VITEEE 2006 Question Paper Vellore Institute of Technology Engineering Entrance Examination

SOLVED PAPER

2006

PART - I (PHYSICS)

A potential difference of 300 V is applied to a combination of 2.0µF and 8.0 µF capacitors connected in series. The charge on the 2.0µF capacitor is

 $2.4 \times 10 - 4C$

(b) $4.8 \times 10-4C$

 $7.2 \times 10 - 4 C$

 $(d)9.6 \times 10-4 C$

T(cw)o point charges 4C and - 2C are separated by a distance of 1 m in air. Then the distance of the point on the line joining the charges, where the resultant electric field is zero, js (in metre)

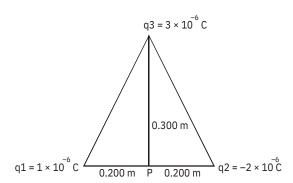
(b) 0.75

(c) 0.67

(d) 0.81

Figure shows a triangular array of three point charges. The electric potential V of these source charges at the midpoint P of the base of the triangle is

9 109Nm2C 2



55k (a

(b) 45k

V

(c) 63k 49k

(d) V

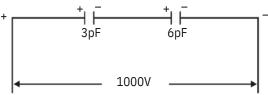
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A current of 5A is passing through a metallic wire of cross-sectional area $4 \times 10-6$ m2. If the density of the charge carriers in the wire is $5 \times 1026m-3$, the drift speed of the electrons will be $[e = 1.602 \times 10-19C]$ (a)

1.56×10-2ms-1 (c) (b2) .14.29×81×01-02-

m2ms-s1-1 The

5. series combination of(dt)w 20.8 c4a \times p1a0c-it2omrss-s1hown in figure is connected across 1000V. The magnitude of the charges on the capacitors



 $3 \times 10 - 9 C$ $2.5 \times 10 - 9 C$

(b) $2 \times 10 - 9 \text{ C}$ (d) $3.5 \times 10 - 9 \text{ C}$

- T(achr)eree resistances of values 2ald 6 to be connected to produce an effective resistance of 4 . This can be done by connecting
 - (a) 6 resistance in series with the parallel combination of 2 and 3 resistance in a series WI
 - resistance in series with the parallel
 - (c) combination of 2 and 6
 - (d) 2 resistance in series with the parallel combination of 3 and 6
 - 2 resistance in parallel with the parallel combination of 3 and 6
- The resistance of a field coil measures 50 at 70°C. The temperature 20°C and 65 coefficient of resistance is

(a) 0.0086/°C

(b) 0.0068/°C

(c) 0.0096/°C

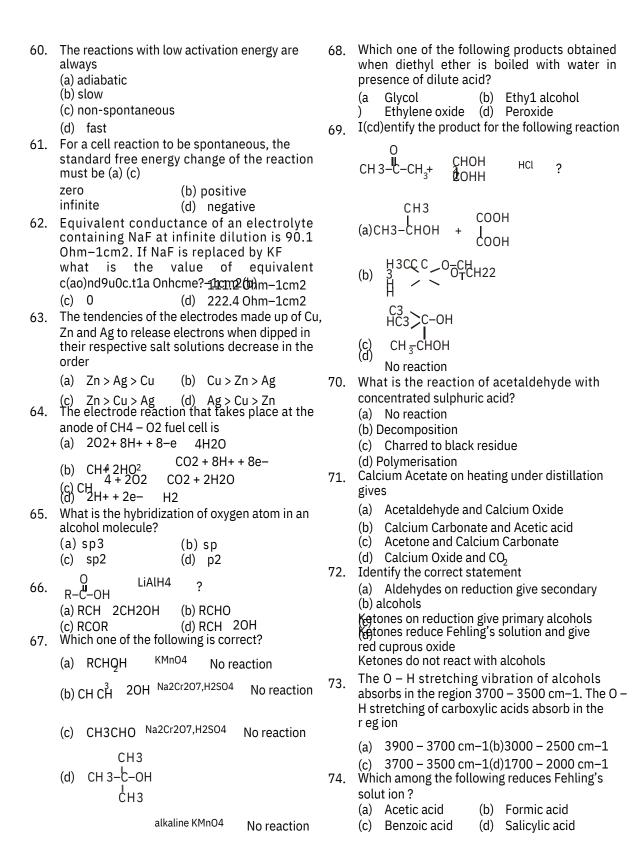
(d) 0.0999/°C

- The electrolyte used in Lechlanche cell is
 - copper sulphate solution
 - ammonium chloride solution (b)
 - (c) dilute sulphuric acid
 - (d) zinc sulphate

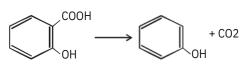
9.	A galvanometer has a resistance of 50 . If a resistance of 1 is connected across its terminals, the total current flow through the ga rlevparneosmenetse rt hise [mIaximum current that can be passed through the galvanometer]	17.	Our eyes respond to wavelengths ranging from (a) (b400) nm to 700 (d) nm 700 nm to 800 nm 0 to to +
	(a 42 g (bd))535IgIg1	18.	A new system of units is evolved in which the values of 0 and 0are 2 and 8 respectively. Then
10.) I I(cn) a 4t6angent galvanometer, a current of 1A produIces a deflection of 30°. The current required to produce a deflection of 60° is (a) 3A (b) 2A (c) 4A (d) 1A	19.	the speed of light in this system will be (a) 0.25 (b) 0.5 (c) 0.75 (d) 1 A ray of light strikes a piece of glass at an angle of incidence of 60° and the reflected beam is
11.	In the presence of magnetic field 'B' and electric field 'E', the total force on a moving		completely plane polarised. The refractive index of glass is
	charged particle is		(a) $2\sqrt{3}$ (b) $\sqrt{3}$
	(a) F v[(q B) E]		3 1
	(b) F q[(v E) B]		(c) $\frac{\sqrt[3]{2}}{2}$ (d) $\frac{1}{2}$
	(c) F q[(v B) E]	20.	In an experiment on Newton's rings, the diameter of the 20th dark ring was found to be 5.82mm and
	(d) F B[(q E) v]		that of the 10th ring 3.36 mm. If the radius of the
12.	A circular coil of radius 40 mm consists of 250 turns of wire in which the current is 20mA. The		plano-convex lens is 1 m, the wavelength of light used is
	magnetic field in the center of the coil is [= $4 \times$		(a) 5646 A° (b) 5896 A°
	10-7 Hm-1]	- 4	(c) 5406 A° (d) 5900 A°
	(a 0.785 (b) 0.525) G (d) G	21.	What is the angular momentum of an electron in the fourth orbit of Bohr's model of hydrogen
13.	(RcM)S Ova.6lu2e9 of AC isO o.9f OthOe (a) 7%G (b) 7.G7%	peak	
	(c) 70% (d) 70.7%		(a) h (b) 2h
14.	Q-factor can be increased by having a coil of		(a) $\frac{1}{2}$ (b) $\frac{1}{2}$
	 (a) large inductance, small ohmic resistance (b) large inductance, large ohmic resistance (c) small inductance, large ohmic resistance 		(c) h (d) $\frac{h}{4}$
	(d) small inductance, small ohmic resistance	22.	The transition of an electrom from 2 n = 5,6,
15.	A small piece of metal wire is dragged across the gap between the pole pieces of a magnet in 0.5	!	to n1 = 4 gives rise to
	second. The magnetic flux between the pole		(a) Pfund series(b) Lyman series(c) Paschen series(d) Brackett series
	pieces is known to be $8 \times 10-4$ Wb. The emf induced in the wire is	23.	The ground state energy of hydrogen atom is –
	(a) 16 m V (b) 1.6 V		13.6 eV. What is the potential energy of the electron in this state?
16.	(c) 1.6 m V (d) 16V Current in the LCR circuit becomes extremely		(a -27.2 (b) -13.6 eV
10.	large when	2.4) eV (d) 0 eV
	(a) frequency of AC supply is increased(b) frequency of AC supply is decreased	24.	T(ch)e l+on1g3e.6st wavelength that can be analysed by a seoVdium chloride crystal of spacing $d = 2.82$
	(c) inductive reactance becomes equal to		A° in the second order is
	(d) capacitive reactance inductance becomes equal to capacitance		(a 2.82 (b) 5.64 A°) A° (d) 11.28 A°
			(c) 8.46
			A°

