frac{1}{T2}$$

(c) 
$$\ln \frac{k}{k1} = \frac{Ea}{R} \frac{1}{T1} = \frac{1}{T2}$$

(d) 
$$In \frac{k_2}{k_1} - \frac{E_a}{R} \frac{1}{T_1} \frac{1}{T_2}$$

69. Equivalent amounts of H<sub>2</sub> and I are heated in a closed vessel till equilibrium is obtained. If 80%

of the hydrogen can be converted to HI, the Kc at this temperature is (b) 16

- 70. For the reaction H(g)+I(g), 2HI(g), the equilibrium constant Kp changes with
  - (a) total pressure
  - (b) catalyst
  - (c) the amount  $H_2$  and  $I_2$
  - (d) temperature
- 71. How long (in hours) must a current of 5.0 amperes be maintained to electroplate 60g of calcium from molten CaCl?

(a) 27 hours (b) 8.3 hours

(c) 11 hours (d) 16 hours

72. For strong electrolytes the plot of molar

conductance vs  $\sqrt{Cis}$ 

- (a) parabolic (b) linear
- (c) sinusoidal (d) circular

- 73. If the molar conductance values of Ca2+ and Cl- at infinite dilution are respectively 118.88×10-4 m2 mho mol-1 and 77.33×10-4 m2 mho mol-1 then that of CaCl is (in m2 (a)ho 119.39 × 10-4 (b) 154.66 × 10-4 (c) 273.54 × 10-4 (d) 196.21×10-4
- 74. The standard reduction potentials at 298K for the following half reactions are given against each
  - Zn2+ (aq) + 2e- Zn(s)  $E_{\overline{0}} 0.762 V$  

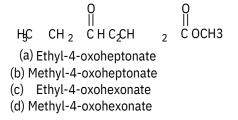
     Cr3+ (aq) + 3e- Cr(s)  $E_{\overline{0}} 0.740 V$  

     2H+ (aq) + 2e- H(g)  $E_{\overline{0}} = 0.00 V$ 
     $Fe3+ (aq) + 3e- Fe2+ (aq)E_{\overline{0}} + 0.762 V$  

     The strongest reducing agent is

     (a) Zn(s) (b) Cr(s) 

     (c) H(g) (d) Fe2+ (aq)
- 75. The epoxide ring consists of which of the following ?
  - (a) Three membered ring with two carbon and one oxygen
  - (b) Four membered ring with three carbon and one oxygen
  - (c) Five membered ring with four carbon and one oxygen
  - (d) Six membered ring with five carbon and one oxygen
- 76. In the Grignard reaction, which metal forms an organometallic bond?
  (a) Sodium
  (b) Titanium
  (c) Magnesium
  (d) Palladium
- 77. Phenol is less acidic than
  - (a) p-chlorophenol
  - (b) p-nitrophenol
  - (c) p-methoxyphenol
  - (d) ethanol
- 78. Aldol condensation is given by
  (a) trimethylacetaldehyde
  (to)etaldehyde
  (to)nzaldehyde
  (d) formaldehyde
- 79. Give the IUPAC name for



- 80. In which of the below reaction do we find , unsaturated carbonyl compounds undergoing a ring closure reaction with conjugated dienes?
  - (a) Perkin reaction
  - (b) Diels-Alder reaction
  - (c) Claisen rearrangement
  - (d) Hoffman reaction

#### **PART - III (MATHEMATICS)**

81. Let the pairsa,b andc, d each determine a plane. Then the planes are parallel if

(a)	a c	b d	0
(b)	a c	b d	0
(c)	a b	c d	0
(d)	a b	c d	0

82. The area of a parallelogram with  $3i^{j}-2k^{a}$  and  $4k_{3i}as$  diagonals is

(a)	$\sqrt{72}$	(b)	$\sqrt{73}$
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- (c)  $\sqrt{74}$  (d)  $\sqrt{75}$
- 83. If cosx + cos2 x =1then the value of sin12 x+ 3sin10 x + 3sin8x + sin6 x-1 is equal to (a) (c) The product of (b) values of (cos1 (d) 0
- 84. equal to +i sin )3/5 is

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(a) 1 (b) cos +i sin

(c) cos3 +i sin3 (d) cos5 +i sin5

85. The imaginary part of 
$$\frac{1}{i} \frac{i^2}{2i-1}$$
 is

(a) 
$$\frac{4}{5}$$
 (b) 0

(c)  $\frac{-}{5}$  (d)  $-\frac{4}{5}$ 

86. If 
$$\sin^{-1}x \sin^{-1}y = \frac{1}{2}$$
, then  $\cos^{-1}x + \cos^{-1}y$  is 93. If  $(x + y)\sin u = x2y2$ , then  $\frac{u}{x} y - \frac{u}{y}$   
equal to  
(a)  $\frac{1}{2}$  (b)  $\frac{1}{4}$  (c)  $\frac{1}{2}$  (b)  $\frac{1}{4}$  (c)  $\frac{1}{2}$  (b)  $\frac{1}{4}$  (c)  $\frac{1}{2}$  (b)  $\frac{3}{2351}$  (c)  $\frac{2351}{2048}a^{113}$  (c)  $\frac{23311}{2048}a^{113}$ 

98. The value of the integral  $e^x \frac{1-x}{1} \frac{2}{x^2} dx$  is

(a) 
$$ex \frac{1-x}{1-x^2} C$$
  
(b) 
$$ex \frac{1-x}{1-x^2} C$$
  
ex

(c) 
$$\frac{1}{1} \times 2$$
 (d)  $ex(1-x) + C$ 

(a)

99. If xsin 
$$\frac{y}{x}$$
 dy ysin  $\frac{y}{x}$  -x dx

and y1  $\frac{1}{2}$ , then the value of cos  $\frac{y}{x}$  is equal to

(a) x (b) 
$$\frac{1}{x}$$

100.The differential equation of the system of all circles of radius r in the XY plane is

(a) 1 
$$\frac{dy}{dx}^{3}^{2}$$
  $r^{2}$   $\frac{d^{2}y}{2}^{2}$   
(b) 1  $\frac{dy}{dx}^{3}^{2}$   $r^{2}$   $\frac{d^{2}y}{2}^{3}$   
(c) 1  $\frac{dy}{dx}^{2}^{3}$   $r^{2}$   $\frac{d^{2}y}{2}^{2}$   
(d) 1  $\frac{dy}{dx}^{2}$   $r^{2}$   $\frac{d^{2}y}{2}^{3}$ 

101. The general solution of the differential equation

$$\frac{d^{2}y}{dx^{2}} 2\frac{dy}{dx} y 2e^{3x} \text{ is given by}$$
(a)  $y c_{1} c2x e^{x} \frac{e^{3x}}{8}$   
(b)  $y c_{1} c2x e^{-x} \frac{e^{-3x}}{8}$   
(c)  $y c_{1} c2x e^{-x} \frac{e^{3x}}{8}$   
(d)  $y c1 c2x e^{x} \frac{e^{-3x}}{8}$ 

102. The solution of the differential equation

ydx+(x-y3)dy = 0 is  
(a) xy 
$$\frac{1}{3}$$
y3 C (b) xy = y4 + C  
(c) 3 (d) 4y = y3 + C  
y4 = 4xy + C

103.The number of positive integral solutions of the equation x xxxx=1050 is

equ	анон қ хаха	21020 IS		
(a)	1870 -	(b)	1875	
(c)	1865	(d)	1880	
104.	Let A= {1,2,3	8,, n}and	d B ={a,b,c}, t	hen the
num	ber of functi	ons from A	to B that are	onto is
(a)	3n – 2n 3 (2n – 1)	(b)	3n – 2n –1	
(c)	3 (2n – 1)	(d)	3n – 3(2n – 1	1)
05.Every	/body in a ro	om shakes	s hands with	

105.Everybody in a room shakes hands with everybody else. The total number of hand shakes is 66. The total number of persons in the room is

(a)	9	(b) 12
(c)	10	(d) 14

106.If(G,\*) is a group and the order of an element aG is 10, then the order of the inverse of  $a^* a$  is (a)

