# **BITSAT 2015 Question Paper with Answer Key Birla Institute of Technology and Science Admission Test**

# **BITSAT : SOLVED PAPER 2015**

# (memory based)

This question paper contains total 😘 🚱 questions divided into four parts Part > Physics Q No 🐔 to

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Part ♭V Mathematics Q No 🌣 to 🌣�

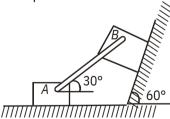
- 꾀II questions are multiple choice questions with four options only one of them
- 쟼ach correct answer awarded 🛭 marks and 🚓 for each incorrect answer
- uration of paper □

# PART - I: PHYSICS

An artificial satellite is moving in a circular orbit around the earth with a speed equal to half the magnitude of the escape velocity from the earth. The height (h) of the satellite above the Sarface is (Take radius of earth as Re)

(a) h = 2R

- (c)  $h = 2R_e$ In figure, two blocks are separated by a uniform strut attached to each block with frictionless pins. Block A weighs 400N, block B weighs 300N, and the strut AB weigh 200N. If  $\mu = 0.25$  under B, determine the minimum coefficient of friction under A to prevent motion.



- (b) 0.2 (c) 0.8 (a) 0.4 (d) 0.1
- Two tuning forks with natural frequencies 340 Hz each move relative to a stationary observer. One fork moves away from the observer, while the other moves towards the observer at the same speed. The observer hears beats of

- frequency 3 Hz. Find the speed of the tuning forks.
- (a) 2.5.5m/ns/s(b) 2 displacement/of a particle is given at time t, by:

 $x = A\sin(-2wt) + B\sin 2wt$  Then.

(a) the motion of the particle is SHM with an

amplitude of 
$$\sqrt{A2 + \frac{B2}{4}}$$

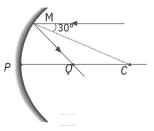
- (b) the motion of the particle is not SHM, but oscillatory with a time period of T = p/w
- the motion of the particle is oscillatory with
- a time period of T = p/2w
- the motion of the particle is a periodic.
- A ray parallel to principal axis is incident at 30° from normal on concave mirror having radius of curvature R. The point on principal axis where rays are focussed is O such that PO is

(a) 
$$\frac{R}{2}$$

(b) 
$$\frac{R}{\sqrt{3}}$$



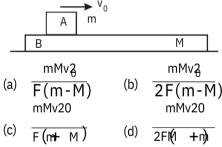
(d) 
$$R_{e}^{2} - \frac{1}{\sqrt{3}} = \frac{1}{2}$$



A solid sphere of radius R has a charge O distributed in its volume with a charge density r =  $kr\alpha$ , where k and  $\alpha$  are constants and r is the distance from its centre. If the electric field at r

is  $\frac{1}{8}$  times that at r = R, the value of  $\alpha$  is (a)

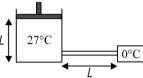
- (a) 3 (b) 5 (c) 2 (d) 7 A charged particle moving in a uniform magnetic 7 field and losses 4% of its kinetic energy. The radius of curvature of its path changes by
- (b) 4% (c) 10%
- Calculate the wavelength of light used in an 8. interference experiment from the following data: Fringe width = 0.03 cm. Distance between the slits and evepiece through which the interference pattern is observed is 1m. Distance between the images of the virtual source when a convex lens of focal length 16 cm is used at a distance of 80 cm from the eyepiece is 0.8 cm.
  - (a) 0.0006 Å
- (b) 0.0006 m
- (c) 600 cm
- (d) 6000 Å
- The masses of blocks A and B are m and M respectively. Between A and B, there is a constant frictional force F and B can slide on a smooth horizontal surface. A is set in motion with velocity while B is at rest. What is the distance moved by A relative to B before they move with the same velocity?



- 10. An elastic string of unstretched length L and force constant k is stretched by a small length x. It is further stretched by another small length y. The work done in the second stretching is
  - (a) 1/2 Ky2
- (b) 1/2 Ky(2x + y)
- (c) 1/2 K(x2 + y2) (d) 1/2 k(x + y)2
- A body is thrown vertically upwards from A, the top of the tower, reaches the ground in time 1. If it is thrown vertically downwards from A with

The same speed to flate freedy filter growth drint him tente it takes to reach the ground is given by

- 12. 0.5 mole of an ideal gas at constant temperature 27°C kept inside a cylinder of length L and crosssection area A closed by a massless piston.



The cylinder is attached with a conducting rod of length L, thouseredction directi(1/11/9) kn and dose other end is maintained at 0°C. If piston is moved such that rate of heat flow through the conducing rod is constant then velocity of piston when it is at height L/2 from the bottom of cylinder is: [Neglect any kind of heat loss from system ]

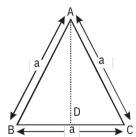
- (a)  $c = \frac{k \ddot{o}}{e^2 R^2 \dot{\sigma}} \dot{m} / sec$  (b)  $c = \frac{k \ddot{o}}{10 R^2 \dot{\sigma}} \dot{m} / sec$

field B with its plane perpendicular to the field. The sides of the loop start shrinking at a constant rate a. The induced emf in the loop at an instant when its side is ' $\alpha$ ' is

- (a)  $2\alpha aB$  (b)  $\alpha 2aB$  (c)  $2\alpha 2aB$  (d)  $\alpha aB$ The beam of light has three wavelengths 4144Å,4972Å and 6216 Å with a total intensity of 3.6 × 10-3 Wm2 equally distributed amongst the three wavelengths. The beam falls normally on the area 1 cm2 of a clean metallic surface of work function 2.3 eV. Assume that there is no loss of light by reflection and that each energetically capable photon ejects one electron. Calculate the number of photoelectrons liberated in 2s.
  - (a)  $2 \times 109$
- (b) 1.075 × 1012
- (c) 9 × 108
- (d)  $3.75 \times 106$
- A square gate of size 1 m × 1m is hinged at its mid-point. A fluid of density r fills the space to the left of the gate. The force F required to hold the gate stationary is

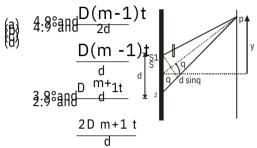


- 16. When 0.50 Å X-rays strike a material, the photoelectrons from the k shell are observed to move in a circle of radius 23 mm in a magnetic field of 2 × 10–2 tesla acting perpendicularly to
  - the direction of emission of photoelectrons. What is the binding energy of k-shell electrons? (a) (c) (d) keV
- 17. In CE 9transistor amplifier, 5. The audio signal voltage across the collector residence of 2 kW is 2 V. If the base resistance is 1kW and the current amplification of the transistor is 100, the input signal voltage is
  - (a) 2 mV (b) 3 mV (c) 10 mV(d)0.1 mV
- 18. At the corners of an equilateral triangle of side a (1 metre), three point charges are placed (each of 0.1 C). If this system is supplied energy at the rate of 1 kw, then calculate the time required to move one of the mid-point of the line joining the other two.