25. 26.	Which is the incorrect st following? P(ah)oton is a particle with P(bh)oton is a particle with P(ch)otons travel with velocyacuum P(dh)otons even feel the puthe deBroglie wavelength a steel ball of mass 1000 gm 1 ms-1 is [h = 6.626 × 10-	zero rest mass zero momentum city of light in ull of gravity associated with a moving at a speed of	33.34.	When the conductivity of a semiconductor is only due to the breaking up of the covalent bonds, the semiconductor is known as (a) donor (b) extrinsic (c) intrinsic (d) acceptor In a P-type semiconductor, the acceptor impurity produces an energy level (a) just below the valence band (b) just above the conduction band (c) just below the conduction band
	(a 6.626 × 10- (b)	6.626 × 10−37m		(d) just above the valence band
27.) 31m 6.626 × (d)	6.626 × 1034m		(a)s an amplifier with proper negative feedback (c) network circuits
		\[\frac{1}{2} \pi = \frac{1}{2} \]		(d) converts alternating current into direct cur r en t
		$v \sqrt{\frac{3}{2}}$ 4c		an amplifier with no feedback network an amplifier with proper positive feedback network circuits
	(c) $v = \sqrt{\frac{3}{2}}c$ (d)	v = 2c	36.	Which of the following gates can perform perfect
28. 29.	(c) 15 × 1016 J (d) The difference between th nucleus and the sum of nucleons composing a nucl (a) packing fraction(b) (c) binding energy (d) The half life period of Radio	d into energy? 11 × 1016 J 18 × 1016 J e rest mass of the the masses of the eus is known as mass defect isotopic mass	37. 38.	binary addition? (a) AND gate (b) OR gate (c) EXOR gate (d) NAND gate The frequency of an FM transmitter without signal input is called (a) the centre frequency (b) modulation factor (c) the frequency deviation (d) the carrier swing The fundamental radio antenna is a metal rod which has a length equal to (a) in free space at the frequency of operation
	mean life time is	3		(b) in free space at the frequency of
	(a) 1.5 minute (b)	0.6931 minute		operation
31.	'Pair production' involves ophoton into			(c) in free space at the frequency of operation
	(a) a neutron-electron pa(b) a positron-neutron pa(c) an electron-proton pa(d) an electron-positron pa	ir ir	20	(d) $\frac{3}{4}$ in free space at the frequency of operation
32.		roton and neutron fall hotons baryons	39.	Vidicon works on the principle of (a) electrical conductivity (b) photoconductivity (c) thermal conductivity (d) SONAR

40.	The maximum range, dmax, of radar is (a) proportional to the cube root of the peak (b) transmitted power	49.	centered cubic unit cell? (a) 1 (b) 2
	proportional to the fourth root of the pook		(c) 4 (d) 3
	(c) proportional to the fourth foot of the peak transmitted power	50.	Schottky defect in solids is due to
	(d) proportional to the square root of the peak		(a) a pair of cation and anion vacancies (b) occupation of interstitial site by a pair of
	transmitted power		(c) cation and anion
	not related to the peak transmitted power		(d) occupation of interstitial site by a cation
	at all		occupation of interstitial site by an anion
	PART - II (CHEMISTRY)	51.	Which one of the following is amorphous?
	TART - II (GITEMIGTRI)		(a) Polystyrene (b) Table salt (c) Silica (d) Diamond
41.	īpbteasseignivalent weight of	52.	
71.	permanganate when it acts as oxidising		system is (a) Po (c) Cu
	agent in ferrous ion estimation is		(b) Na
	(a) 158 (b) 31.	53.	(d) Ag When ideal gas expands in vacuum, the work
	(c) 79 (d) 6	55.	done by the gas is equal to
42.	The magnetic moment of l3a9n.thanide ions is		(a) PV (b) RT
	determined from which on5e of the following		(c) 0 (d) nRT
	relation?	54.	
	(a) $\sqrt{n(n-2)}$ (b) $g\sqrt[4]{(J-1)}$		N2O4(g) 2NO2(g), the pressure (a remains constant(b) decreases
	(c) $g \eta (n-1)$ (d) $2 \eta (n-1)$) increases (d) becomes zero
43.	Which one of the following has maximum numbe	er55.	(6c m)oles of an ideal gas expand isothermally and
43.	of unpaired electrons?		reversibly from a volume of 1 litre to a volume of 10 litres at 27°C. What is the maximum work
	(a) Mg2+ (b) Ti3+		done?
	(c) V3+ (d) Fe2+		(a) 47 kJ (b) 100 kJ
44.			(c) 0 (d) 34.465 kJ
	(a) ZnH ² (b) Na2ZnO2	56.	,
4.5	(c) ZnO (d) Zn(OH) How many isomers does Co(en)2Cl2+ have?		Zn(s) + CuSO4(aq) $ZnSO4(aq) + Cu(s)$ is an
45.	(a) 1 (b) 3		example of a (a) spontaneous process
	(c) 2 (d) 4		(b) isobaric process
46.	NH3 group in a coordination compound is named	d	(c) non-spontaneous process
	as		(d) reversible process
	(a) ammonium (b) ammine	57.	For the reaction, H2 (g) + I2 (g) 2HI (g)
4=	(c) amine (d) ammonia		(a) $Kpp == K-Kcc$ ((bd) $K0c = 0Kp$
47.	Name3)t4he complex Ni(PF (a) tetrakis (phosphorus (III) fluoride) nickel	58.	The increase of pressure on ice water at a
		50.	constant temperature will
	(b) tetra (phosphorus (III) fluoride) nickel		c(ausewater to vaporize(b) water to freeze
	(c) Nickel tetrakis phosphorus (III) fluoride) no change (d) ice to melt
	(d) (phosphorus (III) tetrakis fluoride) nickel	59.	T(ch)e order of the reaction
	(0)		N2O5 N2O4(g) + $\frac{1}{1}$ O2(g) is
48.			11200 11207(6) 1 02(6) 13
	The purple colour of KMnO4 is due to		(a) 2
	The purple colour of KMnO4 is due to (a charge transfer (b) d-d transition) f-f transition (d) d-f transition		(a) $\begin{array}{cccccccccccccccccccccccccccccccccccc$