10 (b) 
$$\frac{1}{10}$$
  
(c) 5 (d)  $\frac{1}{5}$ 

107.A box contains 9 tickets numbered 1 to 9 inclusive. If 3 tickets are drawn from the box one at a time, the probability that they are alternatively either {odd, even, odd} or {even, odd, even} is

(a) 
$$- \begin{array}{c} 5\\ 17 (b) \\ 5\\ 16 (d) \\ \hline 18 \end{array}$$

108. If 
$$P(A) = \frac{1}{12}$$
,  $P(B) = \frac{5}{12}$  and  $P(B/A) = \frac{1}{15}$  then  
p A B is equal to  
(a)  $\frac{89}{180}$  (b)  $\frac{90}{180}$   
(c)  $\frac{91}{180}$  (d)  $\frac{92}{180}$   
109. If the probability density function of a random  
variable X is  $f(x) = \frac{x}{2}$  in 0 x 2, then  
 $P(X > 1.5 X > 1)$  is equal to  
(a)  $\frac{7}{16}$  (b)  $\frac{3}{4}$   
(c)  $\frac{7}{12}$  (d)  $\frac{2}{1}$   
110. If X is a poisson variate suctofthat  
 $2P(X = 0) + P(X = 2) = 2P(X = 1)$  then E(X) is  
equal to  
(a) 1 (b) 2  
(c) 1.5 (d) 1.75  
111. If A 1 tan  
 $-tan 1$  and AB = I, then  
(cos 2)B is equal to  
(a) A() (b) A  $\frac{-}{2}$   
(c) A(-) (c) A  $\frac{-}{2}$   
112. If  $x = -5$  is a root of  $\begin{vmatrix} 2x & 1 & 4 & 8 \\ 2 & 2x & 2 \\ 7 & 6 & 2x \end{vmatrix} = 0$ , then  
the other roots are  
(a 3, 3.5 (b) 1, 3.5)  
1.7 (c) 2, 7  
113. The simultaneous equations Kx + 2y-z = 1,  
(K - 1)y-2z = 2 and (K + 2)z = 3 have only one  
solution when  
(a) K = -2 (b) K = -1  
(c) K = 0 (c) (K = 1)

-1 2 5 114. If the rank of the matrix 2 - 4 a - 4 is 1, 1 -2 1 then the value of a is (a) -1 (b) 2 (d) 4 (c) -6 115. If 4ac for the equation ax4 + bx2 + c = 0, then **bl** the roots of the equation will be real if (a) b>0, a<0, c>0 (b) b<0, a>0, c>0 (c) b>0, a>0, c>0 (d) b>0, a>0, c<0 116. If x > 0 and  $\log x_3 + \log(x_3 - \sqrt{x}) + \log(3(\sqrt{x}) + \sqrt{x})$  $\log_3 \sqrt[8]{x} + \log_3 \sqrt[16]{x} + \dots = 4$ , then x equals (a) 9 (b) 81 (d) 27 (c) 1 117. The number of real roots of the equation  $x \stackrel{1}{-x}^{3} x \stackrel{1}{x} 0$  is 0 (b) 2 (a) 4 (c) (d) 6

118.If H is the harmonic mean between P and Q, then

the value of 
$$\frac{H}{P} = \frac{H}{Q}$$
 is

(a)	2	(b)	PQ PQ
(c)	$\frac{1}{2}$	(d)	PQ PQ

119.If aand bare two unit vectors, then the vector

 $(a+b) \times (a \times b)$  is parallel to the vector

(a) <sub>a+b</sub>	(b)	2a +b
--------------------	-----	-------

- (c) a -b (d) 2a -b
- 120.If is the angle between the lines AB and AC where A, B and C are the three points with coordinates (1,2,-1), (2,0,3), (3,-1,2) respectively,

ther	$\sqrt{462}\cos$	is equal t	0
(a)	20	(b)	10
(c)	30	(d)	40

#### 2007 SOLUTIONS

#### PART - I (PHYSICS)

1. (d) The magnetic moment of the ground 5. state of an atom whose open sub-shell is half filled with n electrons is given by

> $\sqrt{n(n \ 2)}$ . B where B is the gyromagnetic moment of the atom. Here, n = 5.5(5  $\sqrt{2}$ ). B  $\sqrt{35}$  B

- 2. (a) Bragg's law gives 2dsin = n, n= order of reflection, d= distance between planes.
   Forme and d, n for a given, smallest d for least n, can be found. If crystal is symmetric reflections from different planes may cancel out.
- (b)According to Moseley's law, square root of frequency of X-ray is plotted against atomic number it gives straight line, the relation is

$$\sqrt{f}$$
 cZ–1where c = constant

(for  $\sqrt{f}$  0,Z c, for Z = 0,  $\sqrt{f}$  -c) Option (b) is correct. as Z can not be n egative.

4. (b) Balmer series is given for n = 2 and  $n^2 = 3, 4, ...$ 

Rc 
$$\frac{1}{2^2} - \frac{1}{n_2^2}$$

For Ist line in spectrum  $n^2 = 3$ 

$$\begin{array}{c} 1 \quad \text{Rc} \quad \frac{1}{2^2} - \frac{1}{n_2^2} \quad \text{Rc} \quad \frac{1}{4} - \frac{1}{9} \quad \text{f} \\ f \quad \frac{5}{36} \text{Rc} \quad \text{Rc} \quad \frac{36}{5} \text{f} \end{array}$$

For second line  $n^2 = 4$ 

$$_{2}$$
 Rc  $\frac{1}{22}$   $\frac{1}{42}$  Rc  $\frac{1}{4}$   $\frac{1}{16}$ 

$$_{2} \quad \frac{3}{16} \operatorname{Rc} \quad \frac{3}{16} \quad \frac{36}{5} \operatorname{f} \quad 1.35 \operatorname{f}.$$

(d) Here, Kinetic energy = Rest energy we know that Kinetic energy (Relativistic) = (m - m)c2,

and Rest energy = mc2, where m = rest mass, c = velocity of light Also, mass (m) of a particle moving with velocity v is given by

m 
$$\frac{m_0}{\sqrt{1 \frac{v^2}{c^2}}}$$
.  
(m - m)c<sup>2</sup> = mc<sup>2</sup> provides

$$\frac{m0}{\sqrt{1 - \frac{v^2}{c^2}}} m_0 c^2 mc^2$$
  
or,  $\frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$  1 1  
or,  $\frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$  2 or,  $1 \frac{v^2}{c^2} \frac{1}{4}$   
or,  $\frac{v^2}{c^2}$  1  $\frac{1}{4} \frac{3}{4}$   
 $v \frac{\sqrt{3}}{2}c$ .  
 $1 - \frac{v^2}{c^2} = \frac{1}{4}$   
 $\frac{v^2}{c^2} = 1 \frac{1}{4} = \frac{3}{4}$   $v^2 = \frac{3}{4}c^2$   
 $v = \sqrt{\frac{3}{2}}c$ 

6. (d) de-Broglie wavelength () of a particle of 10. (c) Radio carbon dating is done by measuring mass m and moving with a velocity v is ratio of 14C present in the sample, since

given by,  $\frac{h}{mv}$ , where h is Planck's constant. mvWhen a particle having charge q is accelerated through a potential V then

$$qV = \frac{1}{2}mv^2$$

h /2maV

Hence, de-Broglie wavelength of electron,

$$e \frac{h}{\sqrt{2meV}}$$

and de-Broglie wavelength of proton,

$$_{p} \quad \frac{h}{\sqrt{2m_{B}V}}$$
 , where e represents the

charge of electron (or proton)

$$\frac{e}{p} \sqrt{\frac{m_p}{m}}$$

7. (c) Relative speed is given by

$$u = \frac{u' \cdot v}{1 \cdot \frac{u' \cdot v}{c^2}}$$

Here, u' = 0.8 c and v = 0.4 c

u 
$$\frac{0.8c \ 0.4c}{1 \ \frac{(0.8c)(0.4c)}{c^2}} = \frac{1.2}{c} = 0.9 c.$$

- 8. (d) By Einstein's equation, Shotoemission
   Ocicers when h > 0 or h > h 17
   frequency of incident photon is greater than threshold frequency.
- 9. (c) Radius of nucleus is given by R A1/3 R ROA  $^{1/3}$ , where A = mass number