- (a) 50 h (b)60 h (c) 48 h (d)54 h
- 19. A vessel of volume 20L contains a mixture of hydrogen and helium at temperature of 27°C and pressure 2 atm. The mass of mixture is 5g. Assuming the gases to be ideal, the ratio of mass of hydrogen to that of helium in the given mixture will be
- (a) 1:2 (b)2:3 (c) 2:1 (d)2:5
  The resistance of a wire is R. It is bent at the middle by 180° and both the ends are twisted together to make a shorter wire. The resistance of the new wire is
- (a) 2R (b)R/2 (c) R/4 (d)R/821. In a YDSE, the light of wavelength l = 5000 Å is used, which emerges in phase from two slits a distance d =  $3 \times 10$ –7m apart. A transparent sheet

of thickness  $t = 1.5 \times 10-7m$  refractive index m = 1.17 is placed over one of the slits. what is the new angular position of the central maxima of the interference pattern, from the centre of the screen? Find the value of y.

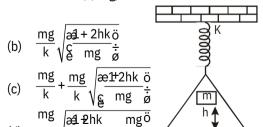


- 22. The position of a projectile launched from the origin at t = 0 is given by  $F = 40i^+ + 50j^-$  m at t = 2s. If the projectile was launched at an angle q from the horizontal, then q is (take g = 10 ms 2)
  - (a)  $\tan \frac{-12}{3}$
- (a)  $\tan^{-1}\frac{3}{2}$
- (c)  $\tan^{-1}\frac{7}{4}$
- tan -1\_4
- 23. Water is flowing on a horizontal fixed surface, such that its flow velocity varies with *y* (vertical direction) as

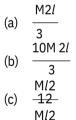
$$v = k_{\mathbf{Q}} \frac{2y^2}{\alpha^2} - \frac{y_3^3 \ddot{o}}{\alpha^2 \dot{\phi}}$$
 If coefficient of viscosity for

water is h, what will be shear stress between layers of water at  $y = \alpha$ .

- (a)  $\frac{hk}{a}$
- (b)  $\frac{h}{ka}$
- (c) ha
- (d) None of these
- 24. A load of mass m falls from a height h on to the scale pan hung from the spring as shown in the figure. If the spring constant is k and mass of the scale pan is zero and the mass m does not bounce relative to the pan, then the amplitude of vibration is (a) mg/d



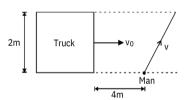
- 25. In an ore containing uranium, the ratio of U238 31. to Pb206 is 3. Calculate the age of the ore, assuming that all the lead present in the ore is the final stable product of U238. Take the halflife of U238 to be  $4.5 \times 109$  yr.
  - (a)  $1.6 \times 193 \text{ yr}$
- (b)  $1.5 \times 104 \text{ yr}$
- (c)  $1.867 \times 109 \text{ yr}$  (d)  $2 \times 105 \text{ yr}$
- 26. A direct current of 5A is superposed on an alternating current  $I = 10 \sin wt$  flowing through the wire. The effective value of the resulting current will be
  - (a) (15/2)A
- (b) 5√3A
- 55/A
- (d) 15 A
- 27. A planoconvex lens fits exactly into a planoconcave lens. Their plane surface are parall(a) 50 m (b)25 m(c) to each other. If the lenses are made of different  $A^2$  m wide truck is moving with a uniform speed materials of refractive indicates of the lenses are made of different  $A^2$  m wide truck is moving with a uniform speed  $A^2$  m with a uniform spe the lenses, then focal length of combination is
  - (c)  $\frac{R}{2(\mu \mu_2)}$  (d)  $\frac{R}{2} (\mu_1 + \mu_2)$
- 28. A thin rod of length 4l and mass 4m is bent at the points as shown in figure. What is the moment of inertia of the rod about the axis passes through point O and perpendicular to the plane of paper?



- \_24 (d)
- 29. One of the lines in the emission spectrum of Li2+ has the same wavelength as that of the 2nd line of Balmer series in hydrogen spectrum. The electronic transition corresponding to this line is n = 12 ® n = x. Find the value of x.
- (a) 8 (b) 6 (c) 7 (d) 5 Two particles X and Y having equal charges, after being accelerated through the same potential difference, enter a region of uniform magnetic field and describe circular paths of radii 1 and R2, respectively. The ratio of masses of X and Y is (a) (R/R)172

  - (c)  $(R/\bar{R})$ 2

- A glass capillary tube of internal radius r = 0.25mm is immersed in water. The top end of the tube projected by 2 cm above the surface of the water. At what angle does the liquid meet the tube? Surface tension of water = 0.7 N/m. (a) (c) A particle of mass) 2 on is projected at an
- angle 96 45 with the (td)riz 70 fal with a velocity
  - 202m/s. After 1s, explosion takes place and the particle is broken into two equal pieces. As result of explosion, one part comes to rest. The maximum height from the ground attained by other part is
  - 40 m (d)35 mv 0 = 8 m/s along a straight horizontal road. A pedestrain starts to cross the road with a uniform speed v when the truck is 4 m away from him. The minimum value of v so that he can cross the road safelv is



- (a) 2.62
- (b) 4.6 m/s
- (c) m/s
- (d) 1.414 m/s
- A new moving with speed v makesa head on collism/s with a hydrogen atom in ground state kept at rest. The minimum kinetic energy of the neutron for which inelastic collision takes place is
- (a) 10.2
- (b) 20.4
- (c) eV
- (d) eV
- Vertidal displacement of a Planek with a body of massay on it is varying according to law y = sin wt + 3coswt. The minimum value of w for which the mass just breaks off the Planck and the moment it occurs first after t = 0, are given by

(a) 
$$\sqrt{g/2}$$
,  $\frac{\sqrt{2}}{6} \frac{p}{\sqrt{g}}$  (b)  $\frac{g}{\sqrt{2}}$ ,  $\frac{2}{3} \sqrt{p/g}$   $\sqrt{g/2}$ ,  $\frac{p}{2} \sqrt{2/g}$   $\sqrt{2g}$ ,  $\sqrt{2g}$ ,  $\sqrt{g/3g}$ 

A parallel plate capacitor of capacitance C is connected to a battery and is charged to a potential difference V. Another capacitor of

capacitance 2C is similarly charge to a potential difference 2V. The charging battery is now disconnected and the capacitors are connected in parallel to each other in such a way that the positive terminal of one is connected to the negative terminal of the other. The final energy of the configuration is

(a) Zero

37. In the circuit shown below, the ac source has voltage  $V = 20 \cos(wt)$  volt with w = 2000 rad/s. The amplitude of the current will be nearest to

(a) 2A (b) 3.3A

(c)  $2/5\overline{A}$ 

(d)  $\sqrt{5}A$ 

 $6\Omega$ 

38. A constant voltage is applied between the two ends of a uniform metallic wire. Some heat is developed in it. The heat developed is doubled if both the length and the radius of the wire are halved.

both the length and the radius of the wire are doubled.

the radius of the wire is doubled.

the length of the wire is doubled.