Determine the experimental condition for the following reaction



- (a) in presence of KOH
- (b) on heating
- in presence of NaOH (c)
- (d) in presence of HCl
- 76. Which one of the following is an ingredient of Pthalic acid manufacture by catalytic oxidation
 - (a) (cB)enzene
- (b) Salicylic acid

On coAmntpharraisnoilnic wasitihaleHe)

- 77. С H bond angle of Cbond angle of methane, the C trimethylamine is
 - (a higher
- (b) no change
- not comparable(d) lower
- 78. T(ch)e treatment of acylazide (RCON3) with acidiæ5. or alkaline medium gives
 - (a) RCONH 2
- (bd))RRC-O NCHH2NH
- (c) RCH 2 NH2
- 79. The sequence of basic strength of alky1 amines follows the order
 - (a) RNH 2 < R2NH > R3N
 - (b) (cRR2R3BHN22-R2N NHVHHRHR22< <<
 - (d) RNH

Activation of benzene ring in aniline can be

- 80. decreased by treating with
 - dil. HCl (a acetic acid (c)
- (b) ethyl alcohol
- (d) acetyl chloride

PART - III (MATHEMATICS)

81. The value of x, for which the matrix

$$\frac{2}{x}$$
 1 2

- 2 xis&ingular, is
 - 1
- (a 1
- (c) ±
- (d) 2

82. If x = -9 is a root of $\begin{vmatrix} 2 & x & 2 \\ 7 & 6 & x \end{vmatrix}$ 0, then other

two roots are

- ₿a, 7
- (d) 7
- 83. (cT)he 3va, lues of for which the 2 s, ystem of equation x + y + 6 + z = 1, x + 2y + 4z = 6x + 4y + 10z = 2 is consistent are given by
 - 1, -2 (a 1, 2
- (b) -1, 2
- (d) 1, 1
- (c)

Let A 5 t , then the values of t 7t 6

for which inverse of A does not exist

- (a -2,
- (b) 3, 2 (d) 3, -1
- 12. T(ch)e n-o3n integer roots of

$$x^4 3x^3 2x^2 3x 1 0$$

(a)
$$\frac{1}{2}$$
(3 $\sqrt{13}$), $\frac{12}{2}$ (3 $\sqrt{13}$)

- (b) $1(3 \sqrt{13}), \frac{1}{2}(3 \sqrt{13})$
- (c) $\frac{1}{2}(3 \sqrt{17}), \frac{12}{-}(3 \sqrt{17})$
- (d) $\frac{1}{2}(3 \sqrt{17}), \frac{1}{2}(3 \sqrt{17})$
- $\sqrt{1}$ y2, then the value of y is 86.
- (c) ex e 2
- (d) ex e 2
- 87. Consider an infinite geometric series with the first term a and common ratio r. If its sum is 4 and

the second term is $\frac{3}{1}$ then

- (a) $a = \frac{4}{7}, r = \frac{3}{7}$ (b) $a = 2, r = \frac{3}{8}$
- (c) $a = \frac{3}{2}, r = \frac{1}{2}$ (d) $a = 3, r = \frac{1}{4}$

4cosC = 5, an arc of a bridge is rizontal. If the highest part of
an arc of a bridge is rizontal. If the
rizontal. If the
rizontal. If the
rizontal. If the
rizontal. If the
rizontal. If the
tal; the best ne arch, 2m from
ough (3,5) that + 5y2 = 32 and
hyperbola xy =
curve again at
- –1 -1 d in the
is at the ach side of
•
tal ne a oug + ! hyp cu -1 d in is a

101. If f(2) = 4 and f'(2) = 1,

then $\lim_{x \to 2} xf(2)$ $\lim_{x \to 2} xf(2)$ is equal to

- (a) 0 (b) $\frac{1}{2}$ (c) 1 (d) 2
- 102.What is the least value of k such that the function x2 + kx + 1 is strictly increasing on (1,2)
 - (a) 1 (b) -1 (c) 2 (d) -2 1
- 103.The maximum value of is
 - (a) e (b) ee
- 104.If u = tan-1 $\begin{pmatrix} x3 & y3 \\ x & y \end{pmatrix}$, then $x \neq y = uy$
 - (a) sin 2u
- (b) cos 2u
- (c) sec2 2u
- (d) tan 2u
- 105.If f'x $\frac{x}{\sqrt{1-x}}$ and f(0) = 0, then f(x) =
 - (a) $\frac{2}{3}$ (1 x) $\frac{3}{2}$ 6(1 x) $\frac{1}{2}$ 1

 - (c) $\begin{pmatrix} 2 & 3 & 1 & 1 \\ 3 & (1 & x)^2 & 4(1 & x)^2 & 2 \end{pmatrix}$

- 106. The value of the integral $\frac{2}{\log(\tan x)}$ dx
 - (a) 0 (b) 1
- 2 4 107.What is the area of a loop of the curve r = asin3?
 - a2 a2 (a) a2 (b) 8
 - (c) (d) 24
- 108.The value of the integral etdt
 - (a) e3 (b) 4e3 (c) 4(e3 - e) (d) 4e3 - 2e
- 109. The differential equation that represents all parabolas each of which has a latus rectum 4a and whose axes are parallel to the x axis is
 - (a) $\begin{array}{cc} d^2 \mathbf{Q} & 2dydx \\ d & 0 \end{array}$
 - (b) $\frac{82y}{dx^2} = \frac{dy}{dx} = 0$
 - (c) $a \frac{d^2y}{dx^2}$ dy^3 0
- 110. The solution of $x \cos y = 0$ $y \sin x + x \sin y = 0$

is

- (a) $\log |x| \cos \frac{x}{y}$ c
- (b) logx | cos (
- (c) $log \nmid l sin \frac{x}{y}$ c
- (d) logy | sin yx c