- (c) Radio carbon dating is done by measuring ratio of 14C present in the sample, since proportion of 14C and 12 C in a body is same; but after death 14C decays. Hence knowing the present ratio of 14C to 12 C, sample can be dated.
- (b) particles are positively charged He nucleus, it can accept 2e-, rays are negatively charged which are similar to e-, can donate 1e-, are radiations. Hence ionisation power of is maximum. are most energetic and is least energetic Penetration power of is maximum
- 12. (d) Given half life T= 3.8 days; t = 19 days

$$\frac{N}{N0} \quad ?now \stackrel{1}{=} \quad \frac{19}{3.8} \quad 5$$

$$\frac{N}{N0} \quad \frac{1}{2} \stackrel{\frac{t}{T}}{=} \quad \frac{1}{2} \stackrel{5}{=} \quad \frac{1}{32}$$

$$N \quad \frac{N_0}{0} \quad 0.03N_0$$

32

- 13. (a) If the p-n junctions are identical, then their resistances would be same. In circuit 1, the first p-n function is forward biased and second is reverse biased. Hence the voltages across them would be different. In circuit 2 both are reverse biased. So potential drop would be same. In circuit 3 both are forward biased; again voltages would be same. Zener diode is a semiconductor device and for
- semiconductors, temperature coefficient is negative The truth table corresponds to
   (a) the logic

A Bhence it is NOR gate.

16. (d)  $\overrightarrow{A.B}$  in Boolean algebra, can be written as

17. (a) By Dopplers effect, if source moves towards the observer, frequency received will increase.

As

1

wavelength will decrease.

- 18. (d) A coaxial cable consists of a conducting wire surrounded by a dielectric space, over which there is a sleeve of coppermesh covered with a shield of PVC insulation. The power transmission is regulated by dielectric. At high frequencies energy loss due to mesh is significant (called skin effect). Due to their inherent distortion, plate-
- 19. (b) modulated class C amplifiers are not used as audio amplifiers. Also, class A amplifiers are not used owing to low efficiency. A grid- modulated amplifier has very high frequency. Therefore, in output stage of a TV transmitter, gridmodulated class C amplifier is used. The rms value of carrier current is I c = 8A.

20. (b)

The rms value of modulated current

= Ic + Im = 8.93 A = It Percentage modulation =  $na \times 100$ 

The current relation in AM wave is

$$\frac{I_{t}^{2}}{I_{t}^{2}} = 1 - \frac{m_{a}^{2}}{2} - m_{a} - \sqrt{\frac{I_{t}^{2}}{I_{t}^{2}}} - 1 - 2$$
Modulation index, m<sub>a</sub>  $\sqrt{\frac{8.93^{2}}{8^{2}}} - 1 - 2$ 

$$\sqrt{\frac{79.7}{64} - 1 \ 2} \quad \sqrt{1.24 - 1 \ 2} = 0.701$$

Percentage modulation =  $\mathfrak{m} \times 100 = 70.1\%$ 

21. (d) For a point charge, E 
$$\frac{1}{x^2}$$
. For positive

charges, electric field will decrease in positive direction as distance increases, (case 1), for negative charge, as distance increases field will increase (case 4). As we

move from positive charge to negative charge, field will keep on decreasing (case 2), As we move from negative to positive charge, field will keep on increasing (dase 3) B(q 1)

22. (a) 
$$3 \text{ cm}$$
  
D(q 3)4 cm  
C(q 2)

AC 
$$\sqrt{4^2 \ 3^2} \ \sqrt{25} \ 5 \text{ cm.}$$
  
Potential at A = VB + VC + V<sub>D.</sub>  
 $V_A \ \frac{1}{4} \ 0 \ \frac{q^1}{AB} \ \frac{q^2}{AC} \ \frac{q^3}{AD}$   
 $V_A \ 9 \ 109 \ \frac{4}{4} \ \frac{1^{-12}}{0^{-2}} \ \frac{-20 \ 10^{-12}}{5 \ 10^{-2}} \ \frac{10}{3} \ \frac{1^{-12}}{0^{-2}}$   
 $9 \ 109 \ 10^{-10} \ \frac{10}{4} \ \frac{-20}{5} \ \frac{10}{3} \ 0$   
 $0.9 \ \frac{150 - 240}{60} \ \frac{200}{60}$   
 $\frac{0.9 \ 110}{4} \ 1.65V$ 

23. (d) The capacitance (C) of a parallel plate capacitor with dielectric is given by

$$C = \frac{0 A}{d-t 1 - \frac{1}{K}}$$

60

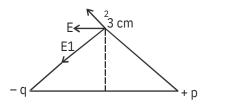
C = 100 pF =  $100 \times 10 - 12$  F<sub>7</sub> 8.85 ×  $10^{12}$ .  $A = r^2 = 3.14 \times (10 - 2)^2 (r = lcm)$ t = 10–3m, d = t, K = 4

C1 
$$\frac{8.85 \ 10^{-12} \ 3.14 \ 10^{-4}}{10^{-3} - 10^{-3} (1 - \frac{1}{4})}$$
$$\frac{27.79 \ 10^{-16}}{10 - 3 - 0.75 \ 10^{-3}}$$
$$\frac{27.79 \ 10^{-13}}{0.25}$$
$$\frac{27.79 \ 10^{-13}}{0.25} \ 111.16 \ 10^{-13} \text{F}$$
(for 1 set)

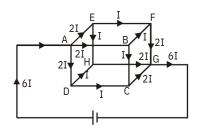
Required C =  $100 \ 10^{-12}$ F

n 
$$\frac{C}{C1}$$
  $\frac{100 \, 10^{-12}}{111.16 \, 10^{-13}}$  10

24. (a) The resultant intensity at a point on 26. (c) equatorial line is E. Eis parallel and opposite to direction of p.



25. (d) Let a total current of 6I enter at A. It divides into three equal parts, each of 2I, along AE, AB and AD. At E, B and D each the current 2I divides into two equal parts, each of I, along EF, EH, BF, BC, DH and DC. At F, H and C, the two currents each of I, combine together to give a current of 2I at each corner. Thus, at G we get the same current 6I as shown in the figure.



Let r be the value of resistance of each arm of the cube and R be the joint resistance across the conners A and G. Applying Kirchhoff's law along the loop AEFGA, we get 2Ir + Ir + 2Ir = E or, 5Ir = E ......(1) Also, by Ohm's law,  $6I \times R = E$ 6IR = 5Ir, using (1) or, R  $\frac{5}{6}$ r. Here, r = 6 (c) Since conductor and semiconductor are connected in parallel hence voltage across them is same. If ammeters show same

> reading hence their resistances R  $\frac{V}{I}$  are same. If voltage is increased by small value Ifteen following the same relation V constant R, both conductor and semiconductor show same current.

27. (d) Time taken by free electrons to cross the conductor

t \_\_\_\_ where drift velocity vd 
$$\frac{I}{neA}$$

$$v_{\rm d} = \frac{1}{8 \ 10^{28} \ 1.6 \ 10^{-19} \ 5 \ 10^{-7}}$$
  
 $\frac{10^{-2}}{64} \, {\rm m/s.}$ 

t  $\frac{1}{vd}$   $\frac{64}{10-2}$  64 102s 6.4 103sec

28. (b) Temperature coefficient, 
$$\frac{R2 - R_1}{R1 t 2 r_1 t}$$

$$t_2 - t1 = \frac{R2 - R1}{R1}$$

$$t^{2-t1} \quad \frac{2-1}{1\ 0.00125}$$

29. (d) Torque on the coil is = nIB A cos. If coil is set with its plane parallel to direction of magnetic field B, then =0°, cos = 1
= nIBA.1 = nIBA = maximum.
Hence, I = maximum (as n,B, A are constant)

30. (d) E at  $\frac{1}{2}$  bt2is the parabolic equation for

thermo emf. The thermoelectric power is

$$S = \frac{dE}{dt}$$

S = a + bt. The graph betwee  $\frac{dE}{dt}$ 

and straight line.