- 39. The frequency of a sonometer wire is 100 Hz. When the weights producing the tensions are completely immersed in water, the frequency becomes 80 Hz and on immersing the weights in a certain liquid, the frequency becomes 60 Hz. The specific gravity of the liquid is
- (a) 1.42 (b)1.77 (c) 1.82 (d)1.2140. A long straight wire along the Z-axis carries a current I in the negative Z-direction. The magnetic vector field B at a point having coordinates (x, y) in the Z = 0 plane is

(a)  $\frac{m_0 I(y\hat{i}-)}{2^p(^2+y^2xj)}$  (b)  $\frac{m_0 I(x\hat{i}+y\hat{j})}{2p(x^2+y^2)}$  (c)  $\frac{m_0 I(x\hat{i}-y\hat{j})}{2p(x^2+y^2)}$  (d)  $\frac{m_0 I(x\hat{i}-y\hat{j})}{2p(x^2+y^2)}$ 

### PART - II: CHEMISTRY

Which of the following pollutants is main product of automobiles exhaust?

(a) CO

(b) CO<sub>2</sub>

(c) NO

(d) Hydrocarbons

The disease caused the high concentration of 42 hydrocarbon pollutants in atmosphere is/are

(a) silicosis

(b) TB

(c) cancer

(d) asthma

43. The element, with atomic number 118, will be

alkali

(b) noble gas

(c) lanthanide

(d) transition element

Which law of the thermodynamics helps in calculating the absolute entropies of substances at different various

tamparatukas?

(b) Second law

(c) Third law

(d) Zeroth law

The color of CoCl 3.5NH3.H2O is

(a) red

(b) orange

(c) orange - yellow (d) pink The metal present in vitamin B 12 is

(a) magnesium

(b) cobalt

(c) copper

(d) zinc

47. Cobalt (60) isotope is used in the treatment of:

(a) Heart diseases (b) Skin diseases

(c) Diabetes

(d) Cancer

48. Polymer used in bullet proof glass is

(a) Lexan

(b) PMMA

(c) Nomex

(d) Kevlar

What is the correct increasing order of Bronsted bases?

> ClO-<clo-3<clo-<clo-(a)

ClO->ClO-3>ClO->ClQ-

ClO-<ClO-<ClO-<ClO-

CIO->CIO-3>CIO-<CIO-(d)

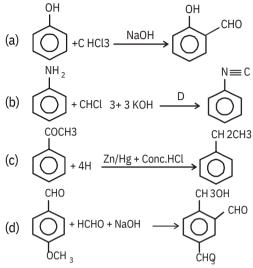
- The boiling point of alkyl halide are higher than those of corresponding alkanes because of
  - (a) dipole-dipole interaction
  - (b) dipole-induced dipole interaction

(c) H-bonding

(d) None of the above

- 51. Some salts containing two different metallic elements give test for only one of them in solution, such salts are
  - (a) double salts
- (b) normal salts
- (c) complex salts
- (d) None of these

52. The carbylamine reaction is



- Laughing gas is
  - (a) nitrogen pentoxide
  - (b) nitrous oxide
  - (c) nitrogen trioxide
  - (d) nitric oxide
- 54. The anthracene is purified by
  - (a) crystallisation
    - (b) filtration
  - (c) distillation
- (d) sublimation
- The common name of K[PtCl(h2 .C2H4)] is
  - potassium salt
- (b) Zeise's salt
- (c) complex salt
- (d) None of these
- 56 The by product of Solvay-ammonia process is (a) CaCC3 (b) NH3 (c) CaCl2 Semiconductor materials like Si and Ge are usually purified by
- (a) (cdistribilization of the followizagnis refinition g 57 (d) electrolytic refining baseliquation
- (a) PH <sup>3</sup>
- (b) AsH3 (c) NH3 (d) SbH3
- Ordinary glass is:
  - (a) Sodium silicate
- 59 (b) Calcium silicate
  - (c) Sodium and calcium silicate
- (d)Mixed salt of Na and Ca
- The prefix 1018 is 60
  - (d) nano (a) giga (b) kilo (c) exa Which of the following is the most basic oxide?
  - (d) Al2O3 (a) Sb2O3 (b) Bi2O3 (c) SeO2
- Which one of the following does not follow octate rule?
- (a) PF<sup>3</sup> (b) BF3 (c) CO2 (d) CCl4

- 63. Which of the following according to Le-Chatelier's principle is correct?
  - Increase in temperature favours the
  - reaction Increase endothermic
  - temperature favours the exothermic reaction Increase in pressure shifts the equilibrium in that side in which number of gaseous moles increases All of the above

(d)

The efficiency of fuel cell is given by the expression, h is

(a) 
$$h = -$$
 
$$\frac{nFE \text{ cell}}{DH}$$
(b)  $h \equiv -$  
$$\frac{nFE_{\text{ cell}}}{DS}$$
(d) 
$$\frac{nFE_{\text{ cell}}}{DA}$$

None of the above

- The mass of the substance deposited when one 65. Faraday of charge is passed through its solution is equal to
  - (a) relative equivalent weight
  - gram equivalent weight (b)
  - specific equivalent weight
  - (d) None of the above
- The unit of rate constant for reactions of second 66. order is
  - (a) L mol-1s-1
- (b)  $L-1 \mod s-1$
- (c) L mol s-1
- (d) s-1
- In a first order reaction with time the concentration of the reactant decreases
  - (a) linearly
- (b) exponentially
- (c) no change
- (d) None of these
- 68. The P−P−P angle in #molecule and S−S−S angle in **8** molecule is(in degree) respectively
  - (a) 60°, 107°
- (b) 107°, 60°
- (c) 40°, 60°
- (d) 60°, 40°
- The number of elements present in the d-block of the periodic table is
  - (a) 40
    - (b) 41
- (c) 45
- (d) 46
- 70. Which of the following represents hexadentate ligand?
  - (a) EDTA
- (b) DMG
- (c) Ethylenediamine(d) None of the above
- Which one of given elements shows maximum number of different oxidation states in its compounds?
  - (a) Am
- (b) Fm (c) La
- (d) Gd