111. The particular integral of $\begin{array}{c} d2 \\ y \end{array}$ 2y x^2 is	117.In rolling two fair dice, what is the probability of obtaining a sum greater than 3 but not exceeding 6?			
(a) $x2-1$ (b) $d \times 2 + 1$ (c) $\frac{1}{2}(x2 1)$ $\frac{1}{2}(x2 1)$	(a) $\frac{1}{2}$ (b) $\frac{1}{3}$			
112. The solution of $(D2 + 16)$ y = $\cos 4x$ is	1 1 (c) 4 (d) 6			
(a) $A\cos 4x + B\sin 4x + \frac{x}{8}\sin 4x$	118.Team A has probability $\frac{2}{3}$ of winning whenever			
(b) $A\cos 4x + B\sin 4x + 8\sin 4x$	it plays. Suppose A plays four games. What is the probability that A wins more than half of its ga m es?			
(c) $A\cos 4x + B\sin 4x = \frac{x}{4} \sin 4x$	16 (a) 1 (b) 9			
(d) $A\cos 4x + B\sin 4x$ 4 $\sin 4x$	19 2 (c) 81 (d) 7			
(b) R (c) R34 == {{((11,,31)),, ((21,,12))}, (2,3), (1,3) (d) R	119.An unprepared student takes five-questions of nltrelations type quiz and guesses every answer. What is the probability that the student will pass, (the)quiz if at least four correct answers is the passing grade?			
114.Find the number of ways in which five large books, four medium-size books, and three small books can be placed on a shelf so that all books of the same size are together.	(a) 1 (b) 3 16			
(a $5 \times 4 \times 3$ (b) $5! \times 4! \times 3!$	(c) $\frac{1}{32}$ (d) $\frac{3}{32}$			
) $3 \times 5! \times 4! \times 3!$ (d) $3! \times 5! \times 4! \times 3!$ 115.C(ocn)sider the set Q of rational numbers. Let be the operation on Q defined by a b = a + b - ab.	120. The probability density $f(x)$ of a continuous random variable is given by $f(x) =$			
The identity element under is (a) 0 (b) 1	Ke $ x $, x . Then the value of K is			
(c) 2 (d) not exist 116.The statement ~ p q is equivalent to (a) p q (b)~ p q	(a) 1 (b) 2 1			

(c) 4

(d) 4

(a) p q

(c) ~ p ~ q

(b)~ p q

(d) p ~ q

2006 SOLUTIONS

3.

5.

PART - I (PHYSICS)

1. (b) V= 300 V, 1C= 2.0F, C2= 8.0F,

Net capacitance, $\begin{bmatrix} 1 & 1 & 1 \\ C_s & C_1 & C_2 \end{bmatrix}$

Now total charge,

- Q = $V \times C = 300 \ 0.6 \times 10^6 = 4.8 \times 10^6$. In series charge is same on capacitors Charge on 2 F capacitor is $4.8 \times 10 - 40$
- 2. (a) Ĉ P C

Let the point P where resultant field is zero be x m from 4C charge and (1-x) m distance apart from -2C charge. Since field is zero at this point then,

$$0 \frac{1}{4_{0}} \frac{4 C}{x 2} \frac{-2C}{1-x^{2}}$$

$$21 - x 2_{x}^{2}$$

Taking root $\sqrt{2}1-x$ x

x 0.58m

(b) The net electric potential is algebraic sum of potential due to individual point charges.

V
$$4\frac{1}{0}\frac{110^{-6}}{0.2}\frac{2}{0.2}\frac{10^{-6}}{0.2}\frac{310^{-6}}{0.3}$$

9 109 5-10 10 10⁻⁶

910 3 5 $4510V^3 = 45 kV$

4. (a) In a metal, conduction current is due to electrons given by

I nAev

drift velocity, v
$$\begin{array}{c} I \\ \text{nAe} \\ 5 \\ 5 & 10^{26} \end{array}$$
 $\begin{array}{c} 1 \\ 106 \\ 1.602 \ 10^{-19} \\ 1 \\ 4 \ 1.602 \ 101 \end{array}$

10-1 6.408 =1.56 ×10 -2 m/s

(b) In series combination of capacitors, charges on both capacitors will be same.

V_s Q Q C1 C2

1000 Q C 1 C2 G_{C2}

2 10-9C

6. (c) Parallel combination of 3 and 6 gives effective resistance,

2 gives net ressistance as 4

7. (b) The value of temperature coefficient of resistance is given by

R2-R1 65 - 50 R1 t2 -1 t 50 70-20

(t1 and t2 are in °C)

15 50 50 0.006/ C

8 (b) In Leclanche cell a strong solution of ammonium chloride acts as an electrolyte. 14. (a)

(d) Ign = t hmea gxa. lcvuarnreonmteter, I
through galvanometer, S = shunt
resistance G = galvanometer

9 resistance, G = galvanometer
resistance then

Ig(galvanometer) = I S G S S S I Ig 51Ig

10. (a) Current in tangent galvanometer

I Gtan

Where G = galvanometer constant H= earth's horizontal field = constant

11. (c) Lorentz force on a charged particle in presence of magnetic and electic field is

F Fe Fm

F qE qv B

12. (a) In a circular coil of n turns, magnetic field is

B 0nI 4 10-7 250 20 10 -3 2r 2 40 10-3 (n = no. of turns, I = current through coil, r = radius of coil)

3 4 250 20 10 ^{-7-3 3} 2 40

250 3.14 10-7

785 10–7 0.785 10 ⁻⁴ tesla = 0.785 gauss

13. (d) RMS value of A.C is

 $I_v = \frac{I0}{\sqrt{2}} = 0.707I \ 0$

I0 = peak value it is 70.7% of peak value.

(a) Q-factor is given by Q $\frac{1}{R}\sqrt{\frac{L}{C}}$

If resistance R is decreased, Q increases and inductance L is increased, Q increases.

15. (c) Induced emf e -d. Assuming, small dt

change in flux $d=8\times10-4$ Wb change in time dt=0.5s

 $|e| = \begin{cases} 8 & 10 - 4 \\ 0.5 \end{cases} = \begin{cases} 80 & 10 - 4 \\ 5 \end{cases}$

 $=16 \times 10 - 4 = 1.6 \times 10 - 3 \text{ V} = 1.6 \text{ mV}$

16. (c) Current through an LCR circuit is maximum when impedance is minimum. Now impedance

$$Z \sqrt{R2} \qquad L - \frac{1}{C}^2$$
 is minimum at

resonance frequency when L C

Z= R = minium i.e., inductive reactance (L) is equal to capacitive reactance (1/C)

- Our eyes respond to visible range from 400 nm to 700 nm
- Velocity of electromagnatic wave in space

(a is c
$$\frac{1}{\sqrt{\frac{0}{1}}}$$
 c $\frac{1}{\sqrt{2}}$ 8

17

18

19. (b) According to Brewster's law, reflected 25. light is plane polarised if unpolarised light falls at the interface of air and medium at aipn caanlgleled and get asn) gel eta thh6e0n

 $= \tan ip$

20. (a) Newton's ring arrangement is used for dofetermining the wavelength monochromatic light. For this the diameter of nth dark ring (Dn) and (n + p)th dark ring (Dn + p) are measured then

 $D2(n_{p)}$ 4(n p)R and D2 4nR $D2_{np}$ Dn

4pR

Here, n = 10, n + p = 20; p = 10; R = 1 m, D1 = 0 3.96 \times 10-3 m, D 2=0 5.82 \times 10- m3

> D220 D ²₁₀ 4pR

(5.82 10 3)2 (3.36 10 ³)2 4 10 1

= 5646 Å

21. (b) Angular momentum in any stationary orbit

is mvr $\frac{nh}{2}$ for 4th orbit, n = 4

mvr 4l

22. (d) According to Bohr's, Brackett series is obtained when an electron jumps to 4th orbit from any other outer orbit Total

23. (a) energy of electron

Potential energy in the orbit P.E. -KZe2

P.E. = $2 \times E$ P.E. = $2 \times (-13.6) = -27.2 \text{ eV}$

24. (a) Bragg's condition is 2dsin = n for second order n = 2, sin = 1. For longest d = 2