Here, r = 6 R  $\frac{5}{6}$  6 5

When t = 0, S = a (intercept). At neutral temperature  $\frac{dE}{dt}$  0 and  $t = t^n$   $0 = a + bt^n$   $t_n$   $\frac{-a}{b}$  and at cold junction ti 2tn  $\frac{-2a}{b}$ 35. (b)M = 5 31. (d) Energy of proton = K.E. = 1MeV = 106 eV.Bq Frequency 2m 6.28 10-4 <sup>+</sup> <u>1.6</u>10 <sup>-19</sup> 2 3.14 1.7 10 -27 0.910 Hz  $10^4 \text{Hz}$ 32. (d) Force on a conductor of length due to a magnetic field of strength B is given by F I(B) F I Bsin Here, = 90° F IB Ι R B RIB Therefore, a force of magnitude (RIB) will act on each wire. The direction of the forces on each wire will be same. Thus. total force on the wire AB = RIB + RIB= 2RIB33. (d) In first case, the two inductances are in series hence total inductance = LO + LO $= 2L_0$ In second case, the current is same, but no. of turns has doubled since the sense of turning is same. 2n <sup>2</sup> n2 Thus L L hence inductance  $L = 4L_0$ In third case, the sense of turns is opposite. So net inductance cancel each other L= 0 34. (b) At resonance, impedance of circuit is minimum.When impedance of capacitor anductor is same, XL = XC Resonance  $\frac{1}{2 \sqrt{LC}}$ 

frequency

$$\frac{1}{2 \sqrt{58010^{-6}}} \frac{1}{2 \sqrt{40010^{-6}}}$$

$$\frac{1}{2 \sqrt{40010^{-6}}}$$

$$\frac{1}{2 \sqrt{40010^{-6}}}$$

$$\frac{1}{3 \sqrt{400}}$$

$$\frac{1}{40}$$

$$\frac{25}{4}$$

$$\frac{1}{40}$$
, I = 10 A, t = 5 \times 10 - 4 s.

Now, emf induced in secondary is

e 
$$-M \frac{dI}{dt}$$
, (-ve sign shows direction)

e 5 
$$\frac{10}{5 \ 10^{-4}}$$
 1 10 5V

36. (d) Average power of an LCR circuit is P = EvIvcos. Maximum power is dissipated at resonance when X = XC. The resonance frequency is given by

$$\frac{1}{2 \sqrt{LC}}$$

$$\frac{1}{2 3.14 \sqrt{25 10^{-3} 400 10^{-6}}}$$

$$\frac{1}{2 3.14 5 20 10^{-5} \sqrt{10}}$$

$$\frac{105}{3.14 200 \sqrt{10}}$$

$$\frac{10^3}{6.28 \sqrt{10}} \frac{159.2}{3.16} 50.31 \text{ Hz}$$

- 37. (d) Coherent sources should have same frequency and wavelength and constant or zero phase difference. Frequency is same only for wave X1 and X4 and phase difference =
- 38. (c) Since position of central maximum is same, hence asin = is same for both wavelengths. i.e., a = constant, = same. is same for both waves

and 
$$\frac{1}{2}$$
 1

39. (b) For bright fringes,  $I_{max} = (a + b)^2$ For dark fringes,  $I_{min} = (a - b)^2$ 

Now 
$$\frac{I_{max}}{I_{min}} = 9 - \frac{a + b^2}{a - b^2} + \frac{a + b}{a - b} = 3a - 3b$$
  
 $a + b = 3(a - b) + a + b = 3a - 3b + 2a = 4b$ 

$$\frac{a}{b}$$
 2  $\frac{a^2}{b^2}$  4

Ratio of intensities of the two slits,

$$\frac{I_1}{I_2} \quad \frac{a^2}{b^2} \quad \frac{4}{1}$$

40. (b) Rising and setting sun appears red because light from the sun travels slightly more distance from the horizon, than when it is overhead. Hence blue light is scattered by dust in the atmosphere because scattering

$$\frac{1}{4}$$
 and  $b < r$ . Red colour is less

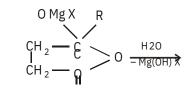
scattered and reaches us.

#### PART - II (CHEMISTRY)

41. (b) Roseumund's reaction –

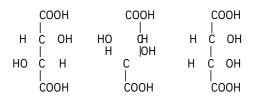
RCOCI H<sub>2</sub> Pd / BaSO4 RCHO HCl

42. (b)  $\underset{CH}{\overset{CH 2 \in \Theta}{I}} > O + RMg X \longrightarrow$ 



$$R - C_{II} - CH_{2} - CH_{2} - COOH$$

43. (a) (+) – Tartaric acid does not have element of symmetry.



(+) – Tartaric acid (A) Meso tartaric acid (D) (Plane of symmetry)

- 45. (a) Toluene is used in the reaction to make both substances (acid and
- 46. (c) alcohol) miscible. Trans esterification is the process of conversion of one ester to another €€€€€0R' + R"OH RCOOR" + R'OH
- 47. (a) It is expected that the basic nature of amines should be in order tertiary > secondary > primary but the observed order in the case of lower members is found to be as secondary > Primary > tetriary. This anomalous behaviour of tetriary amines is due to steric factors i.e crowding of alkyl groups cover nitrogen atom from all sides thus makes the approach and bonding by a proton relatively difficult which results the maximum steric strain in tetiary amines. The electrons are there but the path is blocked, resulting the reduction in basicity. Thus the correct order is

R2 NH > R NH2 > R3N.

48. (d) 
$$C_{652}^{HN+C-}$$
 l + H2O   
C 6H5

C 6H5OH + N2 + HCl Ph en ol

L

М.

53. (d)  ${}^{235}_{92U} {}^{1}_{0}n$   ${}^{144}_{56}Ba {}^{9}_{2}Kr {}^{1}_{0}n$ 

Sum of atomic number of reactants = sum of atomic masses of products.

54. (b) AgCl dissolves in a solution of NH 3 but not in water because Ag+ forms soluble complex ion with NHB.

55. (b) EDTA is hexadentate ligand. 4 oxygen and 2 nitrogen atoms act as donars.

56. (c) A co-ordinate bond is a dative covalent bond in which two atoms form a bond and one of them provides both electrons.

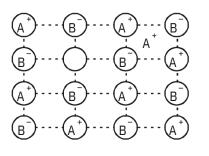
57. (d) [Ni(NH)] 
$$\mathcal{L}_2$$
 sp3d2<sub>hybridisation</sub>

2 unpaired electrons Na<sub>3</sub>[FeF<sub>6</sub>] sp **3** Aybridisation 3 unpaired electrons [Cr(H O)]SO<sub>4</sub> d2sp hybridisation 3 unpaired electrons

K[Fe(CN)] <sub>6</sub> d2sp3hybridisation No unpaired electrons Zero magnetic momoment means all the electrons paired.

- 58. (c) The IUPAC name is dichloro triphenyl phosphine nickel (II).
- 59. (c) (d) **Diffe**(CN)6] Cu is in + 1 oxidation state hence has no unpaired electron hence colourless and diamagnetic.
  - (b) In (NH4)2 [TiCl6] Ti is in + 4 oxidation state. hence has no unpaired electron hence colourless and diamagnetic.
  - (c) In VOSO +4 oxidation state hence has one unpaired electron, thus it is coloured and paramagnetic.
  - In K2Cr2O7, Cr is in +6 oxidation. hence has no unpaired electron and thus it 2Cr2O7 has. Is diamagnetic. Though K no unpaired electron but it is coloured. This is due to charge transfer spectrum.
- 60. (b) On an X-ray diffraction photograph the intensity of the spots depends on electron density of atoms/ions.

61. (a) In Frankels defect an ion leaves its regular site and occupy a position in the space between the lattice sites.



- 62. (b) 8:8 type of packing is present in CsCl. 6:6 type of packing is present in NaCl and KCl.
- 63. (d)When solid melts S increases. because when solid changes into liquid randomness increases.