58

72.	K 4[Fe(CN)6] is used in detecting.	DIRE	ECTIONS (Qs. 84-86): Fill in the blank.				
	(a) Fe3+ ion (b) Cu+ ion (c) Cu3+ ion (d) Fe2+ ion	84.	Freedom and equality are the rights of every human.				
73.	A spontaneous reaction is impossible if (a) (b) (b) (b) DH and DS are negative both (d) DH and DS are positive DH is Which (1) Which (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	85.	<ul> <li>(a) inalienable</li> <li>(b) inscrutable</li> <li>(c) incalculable</li> <li>(d) institutional</li> <li>The team was well trained and strong, but some how their was low.</li> </ul>				
74.	Hardiness-Op Weiter and Do 13 Hogative		(a) morale (d) moral (epling (d) consciousness				
75.	(a) Slaked lime (b) Plaster of Paris (c) Epsom (d) Hydrolith Graphite is a (b)	86.	His speech was disappointing: it all the major issues.  (a) projected (b) revealed (c) skirted (d) analysed				
	(a) molecular solid (d) covalent solid (c) ionic solid metallic solid	DIRE	ECTIONS (Qs. 87-89): Choose the word which				
76.	Which of the following ionic substances will be most effective in precipitating the sulphur sol?	is closest to the opposite in meaning of the underlined word in the sentence.					
	(a) KCl (b) BaCl <sub>2</sub> (c) Fe2(SO4)3 (d) Na3PO4	87.	Hydra is biologically believed to be immortal. (a) undying (b) perishable				
77.	Which of the following fluorides of xenon is impossible? (a) XeF <sup>2</sup> (b) XeF3 (c) XeF4 (d) XeF6	88.	(c) ancient (d) eternal The Gupta rulers <u>patronised</u> all cultural activities and thus Gupta period was called the golden era in Indian History.				
78.	Thomas slag is (a) Ca 3 (PO4) 2		(a) criticised (b) rejected (c) opposed (d) spurned				
	(b) CaSiO 3 (c) Mixture of (a) and (b) (d) FeSiO 3	89.	The General Manager is quete tactful and handles the workers union very effectively.				
79.	A sequence of how many nucleotides in messenger RNA makes a codon for an amino		(a) incautious (b) discreet (c) strict (d) disciplned				
	acid? (a) Three (b) Four (c) One (d) Two		ECTIONs (Qs. 90-92): In each ot the following stions, out of the four alternatives, choose the				
80.	Which of the following molecule/ion has all the three types of bonds, electrovalent, covalent	one v	which can be substituted for the given words/ ence.				
	and co-ordinate: (a) HCl (b) NH + <sub>4</sub> (c) Cl- (d) H 2O2	90.	A person who does not believe in any religion (a) Philatelist (b) Rationalist (c) Atheist (d) Pagan				
F	PART - III (A): ENGLISH PROFICIENCY	91.	A person who believes that pleasure is the chief good				
best	CTIONS (Qs. 81-83): Choose the word which expreses the meaning of the underlined word in entence.	92.	, , , , , , , , , , , , , , , , , , , ,				
81.	Decay is an <u>immutable</u> factor of human life.  (a) important  (b) unique		(a) caretaker (b) warden (c) supervisor (d) curator				
00	(c) unchangeable (d) awful		ECTIONS (Qs. 93-95): Choose the order of the				
82.	It was an <u>ignominious</u> defect for the team. (a) shameful (d) admirable		ences marked A, B, C, D and E to form a logical graph.				
83.	(c) unaccountable (d) worthy The attitude of western countries towards the third world countries is rather <u>callous</u> to say the least.  (a) cursed (d) unkend	93.	<ul> <li>A. Tasty and healthy food can help you bring out their best.</li> <li>C. One minute they are toddlers and next you see them in their next adventure.</li> </ul>				
	(c) unfeeling (d) passive		Your young ones seem to be growing so fast.				

- D. Being their loving custodians, you always
- E. want to see them doing well.

  Their eye sparkle with curiosity and

Their eye sparkle with curiosity and endless questions on their tongues.

Codes (a)

DBCEA (c) CBEDA (b) CADEB (d) ECABD

- 94. A. It is hoping that overseas friends will bring in big money and lift the morale of the people. But a lot needs to be done to kick
  - B. start industrial revival. People had big
  - hopes from the new gover n men t. So far
  - D. government has only given an incremental push to existing policies and programmes.
    Government is to go for big time reforms, which it promised.

E.

Codes (a)

BCDAE (c)

(b) EADCB

DABCE

- (d) CDEAB
- A: Forecasting the weather has always been a defficult business.
  - B: During a period of drought, steams and rivers dried up, the cattle died from thirst and were ruined.
  - C :Many different things affect the weather and we have to study them carefully to make accurate forecast.
  - D :Ancient egyptians had no need of weather in the Nille valley hardly ever changes. In
  - E: early times, when there were no instruments, such as their mometer or the barometer, a man looked for tell tale signs in the sky.

(a) ABDCE (c)

(b) EDCBA (d) BDCAE

ACBDE

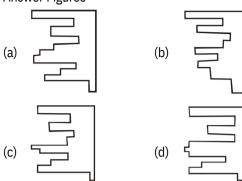
### PART - III (B): LOGICAL REASONING

96. Choose the correct answer figure which will make a complete square on joining with the problem figure

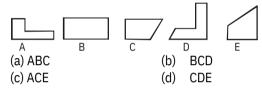
Problem figure



**Answer Figures** 

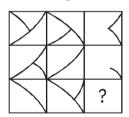


97. In the following question, five figures are given. Out of them, find the three figures that can be joined to form square.

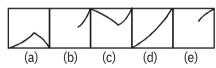


98. Choose the answer figure which completes the problem figure matrix.

**Problem Figures** 



**Answer Figures** 



99. What is the opposite of 3, if four different positions of dice are as shown below:



5 2 (ii)



(d) 2

(a) 6

6 (b) 4

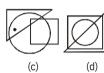
(c) 1

100. In the following questions, one or more dots are placed in the figure marked as (A). The figure is followed by four alternatives marked as (a), (b), (c) and (d). One out of these four options contains region(s) common to the circle, square, triangle, similar to that marked by the dot in figure (A).