(b) Photon moves with speed of light ie, v = c and rest mass of a particle is

 $m^0 m_1 - v^2/c^2$

26. (c)

hence m0 (photon)= 0 photon has zero rest mass.

h
Momentum of photon =
de Broglie wavelength is given by

h $6.626\,10^{-34}$ mv $1000\,10^{-3}$ 1 $6.626\,10^{-34}$ m

27. (b) Let the velocity of a particle be v where mass m is double the rest mass i.e., m = 2m then

 $m_0 \qquad \sqrt{1-\frac{v^2}{e^2}} \qquad m_0 \qquad 2m0 \sqrt{\frac{1-vc^2}{2}}$

$$\frac{1}{2} \sqrt{\frac{\frac{\sqrt{2}}{1-2}}{1-14}} \quad 1 = 1 - \sqrt{\frac{2}{c_2}}$$

$$\sqrt{\frac{1}{1-14}} \quad 4$$

$$\sqrt{\frac{2}{c_2}} \quad 3$$

$$\sqrt{\frac{2}{c_2}} \quad 4$$

$$v \sqrt{\frac{3}{4}c}$$

28. (d) By Einstein's equation E= mc2 where m = 2kg

E = 2×(3 × 10 8)2 = 2 × 3 × 3× 10 16 = 18 × 1016 J

- 29. (b) By definition, the difference between the sum of the masses of neutrons and protons forming a nucleus and mass of nucleus is called mass defect
- 30. (b)Mean life time = 1.44 T where T is half life period of an atom

$$= 1.44 \text{ T} =$$
 0.6931
 0.6931minute

31 (d) (by conservation of charge)

32

33.

(d) Baryons are proton, neutron, lamda,

sigma (–), Xi 0,–

(c) As donor and acceptor impurities are added to semiconductor to make an extrinsic semiconductor, intrinsic semiconductor is formed by internal generation of e- by breaking up of covalent bonds.

- 34. (d) In p-type semiconductor, valency = 3, thus there is one unYformed bond or hole created. This hole is in valence band and is able to cause hole current. The energy levels of acceptor are in forbidden gap just above valence band In an oscillator,
- 35. (d)
 L-C circuit is coupled with transistor amplifier in such a way that there is a positive feed back to the LC circuit i.e., proper energy supply to LC at proper timings. So that total energy of LC circuit remains same. The gates AND, OR, NAND do not give binary addition, however in
- 36. (c) EXOR gate

truth table is

Α	В	Υ	
0	0	0	
0	1	1	
1	0	1	
1	1 1	0	

This shows it gives perfect binary addition

37. (d)In FM, carrier frequency is the constant frequency which is modulated by signal amplitude. It is also called carrier swing. (Centre frequency is fc in AM wave,

frequency deviation fmax – fc,

modulationfactor max)

38. (c) The common antenna is a straight

conductor of length l held vertically

with its lower end touching the ground.

- 39. (b) The vidicon is a storage-type camera tube in which a charge-density pattern is formed43. by the imaged scene radiation on a photoconductive surface which is then scanned by a beam of low-velocity electrons. The fluctuating voltage coupled out to a video amplifier can be used to reproduce the scene being imaged. The electrical charge produced by an image will remain in the face plate until it is scanned or until the charge dissipates.
- 40. (b)Maximum range of radar d $_{\rm max}$ $_{\rm \sqrt{l}}$ and power transmitted by antenna of length lis

p l/
2
 l \sqrt{p} and d $p1/4$

PART - II (CHEMISTRY)

41. (b) The oxidation of ferrous ion by KMnO takes place in acidic medium as per following reaction

2KMnO4 + 8H2SO4 + 10FeSO4

K2SO4 + 2MnSO4 + 8H2O + 5Fe2(SO4)3 Eq. mass of KMnO4

Molecular mass changein oxidation number

$$= \frac{\text{Molecular mass}}{5} = \frac{158}{5} = 31.6$$

42. (b) In case of lanthanoids, 4f orbitals lie too deep and hence the magnetic effect of the motion of the electron in its orbital is not quenched out. Here spin contribution S and orbital contribution L couple together to give a new quantum number J.

Thus magnetic moment of lanthanoids is

given by,
$$g\sqrt{J(J-1)}$$

where J = L - S when the shell is less than half fill

J = L + S when the shell is more than half fill

(d)Mg2+ = 1s2, 2s2, 2p6 (No unpaired electrons)

Ti3+ = 1s2, 2s2, 2p6, 3s2, 3p6, 4s0, 3d1

(One unpaired electrons)

V3+ = 1s2, 2s2, 2p6, 3s2, 3p6, 4s0, 3d2

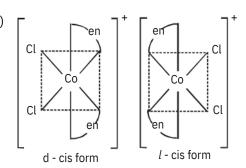
(Two unpaired electrons)

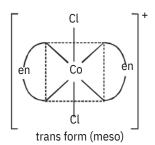
Fe2+ = 1s2, 2s2, 2p6, 3s2, 3p6, 4s0, 3d6

(Four unpaired electrons)

Fe2+ has highest number of unpaired el ect r on s.

44. (d) Zn + 2NaOH Na2ZnO2 + H2 Sod. zincate





- 46. (b) Neutral ligands are given the same names 58. (d)Ice as the neutral molecule. However, two very important exceptions to this rule are: H2O Aquo (Aqua) NH3 Ammine.
- 47 (a) Ni(PF 3)4 tetrakis phosphours (III) fluoride nickel (0). The colour of KMnO transfer.
- . (a) The configuration o4f ism dauneg taon ecshea rgien permagnate ion is d0 but it is coloured because its electrons are photoexited. In face centred cubic lattice, the
- 4.9. (c) atoms are present at eight corners of faces and one each at 6 faces.

Lattice points belonging to face centred

- 50. (a) Schottky defect is caused when equal number of cations and anions are missing from their lattice sites.
- 51 (a) Polystyrene is thermoplastic substance.
 - (a) Po Simple cubic lattice
- 52 Na bcc Cu fcc

53. (c) W_{irr} Pext P1T2 P2T1

During expansion in vaccum $P_{ext} = 0$ work done = 0. 54. (b) As the system is closed, hence the reaction will be reversible, hence according to Le-chatelier principle pressure decreases since the volume is increasing.

55. (d)W = -2.303 nRT loVg2

Given n = 6, T = 27° C = 273 + 27 = 300 K V1 = 1 L, V2 = 10 L

 $W = -2.303 \times 6 \times 8.314 \times 300 \log_{10}^{10}$ = 34.465 kJ

- 56. (a) It is spontaneous process because zinc is more reactive than copper, hence can easily repace Cu from CuSO4.
- 57. (c) $K_p = K \text{ pc } ((gR)T -) \text{ nr}(g) = 2 2 = 0$ n = nKp = Kc
- 58. (d)Ice Water

The volume of ice is more than water. Therefore when pressure is increased the equilibrium shifts in forward direction. It favoures melting of ice.