64. (G)bbs Helmholtz Equation-

G H-T S ......(1) differentiate this equation w.r.t. temperature at constant pressure

$$\frac{G}{T} = \frac{G_y}{P} + \frac{G_y}{T} = \frac{G_x}{T} = \frac{G_x}{T} = \frac{G_y}{T} = \frac{G_y}$$

on combining equation (1) & (3) we get

$$G H T - \frac{G}{T}_{P} \dots (4)$$

Equation (4) is on alternative form of Gibbs Helmholtz equation Dividing equ. (4) by T2, we get

$$\frac{G}{T^2} \quad \frac{H}{T^2} \quad \frac{1}{T} \quad \frac{G}{T} \quad P$$

on rearrangement, we get

$$\frac{G}{T} - \frac{H}{P}$$

$$H -T2 - \frac{G}{T}$$

\_

65. (a) Since G A P. V For a spontaneous process Gshould be negative which is possible only if AP.VorAW 0.

 $2C_{(s)}$  H $_{2(g)}$  C $_{2}H_{2(g)}$  H ? This is the equation for formation of acelytene Given

 $2C_{(s)} 2O_{2(g)} 2CO_{2(g)}; H 787 kJ$  ....(1)

$$H_{2(g)} \stackrel{1}{2}O_{2(g)} H_{2O_{()}}; H_{286 kJ}$$
 ...(2)

$$C2H_{2(g)} = 2\frac{1}{2}O_{2(g)}$$

2CO<sub>2(g)</sub> H2O<sub>()</sub>;

2HI 0

2x

x)

Add eq.(1) and (2)

$$2C_{(s)} H_{2(g)} 2 \frac{1}{2} O_{2(g)} 2CO_{2(g)}$$

 $H_2 O_{()}$ ; H 1073 kJ .......(4) Subtract eq. (3) form eq. (4) we get

$$2C_{(s)} H_{2(g)} C2H_{2(g)};$$

H 237kJ

67. (b) Endothermic reactions are favoured at high temperature. Therefore, increasing the temperature will shift equilibrium to the right.

68. (a) 
$$\ln \frac{k_2}{k_1} = \frac{E_a}{2.303R} \frac{1}{T_1} = \frac{1}{T_2}$$

69.

$$K c = \frac{[HI]^2}{[H_2][I_2]} \quad \frac{(2x)^2}{(1_x)^2}$$
  
Given x = 80% = 0.80  
$$K c = \frac{(2_1 - 0.80)^2}{(1_1 - 0.80)^2} \quad 64$$

70. (d) The equilibrium constant K p will change with temperature for the reaction

 $H_2(g) + I_2(g) = 2HI(g).$ 

Catalyst does not alter the state of equilibrium. Equilibrium constant depends only upon temperature. The relation of k with temp can be shown as

$$\log \frac{k_2}{k_1} = \frac{H}{2.303R} \frac{1}{T_1} - \frac{1}{12}$$

71. (d) Eq. mass of Ca<sup>++</sup> =  $\frac{\text{Mol.mass}}{2}$   $\frac{40}{2}$  20

$$Z = \frac{\text{Eq.mass of water}}{96500} \frac{20}{96500}$$
  
Given w = 60 g, i = 5 amp.  
w = zit

or 
$$60 = \frac{20}{96500} 5 \text{ t}$$

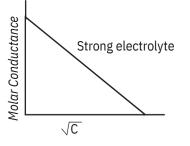
$$t = \frac{96500 \ 60}{20 \ 5}$$
 57900 sec = 16 h.

72. (b) According to Debye - Huckel - Onsagar

equation m  ${}^{\circ}m$  –A B  ${}^{\circ}m$   $\sqrt{C}$ 

where A and B are the Debye – Huckel constants. If we plot a graph between molar conductance <sub>m</sub> against the square

roots of the concentration  $\sqrt{-C}$  a straight line is obtained



73. (c) Molar conductance of  $CaCl_2$ = Molar conductance of  $Ca2+++2 \times (molar conductance of Cl-)$ = 118.88 × 10-4 + 2 (77.33 × 10-4) = 273.54 × 10-4 m2 mho mol-1

- 74. (a) Lower the value of reduction potential, greater will be the reducing power of element. Since Zn has lowest reduction potention hence Zn is the strongest reducing agent. The epoxide ring consists
   75. (a) of three membered ring with two carbon
- 75. (a) of three membered ring with two carbon atoms and one oxygen.

76. (c) Grignard reagent is a sigma bonded organometallic compound in which Mg is bonded with one alkyl and one halogen group. This can be prepared as

77. (a,c)Presence of electron attracting group like – NO 2, – Cl increases the acidity of phenol as it enables the ring to draw more electrons from the phenoxy oxygen and thus releasing easily the proton. Presence of

> **Blea**tron releasing group e.g. – OCH benzene sing decreases the acidity of phenol as it strengthens the negative charge on phenoxy oxygen and thus proton release becomes difficult.

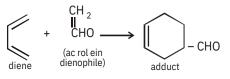
Further phenols are much more acidic than alcohols. The acidic nature of phenol is due to the formation of stable phenoxide ion in solution.

No resonance is possible in alkoxide ions (RO–) derived from alcohols. The negative charge is localized on oxygen atom. Thus alcohols are not acidic. Aldol 78. (b) condensation is given by aldehydes

which have -H atoms. So acetaldehyde gives this reaction.

O    (CH3)3C C H Trimethyl acetaldehyde	O    CH3 C H a cet aldeh yde
O	O
C6H5 C H	H C H
benzaldehyde for	maldehyde

80. (b) It is cycloaddition reaction between a conjugated diene and subsituted alkenseatorrated carboxyl compound.



#### **PART - III (MATHEMATICS)**

81. (c) Sinceaandbare coplanar, therefore a×b is a vector perpendicular to the plane containing aandb. Similarlyc×d is a vector perpendicular to the plane containing candd. Thus, the two planes will be parallel if their normals i.e. a×b and  $c \times d$  are parallel.

Area of a parallelogram  $=\frac{1}{2}|d1 d_2|$ 

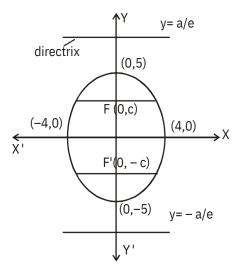
Now, d1×d 2 
$$\begin{vmatrix} \hat{i} & \hat{j} & k \\ 3 & 1 & 2 \\ 1 & 3 & 4 \end{vmatrix}$$
  
= i^(4 6)  $\hat{j}(12 2) k^{(9} 1)$   
d1 × d2 = 2i^14j^10k^  
 $|d_1 d2| = \sqrt{(2)2(14)2(10)2}$   
=  $\sqrt{4}$  196 100  $\sqrt{300}$  2 $\sqrt{75}$   
Area of parallelogram =  $\frac{1}{2} |d_1 d_2|$   
=  $- \times 2 \sqrt{75} = \sqrt{75}$  square units

83. (d) Given: 
$$\cos x + \cos 2x = 1$$
  
 $\cos x = 1 - \cos 2x$   $\cos x = \sin 2x$   
 $\cos 2x = \sin 4x$   $1 - \sin 2x = \sin 4x$   
 $\sin 4x + \sin 2x = 1$   
cubic both sides, we have  
 $\sin 12x + \sin 6x + 3 \sin 6x (\sin 4x + \sin 2x) = 1$   
 $\sin 12x + \sin 6x + 3 \sin 10x + 3 \sin 8x = 1$   
 $\sin 12x + 3\sin 10x + 3 \sin 8x + \sin 6x - 1 = 0$   
84. (c)  $(\cos + i \sin - 3)^{5} = (\cos 3 + i \sin 3 - 1)^{5}$   
 $= (\cos (2k + 3 - ) + i \sin (2k + 3 - ))^{1/5}$   
 $= \cos \frac{2k}{5} - i \sin \frac{2k}{5} - \cos \frac{2}{5} - \frac{3}{5}$   
 $\sin \frac{2k}{5} - \sin \frac{3}{5} - \cos \frac{2}{5} - \frac{3}{5}$   
 $\sin \frac{2}{5} - \sin \frac{3}{5} - \cos \frac{2}{5} - \frac{3}{5}$   
 $\sin \frac{2}{5} - \cos \frac{4}{5} - \sin \frac{6}{5} - \frac{3}{5}$   
 $= \cos \frac{3}{5} - \frac{2}{5} - \frac{3}{5} - \frac{4}{5} - \frac{3}{5} - \frac{3}{5}$   
 $= \cos \frac{3}{5} - \frac{2}{5} - \frac{3}{5} - \frac{4}{5} - \frac{3}{5} - \frac{3}{5}$   
 $= \cos \frac{3}{5} - \frac{2}{5} - \frac{3}{5} - \frac{4}{5} - \frac{3}{5} - \frac{3}{5}$   
 $= \cos \frac{5}{2} - 2 \cdot \frac{3}{5} - 5 - 1 \cdot \frac{2}{5}$   
 $= \cos \frac{5}{2} \cdot \frac{6}{5} - \frac{8}{5}$ 

$$isin \quad \frac{5}{2} \quad \frac{6}{5} \quad \frac{8}{5}$$
  
= cos (3 + 4) + i sin(3 + 4)  
= cos (4 + 3) + i sin (4 + 3)  
= cos 3 + i sin 3

5

85. (d) 
$$\frac{1}{i} \frac{i}{2i}^{2} \frac{1}{1} \frac{1}{2i^{2}} \frac{2i}{2i^{2}} \frac{2i}{i}$$
  