Problem Figure







- 101. Complete the series by replaing '? mark G4T, J9R, M20P, P43N, S90L
  - (a) S90L
- (b)V185J(c) M20P
- (d)P43N
- 102. Neeraj starts walking towards South. After walking 15 m, he turns towards North. After walking 20 m, he turns towards East and walks 10 m. He then turns towards South and walks 5 m. How far is he from his original position and in which direction?
  - (a) 10 m, East (c)10 m, West
- (b) 10 m, South-East (d)10 m, North-East
- 103. The average age of 8 men is increased by 2 yr when one of them whose age is 20 yr is replaced by a new man. What is the age of the new man
  - (a) 28 yr (b) 36 yr (c) 34 yr
- 104. Shikha is mother-in-law of Ekta who is sister-inlaw of Ankit. Pankaj is father of Sanjay, the only brother of Ankit. How is Shikha related to Ankit?
  - (a) Mother-in-law
- (b) Aunt
- (c) Wife
- (d) Mother
- 105. In a gueue of children, Arun is fifth from the left and Suresh is sixth from the right. When they interchange their places among themselves, Arun becomes thirteenth from the left. Then, what will be Suresh's position from the right?
  - (a) 8th
- (b) 14th (c) 15th
- (d) 16th

## PART - IV: MATHEMATICS

106. 
$$\lim_{x^{\circledast} ¥} \frac{\dot{\mathbf{q}}^{2x} x e^{x^2} dx}{e^{4x2}} \text{ equals}$$

- (a) 0
- (b) ¥
- (c) 2
- 107. If w is the complex cube root of unity, then the

æ 1+3+9+27+ value of w+wè2832128 ø is

- (a) -1(b)1
- - (c)
- (d)i
- 108. The root of the equation

2(1+i)x2-4(2-i)x-5-3i=0 which has greater modulus is

- (d) none
- 109. The value of  $\frac{3}{4} + \frac{1}{5} + \frac{6}{3} + \dots$  upto n terms is
  - (a)  $n \frac{4n}{3} \frac{1}{3} = 6$  (b)  $n + \frac{4-n}{3} \frac{1}{3}$
  - (c)  $n + \frac{4^n}{3} \frac{1}{3}$
- (d)  $n \frac{4-n}{2} + \frac{1}{2}$
- 110. The period of tan 3q is
  - (a) p

(b) 3p/4

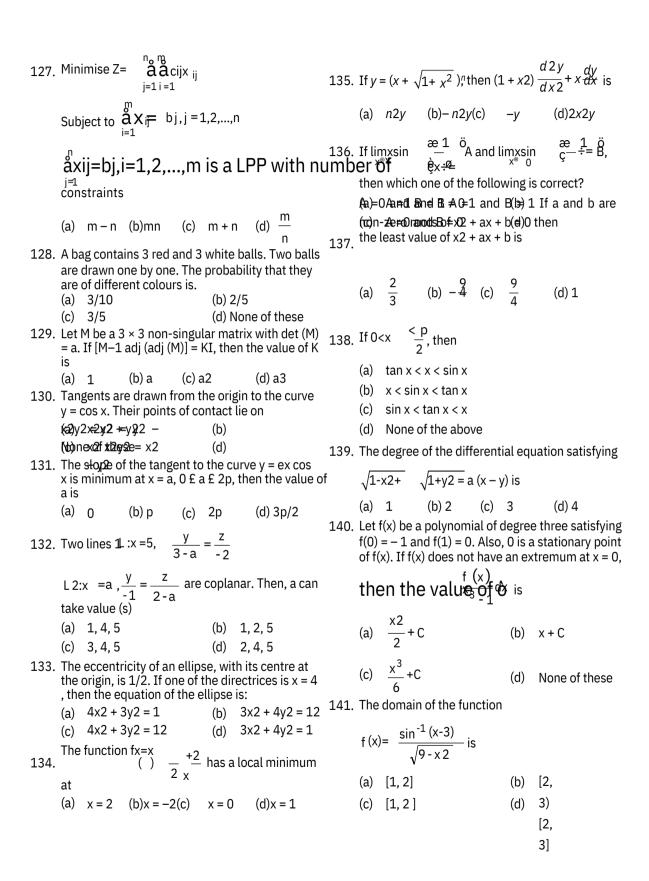
(c) p/2

- (d) None of these
- 111. If a function f(x) is given by

$$f(x) = \frac{x}{1+x} + \frac{x}{(x+1)(2x+1)} + \frac{x}{(2x+1)^{x} 3x+1} + \dots$$
+ then at x = 0, f(x)

- (a) has no limit
- (b) is not continuous
- (c) is continuous but not differentiable
- (d) is differentiable
- 112. If g is the inverse of function f and  $f \phi(x) = \sin x$ , then gc(x) is equal to
  - (a)  $cosec \{g(x)\}$
- (b)  $\sin\{g(x)\}$
- None of these