- 59. (c) It is a first order reaction because rate of reaction [N2O5]
- 60. (d) The reactions with low activation energies are always fast whereas the reactions with
- 61. (d) high activation energy are always slow.
 For spontaneous reaction free energy change is pegative.
- 62. (a) Because at infinite dilution the equivalent conductance of strong electrolytes furnishing same number of ions is same.
- 63. (c) Reducing character i.e tendency to loose electron decreases down the series, hence
- 64. (b) the correct order is Zn > Cu > Ag. £Ht +a n2oHdOe the CfOol l+o w8Hin g+ +r e8aec -tion takes
- 65. (a) Optrycgeen atom in alcohol molecule is sp3 hybridised.
- 66. (d) In this reaction LiAlH 4 acts as reducing

0 || agent. RCOH LiAlH4 RCH2OH

- 67. (d) 3° alcohols are resistant to oxidation and 73. (d) The O H strecting of carboxylic acid are oxidised only by strong oxidising absorb in region of 1700-2000 cm–1 agents 3. They are resistant to loikxied actoionnc i.n HneNuOtral or alkaline KMnO4.
- 68. (b) C2H5 O C2H5 H2O boil,dil.acid 2C2H5OH ethyl alcohol

70. (b)

Para aldehyde (pleasant smelling liquid, used as hypnotic and soporofic) (sleep producing)

cyclic ketal

(used as solid fuel in spirit lamps)

71. (c) 2(CH3COO)2Ca di sti llat ion

CH3COCH3 + 2CaCO3 Acetone Calcium carbonate

- 72. (d) Ketones do not react with alcohol.
 - (i) Aldehydes reduction 1° alcohol
 e.g., CHCHO CH 3CH 02H
 - (ii) Ketones reduction 2° alcohol C = 0 C = 0 C = 0 C = 0 C = 0 C = 0 C = 0
 - (iii)Ketones do not reduce Fefiling solution but aldehydes do so.

74. (b) Formic acid halle of the

group and therefore it reduces Fehling solution.

75. (c) \bigcirc OH NaOH \bigcirc OH + \bigcirc CO₂

This is decarboxylation reaction.

76. (d) Catalytic o xi da ti on

Napthalene

- 77. (b) In both the cases carbon is sp3 hybridised and bond angle is 109°28'.
- 78. (b) This reaction is known as curtius rearrangement.

RCON ₃ N₂ RNCO ^{2 NaOH} Na2CO3 + RNH2

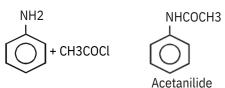
Nazcos + Ri

1° amine is formed.

79. (a) It is expected that the basic nature of amines should be in order tertiary > secondary > primary but the observed order in the case of lower members is found to be as secondary > Primary > tetriary. This anomalous behaviour of tetriary amines is due to steric factors i.e crowding of alkyl groups cover nitrogen atom from all sides thus makes the approach and bonding by a proton relatively difficult which results the maximum steric strain in tetiary amines. The electrons are there but the path is blocked, resulting the reduction in basicity. Thus the correct order is

R2 NH > R NH2 > R3N.

80. (d) On acetylation aniline is converted into acetamide which is resonance stablised and therefore less reactive.



PART - III (MATHEMATICS)

81. (a) We know that, A is singular if |A| = 0

$$|A| \begin{vmatrix} \frac{2}{x} & 1 & 2 \\ 1 & x & 2 \\ 1 & \frac{1}{x} & 2 \end{vmatrix} \times Q^{2}$$

$$|A| \quad {\overset{2}{\tiny X}} \quad 2x \quad 2x \quad 1 \quad 2 \quad 2x \quad 2 \quad 2 \quad {\overset{1}{\tiny X}} \quad x \quad 0$$

x3x2x10 x2(x 1)

0

х 1

82. (b) Given $\begin{vmatrix} x & 3 & 7 \\ 2 & x & 2 \\ 7 & 6 & x \end{vmatrix}$

x3 67x 126 0

But given (x = 9) is a root of given determinant.

(x + 9) is a factor

$$(9)(x^{2} 9x 14) 0$$

$$x 9)(x^{2} 7x 2x 14) 0$$

$$(x 9)(x 7)(x 2) 0$$

$$x 9,7,2$$

83. (c)We have

~
$$\begin{vmatrix} 1 & 1 & 1 & : & & 1 \\ 0 & 1 & 3 & : & & 1 \\ 0 & 0 & 0 & : & ^2 & 3 & 2 \end{vmatrix}$$

applying R₃ R₃ 3R2

But the system is consistent

84. (c)We know that inverse of A does not exist only when |A| = 0

$$t2 \ t \ 6 \ 0 \ t2 \ 3t \ 2t \ 6 \ 0$$

85. (a) Given x4 - 3x3 - 2x2 + 3x + 1 = 0By using Hit & trial method, we have (x - 1) is a factor of given equation (x - 1)(x3 - 2x2 - 4x - 1) = 0

$$(x \ 1)(x \ 1)(x2 \ 3x \ 1) \ 0$$

 $x = 1, -1 \text{ or } x2 - 3x - 1 = 0$
Now $x2 - 3x - 1 = 0$

$$x = \frac{3 \sqrt{9 + 4}}{2}$$

$$x \quad \frac{3 \quad \sqrt{13}}{2}$$

non-integer roots of given equation are

$$\frac{1}{2}(3 \quad \sqrt{13}), \frac{12}{2}(3 \quad \sqrt{13})$$

86. (b) Given ex $y \sqrt{1 + y^2}$

ex
$$y \sqrt{1 y^2}$$

Squaring both side, we have e2x + y2 - 2exy = 1 + y2

$$2ex y = e2x - 1$$

$$e2x$$

y
$$\frac{1}{2ex}$$
 y $\frac{1}{2}$ e^x e^x

87. (d) First term = a & common ratio = r

Given S
$$4\&a$$
 $\frac{3}{4}$

Equation (1) becomes $\frac{3}{4r(1 r)}$ 4

when r
$$\begin{pmatrix} 1 \\ 4 \end{pmatrix}$$
 then a $\begin{pmatrix} 3 \\ 4 \end{pmatrix}$ $\begin{pmatrix} 1 \\ 4 \end{pmatrix}$

88. (c) Given: & are roots of equation ax2 + bx + c = 0

Now,
$$3 3 ()^3 3 ($$

89. (b) Given: The vertices of tetrahedron are P(-1, 2, 0), Q(2, 1, -3), R(1, 0, 1) & S(3, -2, 3)

Volume of tetrahedron 1 PQPRPS 6

Now,

$$PQ (2 1)i^{(1 2)j^{(3)}k^{3}} 3i^{\hat{j}} 3k^{\hat{j}}$$

Similarly, PR 2i^2j^k^

Volume of tetrahedron

90. (a)We have, a tb
$$(i^2j^3k^2)t(\hat{i}^2j^k^2)$$

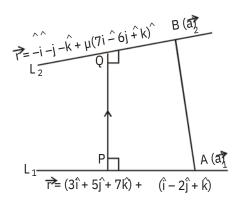
 $(1 t)i^2(2 2t)j^3(3 t)k^2$
It is to c $3i^2j^2$
If $3(1 t) (2 2t) (3 t)(0) 0$
3 3t 2 2t 0 t⁵