 $\frac{1}{2} \frac{1}{2i} \frac{2i}{2i} \frac{2i}{2i} \frac{2i}{2i} \frac{4i}{4i^{2}} \frac{4i}{2i^{2}}$   
 $\begin{bmatrix} i^{2} = -1 \end{bmatrix}$   
 $\frac{4i}{4} \frac{2}{1} \frac{2}{5} \frac{4i}{5} \frac{2}{5} \frac{5}{5}$   
The imaginary part =  $-\frac{4}{5}$   
86. (a) Given sin-1x + sin-1y =  $\frac{2}{2}$  (i)  
we know that sin-1x + cos-1x =  $\frac{2}{2}$   
sin-1x =  $/2 - \cos - 1x$   
Equation (1) becomes.  
 $\frac{1}{2} - \cos - 1x + \frac{1}{2} - \cos - 1y = \frac{1}{2}$   
cos<sup>-1</sup>x + cos<sup>-1</sup>y =  $\frac{1}{2}$   
87. (c) Equation of ellipse  $\frac{x^{2}}{b^{2}} \frac{y^{2}}{a^{2}} 1$ , where  
 $a > b$ .  
Given,  $\frac{x^{2}}{16} \frac{y^{2}}{75} 1$   $b = 4, a = 5$   
But  $e = \sqrt{1} \frac{b^{2}}{a^{2}} \sqrt{1} \frac{1}{6}$   
 $e = \frac{3}{5}$   
equation of directrix  $y = \frac{a}{e}$   
 $y = -\frac{375}{5} 3y = \pm 25$ 



88. (a) Since the normal at (ap2, 2ap) on y2 = 4ax meets the curve again at (aq2, 2aq), therefore px + y = 2ap + ap3 passes thrpugb (aQ2q2aQap + ap3 p(q2-p2) = 2(p-q)p(q+p) = -2p2 + pq + 2 = 089. (d) Given : equation of line, x-3y=1 (1)

9. (d) Given : equation of line, x-3y=1 (1)  
and hyperbola x2 - 4y2 = 1 (2)  
putting x = 1 + 3y in equation (2), we get  
$$(1 + 3y)2 - 4y2 = 1$$
 1+ 9y2 + 6y - 4y2 = 1  
 $5y2 + 6y = 0$  y(5y + 6) = 0  
 $y = 0 \text{ or } y = \frac{6}{5}$   
 $x = 1 \text{ for } y = 0 \text{ & } x = 1$   $\frac{18}{5} = \frac{13}{5}$   
for y = -6/5  
the line (1) cuts the hyperbola (2) in at  
most two point.

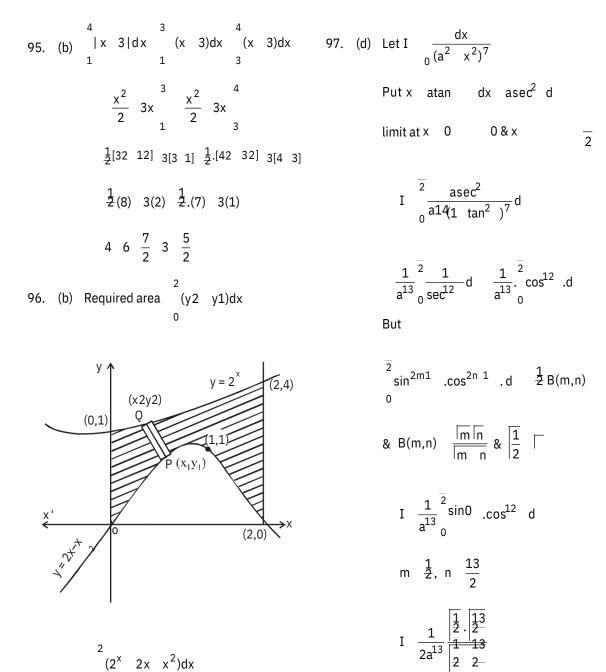
co-ordinates of points are P(1,0) &

Q 
$$\frac{13}{5}, \frac{6}{5}$$
  
PQ =  $\sqrt{1 \frac{13}{5}^2 0 \frac{6}{5}^2}$ 

$$\sqrt{\frac{18}{5}}^{2} \frac{3}{6}}{\sqrt{\frac{324}{25}}} \sqrt{\frac{360}{25}}$$
length of straight line PQ =  $\frac{6\sqrt{10}}{5}$  units.  
90. (c) Given x = t2 + 2t-1 & y = 3t + 5  
x = t2 + 2t + 1-2 & y = 3t + 3+2  
x = (t+1)2 - 2 & y = 3(t+1) + 2 (2)  
(t+1) =  $\sqrt{x}$  2 .....(1)  
Equation (2) becomes [using equation (1)]  
y =  $3\sqrt{x}$  2 2  
y-2 =  $3\sqrt{x}$  2  
squaring both sides, we get  
(y-2)2 = 9 (x + 2)  
Y 2 = 9X where Y = y - 2 & X = x + 2  
This equation represents a parabola  
91. (c) Slope of the normal at (3,4) is the value of  
 $\frac{1}{f'(x)}$  at x = 3 or  $\frac{1}{f'(3)}$  = tan  $\frac{3}{4}$  = -1  
f''(3) = 1  
92. (c) Given : f(x) = x2 e-2x, x > 0  
f'(x) = x2.e-2x(-2) + e-2x.2x  
put f'(x) = 0 2e-2x. x (-x + 1) = 0  
x = 1 or x = 0  
f''(x) = (-4x2 - 6x + 1)e-2x  
f''(1) = -9e-2x < 0  
f''(0) = e-2x > 0  
value of f(x) is maximum at x = 1  
f(x) = x2.e-2x f(1) = e-2 =  $\frac{1}{e2}$   
93. (d) Given : (x + y) sin U = x2y2  
sinU =  $\frac{x2y2}{x y}$  = v (let)  
Here n = 2 - 1 = 1  
Euler's theorem<sup>x</sup>.  $-\frac{v}{x}$  y.  $-\frac{v}{y}$  nv  
 $x \cdot \frac{\sin U}{x}$  y.  $-\frac{v}{y}$  sinU  
x.cosU  $\frac{U}{x}$  y.cosU.  $-\frac{U}{y}$  sinU

$$\begin{array}{ccc} x & U & U & \sin U \\ x & x & y & y & \cosh U \\ U & U & & \\ x & -x & y & -y & \tan U \end{array}$$