113.	3. A bag contains (2n + 1) coins. It is known that n of these coins have a head on both sides, whereas the remaining (n + 1) coins are fair. A			119	Let a, b and c be three vectors satisfying a $\times$ b = $(a \times c)$ , $ a  =  c  = 1$ , $ b  = 4$ and $ b \times c  = \sqrt[4]{15}$ . If b – $2c = la$ , then l equals						
114.	coin is picked up at random from the bag and tossed. If the probability that the toss results in a head is $31/42$ , then n is equal to (a) 10 (b) 11 (c) 12 (d) 13  If f (x) is a differential function, then the solution of the differential equation dy + {y f¢(x) - f (x) f¢ (x)}dx = 0, is					(a) 1 (b)-1 (c) 2 (d)-4  The total number of 4-digit numbers in which the digits are in descending order, is  (a) 10C × 4! (b) 10C  (c) (d)					
						(0)	10! 4!			(4)	None of these
	(a) $y = \{f(x) - \} + Ce^{-f(x)}$				121.	The line which is parallel to X-axis and crosses					
						the curve y= $\sqrt{x}$ at an angle of 45°, is					
	$_{(c)}^{(b)}$ $yf(x)=\{f(x)\}2c$			(a)	$x = \frac{1}{4}$			(b)	$y = \frac{1}{4}$		
	(d)	$fye(x)=f(\theta)f(x)+C$	:				1				
		fye(x)=f(e)f(x)+C $y-f(x)=f(e)f(x)$				. ,	y= <del>2</del>				y = 1
115.	The	area of the region R = {( £ 1} is		x  £  y  and x2	122.	are 1	.0 and	9 units, i	espect	ively. I	o larger sides If the angles are side can be
	(a)	$\frac{3p}{8}$ sq units	(b)	$\frac{5p}{8}$ sq units			5±√6 £ofthe	se		(b) (d)	3.₹
	(c)	$\frac{p}{2}$ sq units	(d)	$\frac{p}{8}$ sq unit	123.			etic mea ncies 1,			0, 1, 2,, n C įs
116.	Universal set, $U = \{x \mid x5 - 6x4 + 11x3 - 6x2 = 0\}$ $A = \{x \mid x2 - 5x + 6 = 0\}$ $B = \{x \mid x2 - 3x + 2 = 0\}$					(a) The	n mean ervati	(b) $\frac{2n}{n}$	(c)	n+1 ation	(d) $\frac{n}{2}$ of a set of n t a point c is
	What is $(A \ C B)'$ equal to? (a) $\{1, 3\}$ (b) $\{1, 2, 3\}$					defi	<sup>nគ្ព</sup> a(xi	Ò			
		{0, 1, 3}		{1, 2, 3} {0, 1, 2, 3}			ı=1		viotion	a abau	ut 2 and 2 are
117.	If co	s-1x-co- s1 $\frac{y}{2}$ = a,				18 ai	nd 10 ı is set c	espectives of observ	ely, the	e stanc	ut – 2 and 2 are dard deviation
	then $42x - 4xy \cos a + 2y$ is equal to						3 alof the			(b) (d)	
	(a) (c)	2 sin 2a 4 sin2a	(b) (d)	4 – 4 sin2a	125.	Let S	be the	focus o		ırabola	a y2 = 8x and PQ e x2 + y2 - 2x -
118.	If —	$\frac{x + e5x}{e3^x} = a_0 + a1x + ax2$	+a 3	3x <sup>3</sup> + then		4y = is					e area of DPQS
	the value of 2a 1+23a3+25a5+ is					/ \	4 sq u				3 sq units
	. ,	e2 + e-2 e4 + e-4	(b) (d)	e4 – e–4 0	126.				roots of		8 sq units quation ex–1 + x
						(a)	1	(b) 2	(c)	3	(d) 4



142.	If the lines 1x to divisent; then the points (p1, q1), q (p2, q2) and (p3, q3) (a) are collinear (b) form an equilateral triangle (c) form a scalene triangle (d) form a right angled triangle	<ul><li>147.</li><li>148.</li></ul>	A line makes the same angle with each of the X and Z-axes. If the angle, which it makes with Y-axis, is such that sin2 b = 3sin2 q, then cos2 q equals (d) 2/3  (a) Ipjina binamiasdistribution n = 4, P(X = 0) = then P(X = 4) equals 16 81,
144.	Area of the circle in which a chord of length $\sqrt{2}$ makes an angle p/2 at the centre, is (a) p/2 sq units (b) 2p sq units (c) p sq units (d) p/4 sq units  If $\frac{\cos A}{\cos B} = n$ , $\frac{\sin A}{\sin B} = m$ , then the value of $(m2 - n2)$ $\sin 2B$ is (a) $1 + n2$ (b) $1 - n2$ (c) $n2$ (d) $-n2$ If complex number z 1, z2 and 0 are vertices of equilateral triangle, then $z_1^2 + z_2^2 - z_1^2 z_2^2$ is equal		(a) $\frac{1}{16}$ (b) $\frac{1}{}$ (c) $\frac{1}{27}$ (d) $\frac{1}{8}$ Let f: R $^{\circ}$ R be a function such that  f (x + y) = f (x) + f (y), "x, y Î R  If f (x) is differentiable at x = 0, then which one of the following is incorrect?  (a) f(x) is continuous, "xÎR  (b) f¢(x) is constant, "xÎR  (c) f(x) is differentiable, "xÎR  (d) f(x) is differentiable only in a finite interval containing zero.
146.	to (a) 0 (b) $z1-z2(c)$ $z1+z2$ (d)1 If $r = \{(x, y)   x2 + y2 = 1; x, y \hat{1} R\}$ . Then, r is (a) reflexive (b) symmetric (c) transitive (d) anti-symmetric	150.	If binomial coefficients of three consecutive terms of $(1 + x)n$ are in HP, then the maximum value of n is  (a) 1 (b) 2  (c) 0 (d) None of these

# SOLUTIONS

# PART - I: PHYSICS

The escape velocity from earth is given by

ve = 2/gRe... (i)

The orbital velocity of a satellite revolving around earth is given by

$$v0 = \frac{\sqrt{GMe}}{(Re + h)}$$

where, Me = mass of earth, Re = radius of earth, h = height of satellite from surface of earth.

By the relation  $GM \in gR2_{\rho}$ 

So, 
$$v0 = \frac{\sqrt{gR_e^2}}{(Re+h)}$$
 ... (ii)

Dividing equation (i) by (ii), we get

$$\frac{v_e}{v_0} = \frac{\sqrt{2(Re+h)}}{\binom{R_e}{ve}}$$

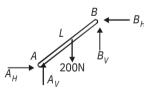
Given,  $v0 = \frac{ve}{2}$ 

$$\frac{2v_e}{v_e} = \frac{\sqrt{2(R_e + h)}}{R_e}$$

Squaring on both side, we get

$$4 = \frac{2(Re + h)}{Re}$$

or Re + h = 2Re i.e., h = Re Consider FBD of structure. 2.