91. (d) The equation of the plane through the line of intersection of the given planes is (x2 x+ +y 3+y z+ -4 6z)+5)=0...(1) If equation (1) passes through (1, 1, 1), we have

Putting $\frac{3}{14}$ in (1), we obtain the equation of the required plane as

$$(x \ y \ z \ 6) \ \overset{3}{1}4(2x \ 3y \ 4z \ 5) \ 0$$
 $20x \ 23y \ 26z \ 69 \ 0$

92. (d) Shortest distance^{PQ} $\frac{\begin{vmatrix} b_1 & b2 & . & a_2 & a_1 \\ & b1 & b_2 \end{vmatrix}}{\begin{vmatrix} b_1 & b_2 & . & a_2 & a_1 \end{vmatrix}}$ 94. (b) Now, $a_2 \quad a_1 \quad \hat{i} \quad \hat{j} \quad \hat{k} \quad \hat{3} \quad \hat{i} \quad \hat{5} \quad \hat{j} \quad \hat{7} \quad \hat{k} \quad \hat{a}_2 \quad a_1 \quad \hat{4} \quad \hat{6} \quad \hat{j} \quad \hat{8} \quad \hat{k}$



And
$$b_1$$
 b_2 $\begin{vmatrix} \hat{i} & \hat{j} & k \\ 1 & 2 & \\ 7 & 6 & 1 \\ & & 1 \end{vmatrix}$

$$b_1 \ b_2 \ \hat{i}(26) \ \hat{j}(17) \ k(614)$$
 $b_1 \ b_2 \ 4i \ 6j \ 8k$
Shortest distance

PQ
$$\left| \frac{(4i^{\circ} 6j^{\circ} 8k^{\circ}).(4i^{\circ} 6j^{\circ} 8k^{\circ})}{\sqrt{16 \ 36 \ 64}} \right|$$

PQ
$$\frac{16 \ 36 \ 64}{\sqrt{116}}$$

$$\begin{vmatrix} \frac{11}{\sqrt{6}} \\ \frac{1}{\sqrt{6}} \end{vmatrix} = \sqrt{116} = 2\sqrt{29}$$

$$\begin{array}{c} 11 \\ PO \\ 6 \end{array} = 2\sqrt{29} \text{ units}$$

93. (c) Given, |z i| |z i| 4 |z (0 i)| |z (0 i)| 0

This equation represent the interior and boundary of ellipse with foci at (0, 1) & (0, -1), whose major axis is along the yaxis.

94. (b)
$$i^{n}$$
 in i^{n} in i

95. (b) Given: sin 1,cos,tan are in G.P.

$$\cos^2$$
 $\sin \tan$ $\cos 3$ $\sin 2$
 \cos^3 $1\cos 2$
 $(\cos^3$ $\cos 2) 1$...(1)

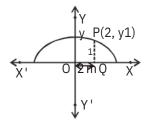
Cubic both sides, we have

$$\cos \cos \cos 6 - 3\cos^5 \cdot (\cos^3 - \cos^2) - 1$$
 $\cos \cos^6 - 3\cos^5 - 1$
[Using equation (1)]
 $\cos \cos \cos 6 - 3\cos 5 - 1 = 0$

97. (b) Equation of the semielliptical bridge

Here,
$$2a = 9$$

a
$$\frac{9}{2}$$
, b = 3



Here,
$$OQ = 2 \text{ m, let } PQ = y_1$$

 $P(2, y1)$

Since point P lies on the ellipse (2)

Hence, best approximation of the height of

the arch
$$\frac{8}{3}$$
 m.

98. (c) Given: Equations of ellipses

$$3x2 + 5y2 = 32$$
 ...(1)

$$\& 25x2 + 9y2 = 450$$
 ...(2)

Tangents to the ellipse (1) & (2) are passing through the point (3, 5)

$$3(3)2 + 5(5)2 - 32 = 27 + 75 - 32 > 0$$

So the given point lies outsides the ellipse. Hence, two real tangents can be drawn from the point to the ellipse,

$$\& 25(3)2 + 9(5)2 - 450 = 225 + 225 - 450 = 0$$

The point lie on the ellipse. Hence one real tangent can be drawn.

No. of real tangents = 3

99. (b) The equation of tangent at
$$ct$$
, ct is

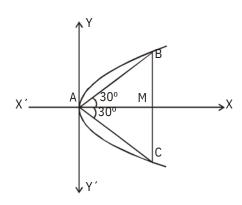
$$ty = t3x - ct4 + c$$

If it passes through ct',ct' then

t t3t'2 t4t't'

Note: If we take the co-ordinate axes along the asymptotes of a rectangular hyperbola, then the general equation x2 - y2 = a2 becomes xy = c2, where c is a constant.

AM
$$\cos 30^{\circ} \frac{\sqrt{}}{2}$$



So, the coordinates of B are $\frac{\sqrt{3}}{2}$, $\frac{1}{2}$

Since, B lies on y2 = 4x

$$\frac{2}{4}$$
 4 $\frac{\sqrt{3}}{2}$

$$\frac{16}{2} \cdot \sqrt{3}$$
 $8\sqrt{3}$

101. (d) Let
$$f(x) = ax + b$$

Given $f(2) = 4 & f'(2) = 1$
 $f(2) = a \cdot 2 + b = 4$ 2a + b = 4 ...(1)

& f'(x) = a f'(2) = a = 1 a = 1

$$2 \times 1 + b = 4$$
 b = 2 [using equation (1)]
 $f(x) = x + 2$

Now,
$$\lim_{x \to 2} \frac{\lim_{x \to 2} x + 2}{x + 2}$$

 $\lim_{x \to 2} 4$
 $\lim_{x \to 2} x + 2$
 $\lim_{x \to 2} (x + 2)$

$$x = 2 (x = 2)$$

102. (d) Let $f(x) = x2 + kx + 1$

f'(x) = 2x + kf(x) is strictly increasing on (1, 2)

if f'(x) > 0 for x (1, 2)

$$2x + k > 0$$
 for x (1, 2)
 $k > -2x$ for x (1, 2)
Now, $1 < x < 2$ $2 < 2x < 4$
 $-2 > -2x > -4$

$$-4 < -2x < -2$$

Hence least value of k = -2.

103. (c) Let y
$$1x^{x}$$
 y xx
Then $\log y = -x \log x$

Also,
$$\begin{pmatrix} d2 \\ y \end{pmatrix}$$
 at $x = \begin{pmatrix} 1 \\ e \end{pmatrix}$ is $e^{1} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$ dy dx

So, $x = \begin{bmatrix} 1 \\ e \end{bmatrix}$ is a point of local maxima.