94. (c) Equation of the given curve in parametric for m, x = t2 + 1 and y = t2 - t - 6Y-coordinate of the point, where the given curve meets X-axis is 0. When y = 0, then t2 - t - 6 = 0t<sup>2</sup> 3t 2t 6 0 t(t 3) 2(t 3) 0 (t 3)(t 2) 0 t 3 or 2 when t = 3, then x = 10when t = -2, then x = 5Hence, the points where the curve meets the X-axis are (10, 0) and (5, 0). dy Now,  $\frac{dy}{dx} = \frac{dt}{dx}$ 2t 1 2t dt Slope of the tangent at point (10, 0)  $\frac{dy}{dx} \underset{x \ 10}{} \frac{dy}{dx} \underset{t \ 3}{} \frac{5}{6}$ m1 Slope of the tangent at point (5, 0),  $\frac{dy}{dx} \underset{x \ 5}{\overset{5}{\overset{}}} \frac{dy}{dx} \underset{t \ 2}{\overset{2}{\overset{}}} \frac{5}{4} \frac{5}{4}$  $m_2$ If be the angle beween two tangents, then 55  $\begin{array}{r}
 \frac{3}{4} \quad \stackrel{\circ}{\underline{6}} \\
 \frac{1}{5} \quad \stackrel{\circ}{\underline{5}} \\
 1 \quad \stackrel{\circ}{\underline{6}} \quad \stackrel{\circ}{\underline{4}}
\end{array}$ m2 m1 1 m1m2 tan 15 10 5 <u>12</u> 49 10 12 49 24 25 24 24 10 tan 49  $\tan \frac{1}{49}$   $\tan \frac{1}{0}$   $\tan \frac{1}{0}$ 4 9



 $\frac{231}{2048} \cdot \frac{1}{a13}$ 

 $\frac{1}{2a^{13}}.\frac{\lceil .\frac{11}{2}, \frac{9}{2}, \frac{7}{2}, \frac{5}{2}, \frac{3}{2}, \frac{1}{2}.\rceil}{6.5.4.3.2.1}$ 

98. (c) Let I 
$$ex \frac{(1 x)^{2}}{(1 x2)2} dx$$
I 
$$ex \frac{1 x^{2} 2x}{(1 x2)2} dx$$

$$e^{x} \frac{1 x}{(1 x^{2})^{2}} \frac{2x}{(1 x^{2})^{2}} dx$$
I 
$$e^{x} \frac{1 x}{(1 x^{2})^{2}} \frac{2x}{(1 x^{2})^{2}} dx$$
I 
$$e^{x} \frac{1}{(1 x^{2})} dx = 2 ex \cdot \frac{x}{(1 x^{2})^{2}} dx$$
I 
$$\frac{1}{(1 x^{2})} e e^{x} \cdot (1 x^{2}) = 2x dx$$

$$2 \frac{e^{x} x}{(1 x^{2})^{2}} dx$$
I 
$$\frac{e^{x}}{1 x^{2}} = 2 \frac{exx}{(1 x^{2})^{2}} dx$$
I 
$$\frac{e^{x}}{1 x^{2}} = 2 \frac{e^{x} x}{(1 x^{2})^{2}} dx$$
I 
$$\frac{e^{x}}{(1 x^{2})^{2}} dx$$
I 
$$\frac{e^{x}}{1 x^{2}} = 2 \frac{e^{x} x}{(1 x^{2})^{2}} dx$$
I 
$$\frac{e^{x}}{(1 x^{2})^{2}} dx$$
I 
$$\frac{e^{x}}{1 x^{2}} = 2 \frac{e^{x} x}{(1 x^{2})^{2}} dx$$
I 
$$\frac{e^{x}}{(1 x^{2})^{2}} dx$$
I 
$$\frac{e^{x}}{$$

99. (c) Given: xsin  $\frac{y}{x}$  dy ysin  $\frac{y}{x}$  x dx

$$\frac{dy}{dx} \quad \frac{y\sin \frac{y}{x} x}{x\sin \frac{y}{x}}$$
Put  $\frac{y}{x}$  z  $\frac{dy}{dx}$  z.1 x. $\frac{dz}{dx}$ 
x. $\frac{dz}{dx}$  z  $\frac{zx\sin z}{x\sin z}$  z cosec z
x  $\frac{dz}{dx}$  cosec z sinz dz  $\frac{dx}{x}$ 
cosz logx c
cos  $\frac{y}{x}$  logx c
But y(1)  $\frac{z}{2}$  x 1,y  $\frac{z}{2}$ 

$$cos \frac{y}{2} \quad log(1) \quad c \quad c \quad 0$$
$$cos \quad \frac{y}{x} \quad logx$$

100. (c) The equation of the family of circles of radius r is (x - a)2 + (y - b)2 = r2 ...(1) Where a & b are arbitrary constants. Since equation (1) contains two arbitrary constants, we differentiate it two times w.r.t x & the differential equation will be of second order. Differentiating (1) w.r.t. x, we get

 $2(x a) 2(y b) \frac{dy}{dx} 0$ 

$$(x a) (y b) \frac{dy}{dx} 0 ...(2)$$

Differentiating (2) w.r.t. x, we get

1 (y b) 
$$\frac{d^2y}{dx^2}$$
  $\frac{dy}{dx}^2$  0 ...(3)

$$\begin{array}{c} 1 \quad \frac{dy}{dx} \\ (y \quad b) \quad \frac{d^2y}{dx^2} \\ \frac{dx^2}{dx^2} \end{array} \qquad ...(4)$$

On putting the value of (y - b) in equation (2), we get

x a 
$$\frac{1 \quad \frac{dy}{dx}^2 \quad \frac{dy}{dx}}{\frac{d^2 \chi}{2}} \qquad \dots (5)$$

Substituting the values of (x - a) & (x - b) in (1), we get

$$\frac{1 \left(\frac{dy}{dx}\right)^{2} \left(\frac{dy}{dx}\right)^{2}}{\left(\frac{d^{2}y}{dx^{2}}\right)^{2}} \frac{1 \left(\frac{dy}{dx}\right)^{2}}{\left(\frac{d^{2}y}{dx^{2}}\right)^{2}} r^{2}}$$

$$\frac{1 \left(\frac{dy}{dx}\right)^{2} \left(\frac{d^{2}y}{dx^{2}}\right)^{2}}{1 \left(\frac{dy}{dx}\right)^{2} r^{2}} r^{2} \left(\frac{d^{2}y}{2}\right)^{2}}$$

101. (c) Given: 
$$\frac{d2}{y}$$
  $2\frac{dy}{dx}$   $y$   $2e3x$   
The auxflixity equation is  
 $D2 + 2D2 + 1 = 0 \text{ or } m2 + 2m + 1 = 0$   
(m 1)(m 1) 0 m 1, 1  
i.e., repeated roots  
Complementary function = ( $q + c_x$ )e-x  
Now Particular Integral (P.I.)  
 $\frac{1}{D2} \frac{1}{2D} \frac{1}{2.2} e^{3x}$  [D = 3]  
P.I.  $\frac{1}{3^2} \frac{1}{2.3} \frac{1}{1} \cdot 2e^{3x}$   $\frac{2e^{3x}}{16} \frac{e^{3x}}{8}$   
Solution  $y = C. F. + P. I.$   
 $y = c_1 - c2x e^{-x} - \frac{e^{3x}}{8}$   
102. (c) Given  $ydx + (x - y3) dy = 0$   
 $y\frac{dx}{dy} - x - y^3 - 0$   $\frac{dx}{dy} - \frac{1}{y}x - y^2$   
compare this equation to general equation  
i.e.  $\frac{dx}{dy} - Px - Q = P - \frac{1}{y}, Q - y^2$   
I.f.  $e^{-Pdy} - e^{-\frac{1}{y}\frac{dy}{dy}} e^{-\log y} - y$   
 $x \times I.f. - Q I.f. dy - C_1$   
 $x.y - y2.y dy C_1 - xy - \frac{y4}{4} - C_1$   
 $\frac{4xy}{4} \frac{4xy}{4xy} - 4C_1$   
 $y - 4C_1 - y^4 - 4xy C,$   
where  $C = -4C_1$   
103. (b) Given,  $x + x^2x^3x^4x^5 - 1050$   
 $x + x^2x_5x^4x^5 - 2 - 3 - 5^2 - 7$ 

Each of 2, 3 or 7 can take 5 places and 52 can be disposed in 15 ways. Hence, number of positive integral solution =  $53 \times 15 = 1875$ 