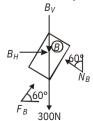


Applying equilibrium equations,

$$Av + Bv = 200 \text{ N} ... (i)$$

*AH* = *BH* ... (ii)

From FBD of block B,



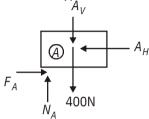
 $B + BF \cos 60^\circ - NB \sin 60^\circ = 0$ 

 $B_0 \cos 60^\circ - BV - 300 + FB \sin 60^\circ = 0$ 

**B** = 0.25 NB

... (iii) H = 0.74 NB = 0

-B + 0.71 NB = 300- & + v., - ... FBD of block A



FA - AH = 0

NA - AV = 400... (v)

 $FA = \mu A NA$ 

 $\setminus \mu ANA - AH = 0$ ... (vi)

On solving above equations, we get

 $NA = 650 \text{ N}, FA = 260 \text{ N}, FA = \mu A N A$ 

(a) Let v = speed of sound and vS = speed of 3. tuning forks. Apparent frequency of fork moving towards the observer is

Apparent frequency of the fork moving away from the observer is

$$n_2 = \frac{æ}{c} \frac{v}{v} \ddot{o}$$

 $\stackrel{\text{\'e}}{\text{V}} + \stackrel{\text{V}}{\text{V}} = 0$ If f is the number of beats heard per second.

then f = n1 - n2

b f 
$$\frac{\text{ev}}{\text{ev}^2 - \text{vs}} \stackrel{\ddot{\text{o}}}{=} \frac{\text{v}}{\text{ev}^2 - \text{vs}} \stackrel{\ddot{\text{o}}}{=} \frac{\text{v}}{\text{ev}^2 + \text{vs}} \stackrel{\ddot{\text{o}}}{=} \frac{\text{v}}{\text{vs}} \stackrel{\ddot{\text{o}}}{=} \frac{\text{v}}{\text{vs}} \stackrel{\ddot{\text{o}}}{=} \frac{\text{v}}{\text{vs}} \stackrel{\ddot{\text{o}}}{=} \frac{\text{v}}{\text{vs}} \stackrel{\ddot{\text{o}}}{=} \frac{\text{vs}}{\text{vs}} \stackrel{\ddot{\text{o}}}{=} \frac{\text{vs$$

$$v = \begin{cases} v & v = 1 \\ v & v = 1 \end{cases}$$

$$v = \begin{cases} v & v = 1 \\ v & v = 1 \end{cases}$$

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$$v = \begin{cases} v & v = 1 \\ v & v = 1 \end{cases}$$

$$v = \begin{cases} v & v = 1 \\ v & v = 1 \end{cases}$$

$$=\frac{\text{fv}}{2\text{n}}$$

putting 
$$v = 340 \text{ m/s}$$
,  $f = 3$ ,  $n = 340 \text{ Hz}$  we get,

$$v_s = \frac{340'3}{3'340} = 1.5 \text{ m/s}$$

4. (a) The displacement of the particle is given by:

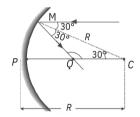
$$x = A \sin(-2wt+)$$
  $B \sin^2 wt$   
=  $-A \sin^2 wt + \frac{B}{2} (1 - \cos^2 wt)$   
=  $-(A \sin^2 wt + \frac{B}{2} \cos^2 wt) + \frac{B}{2}$ 

This motion represents SHM with an

amplitude: 
$$\sqrt{A2 + \frac{B^2}{4}}$$
, and mean position

 $\frac{B}{2}$ .

5. (d) From similar triangles,



$$\frac{QC}{\sin 30} = \frac{R}{\sin 120^{\circ}}$$
or
$$\frac{QC}{\sin 30^{\circ}} = \frac{R}{\sin 30^{\circ}} = \frac{R}{\sqrt{3}}$$

Thus

$$PQ = PC - QC = R \frac{-R}{\sqrt{3}} = R \frac{\approx}{6} \frac{1}{\sqrt{3}} \frac{\ddot{o}}{\dot{o}}$$

6. (c) Using Gauss's law, we have

$$\tilde{N}_{0}^{b}E.dA_{10}^{1}\tilde{O}(rdv)$$

or 
$$E'4pR^2 = \stackrel{\text{def}}{\stackrel{\text{def}}{\text{eff}}} \stackrel{\text{def}}{\stackrel{\text{def}}{\text{eff}}} \stackrel{\text{def}}{\text{eff}} \stackrel{\text{def}}{\text{eff}}$$

$$V = \frac{kR^{(\alpha+1)}}{10(\alpha+3)}$$

G iven, 
$$E2 = \frac{E_1}{8}$$

or 
$$\frac{k \mathop{\mathbb{C}}_{2}^{R} \ddot{o} a^{\frac{1}{4}}}{\mathop{\hat{1}}_{0}^{R} (a^{+3})} = \frac{1}{8} \frac{kR(a^{+1})}{\widehat{10}(a+3)}$$

$$\frac{1}{2} \frac{1}{a+1} = \frac{1}{8}$$
or 
$$a = 2.$$

7. (a) As we know F = mv2 qvB = r mv

And  $k = \frac{1}{2} mv2$ 

\ 
$$mv = \sqrt{2km}$$

$$r = \frac{mv}{qB} = \frac{\sqrt{2km}}{qB}$$

 $r = \sqrt{k} \text{ or } r = c1/2 \text{ (c is a constant)}$ 

$$\frac{dr}{dr} = c \frac{dk^{1/2}}{dr}$$
 or  $\frac{\sum_{r=0}^{Dk} k}{\sum_{r=0}^{Dk} k} = 2\sqrt{k}$ 

or 
$$\frac{Dr}{r} = \frac{cDk}{2\sqrt{kc} k\sqrt{}}$$

Therefore percentage changes in radius of path,

$$\frac{Dr}{r}$$
,  $\frac{Dk}{100} = \frac{Dk}{2k}$ ,  $\frac{100}{100} = \frac{2}{100}$ 

8. (d) Given: fringe with b = 0.03 cm, D = 1 m = 100 cm

Distance between images of the source = 0.8 cm.

Image distance v = 80 cm

Object distance = u

Using mirror formula,

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f} \Rightarrow \frac{1}{60} + \frac{1}{u} = \frac{1}{16}$$

Magnification, 
$$m = \frac{v}{u} = \frac{8}{0} = 4$$

Magnification = i d stances between images of slits distance between slits

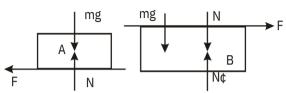
$$=\frac{0.8}{d} = \frac{0.8}{d} = 4$$
 = 4.2 cm

Fringe width 
$$b = \frac{Dl}{d}$$

or, b = 
$$\frac{100l}{0.2}$$
 = 0.03 '10-2

Therefore, wavelength of light used l = 6000 11. (c)

(d) For the blocks A and B FBD as shown 9. bel ow



Equations of motion

$$a_A = \frac{F}{M}$$
 (in x direction)  
 $a_B = \frac{F}{M}$  (in X direction)

Relative acceleration, of A w.r.t. B,

$$aA,B = aA - aB = -\frac{F}{m} - \frac{F}{M}$$

=-æç 
$$\frac{M + m}{F} \ddot{o}$$
 (along – x direction)

Initial relative velocity of A w.r.t. B.

uAB = v0

using equation v2 = u2 + 2as

$$0=v2_{\bar{0}} - \frac{2(Fm+MS)}{Mm} + S = \frac{Mmv^{2}}{2F(m+M)}$$

i.e., Distance moved by A relative to B

$$S_{AB} = \frac{Mmv_{\theta}^2}{2F(m \cdot M)}$$

10. (b) In the string elastic force is conservative in n ature.