Maximum value

104. (a) Euler's theorem x $\stackrel{Z}{x}$ y $\stackrel{Z}{y}$ nz

Given:
$$U = \tan^{-1} \frac{x3}{x} \frac{y3}{y}$$

$$\tan U \frac{x3}{x} \frac{y3}{y} z(let)$$

$$n = 3 - 1 = 2$$

$$x \frac{z}{x} \frac{y}{y} \frac{z}{y} 2z$$

sec2 U.x X y Uy 2tanU

105. (b) Given:
$$f'(x) = \frac{x}{\sqrt{1-x}}$$
, $f(0) = 0$

$$f'(x)dx = \frac{x}{\sqrt{1-x}}dx$$

$$f(x) = \frac{x}{\sqrt{1-x}}dx$$

Let
$$1 + x = t2$$
 $x = t2 - 1$
 $dx = 2t$. dt

$$f(x) = \begin{array}{ccc} t^2 & 1 \\ t & .2t \, dt & 2(t2 & 1) dt \end{array}$$

$$f(x)$$
 2 $\frac{t3}{3}$ t c

But
$$f(0) \quad 0 \quad 2^{13} \quad 1 \quad c \quad 0$$

$$\frac{4}{3}$$
 c 0 c $\frac{4}{3}$ Equation (1) becomes

$$f(x)$$
 $\frac{2}{3}(1x)$ $\frac{3}{2}$ $3(1x)$ $\frac{1}{2}$ 2

Then, I
$$\begin{bmatrix} 2 \\ \log \tan & x \\ 2 \end{bmatrix}$$
 dx $\begin{bmatrix} a \\ f(x)dx \end{bmatrix}$ $\begin{bmatrix} a \\ f(a x)dx \\ 0 \end{bmatrix}$

$$\begin{bmatrix} 2 & 1 \\ \log & \tan x \, dx \end{bmatrix}$$

$$a^2$$
 sin2 d 6 0

I I 2I 0 I 0

[Using eq. (1)]

a2	² 1	² 1 cos2			
٠.	0	2	d		

	3	0	<u>-</u> 2		3 2	2	<u>5</u> 2	3
ſ		n				2	5	
		0	6	3	2	3	6	
T	r	0	٠	0	а	0	а	0

cos2 12sin

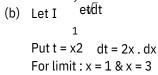
. sin

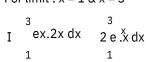
a2 . sin 24

sin2

0

0 & as r varies from
$$r = 0$$
 to $r = 0$.
3 108. (b) Let I et d





2
$$xe^{x} = \frac{3}{1} ex^{\frac{3}{1}}$$

Hence, the area of the loop lying in the

$$_{
m I}$$
 23e3e1 $_{
m e^3}$ $_{
m e^1}$ 2e3.2 4e3

positive quadrant
$$\begin{pmatrix} 1 & 3 \\ 2 & 0 \end{pmatrix} r^2 d$$

109. (d) Equation of the family of such parabolas is
$$(y-k)2 = 4a(x-h)$$
 ...(1) where h & k are arbitrary constants Differentiating w.r.t. x, we get

 $1^3 \sin 2$.13d 2_0

Differentiating again

$$(y \ k) \ \frac{d^2y}{dx^2} \ \frac{dy}{dx} \ ^2 \ 0 \ ...(3)$$

[On putting, 3

d $\frac{1}{3}$ d]

Putting value of (y - k) from (2) in (3), we get

 $\begin{array}{ccc} d2y & dy & ^3\\ 2a\,dx2 & dx & 0$, which is required equation.

110. (b) Given: x cos ec x y dx xdy 0

x y.sin ^{yx} dx xsin ^y dy 0

Put $\frac{y}{x}$ z y zx dy dx z.1 x.dzdx z xdzdx

Equation (1) becomes

log|x| cos yx

$$d2y$$
 111. (c) If dx^2 2y x^2

 $(D2 \quad 2)y \quad x^2 \qquad D \quad d$

Particular integral (P.I.)
$$\begin{array}{cc} 1 & .x2 \\ D2 & 2 \end{array}$$

$$(1 D)^{1} 1 D D2 D^{3} \dots \dots \dots D2$$
P.I. $\frac{1}{2}$.1 $\frac{1}{2}$ $\frac{D2}{2}$ $\frac{D}{2}$ $\frac{$

P.I.
$$\frac{1}{2}$$
. x^2 x^2 x^2 x^2 x^2 x^2

112. (a) If $(D2 + 16)y = \cos 4x$

Here the auxiliary equation is m2 + 16 = 0 $m = \pm 4$

Complementary function

 $= (A \cos 4x + B \sin 4x)$

& Particular Integral (P.I.)

11

3.

11

But D2 a2cos ax 2 asinax

P.I.
$$\begin{array}{c} x \\ 2 \end{array}$$
 sin4x $\begin{array}{c} x \\ 8 \sin 4x \end{array}$

Solution y = Complementary function + Particular Integral

$$y = A \cos 4x + B \sin 4x + \frac{x}{8} \sin 4x$$

(c)
(d) Let us make one packet for each of the books on the same size. Now, 3 packets can be arranged in P(3, 3) = 3! ways 5 large books can be arranged in 5! ways 4 medium size books can be arranged in 4! ways 3 small books can be arranged in 3! ways

Required number of ways = 3! × 5! × 4! × 3! ways

115. (a) An identity relation is one in which every element of a set is related to itself only. a * b = a + b - ab

As in identity relation 'a' is related to 'a', so the correct option will be the one which gives the value of the relation = 'a'. So, equating a + b - ab = a, we get b(1 - a) = 0. Now putting the values of a, we find b and the option in which a = b, will be the answer. For a = 0, b = 0, so the correct option.

For a = 1, b(1 - 1) = 0 b can have multiple values. For a = 2, b(1 - 2) = 0

$$b = 0$$
 but $a = 2$.

- 116. (a) p q ~p ~pvq p q
 T T F T T
 T F F F F
 F T T T
 F F T T
- 117. (b) Let S be the sample space

Events

[sum greater than 3 but not exceeding 6] 120.(a) = {(2, 2), (3, 1), (1, 3), (4, 1), (1, 4), (5, 1) (1, 5), (3, 2), (2, 3), (4, 2), (2,4), (3, 3)}

Required probability =
$$n(E)$$
 12 1
 $n(S)$ 36 3

118. (a) Let 'p' denote the probability of winning of team A whenever it plays

Let X denotes the number of winning games out of 4 games i.e. n = 4

The probability of r success P(X = r) = nr cpr nq - r, r = 0, 1, 2, 3, 4

Probability of winning more than half games = P(X > 2)= P(X = 3) + P(X = 4)

$${}^{4}C_{3}$$
 ${}^{2}_{3}$ 3 ${}^{13}{}^{4}$ 3 ${}^{4}C_{4}$ ${}^{2}_{3}$ 4 1 4 4

4! .8.1 4! .16 3!1! 27 3 4!0! 81

3 16 4 1 2 81 8 6

n =8total number of ways = 25 = 32Since each answercan be true or false & m = favourable number of ways = $5C_4 + 5C_5$

5! 5! 4!1! 5!0! 5 1 6 m 6

Since to pass the quiz, student must give 4 or 5 true answers.

Since f(x) is the probability density function of random variable X.

f(x) 1

Now we have

Ke |x|dx 1 2 K.e |x|dx 1

2 K.e ^xdx 1

2K.e ^x 1 2K 1

K 1