104. (d) Number of onto functions: If A & B are two sets having m & n elements such that 1 n m then number of onto functions from A to B is

$$\begin{array}{c} & -1 & {}^{n} & {}^{n}C_{r}r^{n} \\ \text{Given A} = \{1, 2, 3, - - - n\} \& B = \{a, b, c\} \\ \text{Number of onto functions} \\ & {}^{3} & -1 & {}^{3-r} \cdot 3C_{r} & r^{n} \\ r^{1} \\ & 1 & {}^{3-1} & 3C_{1} & 1^{n} & -1 & {}^{3-2} & 3C_{2} & 2^{n} \\ & {}^{3}C_{3} & 3^{n} & -1 & {}^{3-3} \\ & {}^{3}C_{1} & {}^{3}C22^{n} & {}^{3}C33^{n} \\ & \frac{3!}{2!1!} & \frac{3!}{2!1!} & 2^{n} & \frac{3!}{3!0!} & 3^{n} \\ & 3 & 3 \cdot 2 & 3^{n} \\ & 3^{n} & 32n & 1 \end{array}$$

105. (b) Let there are n persons in the room. The total number of hand shakes is same as the number of ways of selecting 2 out of n.

$${}^{n}C_{2} \quad 66 \quad \frac{n n 1}{2!} \quad 66$$
  
 $n^{2} \quad n \quad 132 \quad 0$   
 $n \quad 12 \quad n \quad 11 \quad 0 \quad n \quad 12$ 

106. (a)We know that, let (G, 0) be a group & e be the identity then

(a \* a)-1 = a-1 o a-1
= (a-1)-1 = a.

107. (d) No. of tickets = 9

No. of odd numbered tickets = 5
No. of even numbered tickets = 4
Required probability = P {odd, even, odd}
+ P (even, odd, even)

$${}^{8} \frac{{}_{9}^{5}C_{1}}{C_{1}} \frac{C_{1}}{C_{1}} \frac{{}^{4}C_{1}}{\Gamma} \frac{{}_{9}^{4}C_{1}}{C_{1}} \frac{{}_{9}^{5}C_{1}}{\Gamma} \frac{{}_{7}^{5}C_{1}}{C_{1}}$$
$$\frac{5}{9} \frac{4}{8} \frac{4}{7} \frac{4}{9} \frac{5}{8} \frac{3}{7} \frac{5}{18}$$

108. (a) Given A 1  $\frac{1}{\sec 2}$   $\frac{1}{\tan 1}$   $\frac{1}{1}$   $\frac{1}{\tan 1}$ PA  $\frac{1}{12}$ , P B  $\frac{5}{12}$ , P B/A  $\frac{1}{15}$ 1  $B = \frac{1}{\sec^2} \cdot \frac{10}{01} \cdot \frac{1}{\tan} = 1$ We know that  $PB/A = \frac{PAB}{PA}$  $B \quad \frac{1}{\sec 2} \quad \frac{1}{\tan 1} \quad \tan 1$  $\frac{1}{15} \quad \frac{P \quad A \quad B}{1/12}$ PAB $\frac{1}{15 \ 12} \ \frac{1}{180}$  $B = \frac{1}{\sec^2}$ . A But. sec2 .B A PABPAPBPAB PAB $\frac{1}{12}$  $\frac{5}{12}$  $\frac{1}{180}$  $\frac{89}{180}$ cos2 <sup>1</sup>.B A 112. (b) Given: 2x 1 4 8 2 2x 2 0 7 6 2x 109. (a)  $\frac{2}{1.5}$  f x dx, where  $\frac{f}{x} = \frac{x}{2}$  $\frac{2}{1.5} \frac{x}{2} dx = \frac{1}{2} \cdot \frac{2}{1.5} x dx = \frac{1}{2} \cdot \frac{x^2}{2} \frac{2}{1.5} x dx = \frac{1}{2} \cdot \frac{x^2}{2} \frac{1}{1.5} x dx = \frac{1}{2} \cdot \frac{1}{2} \cdot$ 2x 1 4x2 12 44x 14  $\frac{1}{4}$  4 2.25  $\frac{1}{4}$  1.75  $\frac{17}{5}$   $\frac{7}{16}$ 81214x 110. (b) If 2 P(X = 0) + P(X = 2) = 24P(X = 1)16x  $8x^3$  24x  $4x^2$  12 Let probability distribution of X be given by 56 96 112x P(X = r)  $\frac{r m}{mre}$  where r = 0, 1, 2, ....  $8x^3$   $4x^2$  152x 140 0 (x + 5) is a factor of above equation  $2 \frac{m0e^{m}}{n!} \frac{m2.e^{m}}{2!} 2 \frac{m.e^{m}}{1!}$  $8x^3$   $40x^2$   $36x^2$  180x28x 140 0 8x2 x 5 36x x 5 28x  $2 \frac{m^2}{2} 2m m^2 4m 4 0$ x 5 8x2 36x 28  $m 2^2 0 m 2$ x 5 4 2x2 9x 7 111. (c) A 1 tan tan 1 &AB I 4 x 5 2 x 2 7 x 2 x 7 0 B IA  $^{1}$ , A<sub>11</sub> 1, A<sub>12</sub> tan , 4 x 5 x 2x 7 12x 7  $A_{21}$  tan  $A_{22}$  1 4 x 5 2x 7 x 1 0 
 |A|
 1
 tan
 1
 tan2
 sec2
 x 5, 3.5,1

0

0

5 0

0

0

0

113. (b) For only one solution |A| 0 k 2 1 0 k 1 2 0 0 k 2 k k 1 k 2 0 k 0,k 1,k 2. k 1 114. (c) Let A 2 5 1 2 5 A 2 4 a 4 0 0 a 6 1 2 a 1 0 0 a 6  $R_2 R_2 2R_1 R_3 R_3 R_1$ clearly rank of A is 1 if a = -6115. (c) Given :  $ax^4 bx^2 c 0$ Equation will be real if D 0  $b^2$  4ac 0  $b^2$  4ac 116. (a) Given :  $\log_3 x \log_3 \sqrt{x} \log_3 \sqrt[4]{x}$  $\log_3 \sqrt[8]{x} \log_3 \sqrt[16]{x} 4$  $\log_{3} x^{1 \frac{1}{2} \frac{1}{4} \frac{1}{8} \frac{1}{1} \frac{1}{6}} 4$  $\log_{3} \frac{1}{x^{1}} \frac{1}{2} 4 \qquad S \qquad \frac{1}{1 r} \log_{2} 4 \qquad x^{2} \qquad 3^{4} \qquad x \qquad 9$ 117. (a)  $x \frac{1}{x}^{3} x \frac{1}{x} 0$  $x \frac{1}{x} x \frac{1}{x^2} = x \frac{1}{x^2} x^2 = 1 = 0$  $x \frac{1}{x} 0 x^2 1 0 x i$ 

Thus, the given equation has no real roots.

118. (a) Given : H is the harmonic mean between P & Q H  $\frac{2PQ}{P O}$   $\frac{1}{H}$   $\frac{P Q}{2PO}$  $\frac{2}{H} \frac{1}{Q} \frac{1}{P} \frac{1}{P} \frac{H}{P} \frac{H}{Q} 2$ 119. (c)We have a b a b a a b b a b a.b a a.a b b.b a b.a b a.b a b a b b.b  $b^2$  1.a.a  $a^2$  1 a.b 1 a b x a b where x a.b 1 is a scalar The given vector is parallel to a b. 120. (a) Given : A, B & C are three points with coordinates (1, 2, -1), (2, 0, 3) & (3, -1, 2) respectively. Now, direction ratio's of AB = 2 - 1, 0 - 2, 3 + 1 = 1, - 2, 4 & direction ratio's of AC = 3 - 1, -1 - 2, 2 + 1 = 2, -3, 3we know that  $\frac{a_{1}a_{2}b_{1}b_{2}cq_{2}}{\sqrt{a1^{2}b_{1}^{2}c_{1}^{2}}\sqrt{a_{2}^{2}b^{2}c2^{2}}}$ cos  $\cos \quad \frac{1 \ 2 \ 2 \ 3 \ 4 \ 3}{\sqrt{1 \ 4 \ 16} \ \sqrt{4 \ 9 \ 9}}$  $\frac{2}{\sqrt{2}} \frac{6}{\sqrt{22}} \frac{12}{\sqrt{462}}$  $\sqrt{462} \cos \theta$ 20