Work done by elastic force of string,

$$W = -(UF - Ui) = Ui - UF$$
.

Therefore, the work done against elastic for ce

$$W_{\text{external}} = -W = \frac{ky}{2}(2x + y)$$

Let the body is projected vertically upwards from A with a speed u0.

Using equation, S= ut 
$$\frac{+1}{2}$$
at2

For case (1) – h = 
$$u_{0.1}$$
  $\frac{1}{2}$   $gt2$  ...(1)

For case (2) – h = 
$$u0t2 - gt_1^2$$
 ...(2)

Subtracting eq (2) from (1), we get

$$0 = u \cdot 0(t2 + ) \pm \frac{1}{2}g(t22 - t)$$

$$\Rightarrow 0 = \frac{1}{2}g(1-t2)$$
 ...(3)

Putting the value of u0 in eq (2), we get

$$^{-h=-\underset{e}{\overset{}{\underset{\rightarrow}}}\underset{e}{\overset{}{\underset{\rightarrow}}}\underset{e}{\overset{}{\underset{\rightarrow}}}\underset{e}{\overset{}{\underset{\rightarrow}}}g(t1\ t_2)t^2-\underset{e}{\overset{}{\underset{\rightarrow}}}\underset{e}{\overset{}{\underset{\rightarrow}}}\underset{e}{\overset{}{\underset{\rightarrow}}}gt_2^2}$$

$$h = (\frac{1}{2}) t. (4)$$

For case 3, u0 = 0, t = ?

þ jgt2

Comparing eq. (4) and (5), we get

$$\frac{1}{2}gt2=1gt1t2 \setminus t = \sqrt{t1t_2}$$

DQ = DW =work done per unit time = 12. (c) Dt

$$\frac{dW}{dt} = P \frac{dV}{dt} = k \frac{aq}{L}, P = \frac{nRT}{V}$$

$$\Rightarrow \frac{0.5R(300)}{V}A.\frac{dl}{dt} = \frac{k\alpha q}{L}$$

$$\Rightarrow v = \frac{k\alpha}{R} \stackrel{\text{e}}{\in} \frac{27}{300} \stackrel{\text{o}}{\rightleftharpoons} = \frac{k}{100R}$$

13. (a) At any time t, the side of the square  $\alpha = (\alpha_0)$ - a t), where  $\alpha 0$  = side at t = 0.

At this instant, flux through the square:

$$f = BA \cos 0^\circ = B (\alpha + \alpha t)^2$$

\ emf induced 
$$F = -\frac{at}{dt}$$

$$E = -B.2 (\alpha 0 - a t) (0 - a) = +2a\alpha B$$

14. (b) As we know, threshold wavelength

$$\begin{array}{c} {}_{\text{Pl}} = {}_{0} & \frac{(6.63\ \ 10\ \ 34)\ \ 3\ \ 100\ \ 3}{2.3\ \ 1.6\ \ 10\ \ 19)} {}^{3} {}^{1} {}^{1} {}^{0} {}^{0} {}^{8} \\ {}^{1} {}^{0} = {}^{5} {}^{4} {}^{0} {}^{4} {}^{1} {}^{0} {}^{-7} {}^{m} {}^{-7$$

Hence, wavelength 4144 Å and 4972 Å will emit electron from the metal surface.

For each wavelength energy incident on the surface per unit time

= intensity of each × area of the surface wavelength

$$=\frac{3.6'10-3}{3}'(1cm^2)=1.2'10-7$$
joule

Therefore, energy incident on the surface for each wavelength in 2s

$$E = (1.2 \times 10 - 7) \times 2 = 2.4 \times 10 - 7 J$$

Number of photons n1 due to wavelength

$$n1 = \frac{\left(2.4 \, 10^{-7}\right) \left(144 \, 10^{-10}\right)}{\left(6.63 \, 10 \, 34\right) \left(10^{8}\right)} = 0.5 \, 10^{12}$$

Number of photons n 2 due to the wavelength 4972 Å

$$n_2 = \frac{\left(2.4 \, 10^{-7}\right) \left(972 \, 10^{-10}\right)}{\left(6.63 \, 10 - 34\right) \left(10^{-8}\right)} = 0.572 \, 10^{12}$$

Therefore total number of photoelectrons liberated in 2s.

$$N = n_1 + n_2$$
  
= 0.5 10 \frac{1}{2} \quad 0.575 \lefta 10^{12}  
= 1.075 \lefta 0.52

15. (c) The net force acting on the gate element of width dy at a depth y from the surface of the fluid, is

Torque about the hinge is

dt= pgydy 
$$\stackrel{\circ}{e} \stackrel{\circ}{2} - y \stackrel{\circ}{o} \stackrel{\circ}{d} y$$

Net torque experienced by the gate is

tnet =  $\stackrel{\circ}{O}$ lt + F  $\stackrel{\circ}{2}$ 

=

r gydy  $\stackrel{\circ}{e} \stackrel{\circ}{2} - y \stackrel{\circ}{o} + F \stackrel{\circ}{2} = 0$ 

PF =  $\frac{r g}{6}$ 

i.e., The force F required to hold the gate

16. (b)

$$F = qvB = m \frac{v}{R} \Rightarrow v = \frac{q}{m}BR$$

The kinetic energy of the photoelectron

$$= \frac{1}{2} \text{mv2} = \frac{1}{2} \frac{e^2 B R^2}{2 m}$$

$$= \frac{1}{2} (1.6) (0) 10^{-2} (23'10'^3) 2$$

$$= \frac{1}{2} (9.1'10^{-31})$$

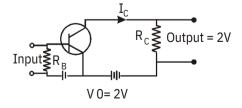
= 
$$2.97 \times 10^{15} \text{ J}$$
  
=  $\frac{2.97 \cdot 10^{-15}}{1.6 \cdot 10^{-19}}$  = 18.36 keV

Energy of the incident photon  $\frac{=hc}{L}$ 

$$=\frac{12.}{4}$$
 = 24.8keV

Therefore, Binding energy = 24.8 - 18.6 = 6.გkeV

17. (c) Given: Voltage across the collector V0 = 2 WycBlactor resistance, R = 2 × 103 1 × 10 ₩; Input signal resistance R = voltage, Vi = ?



$$V0 = ICRC = 2$$

$$I_C = \frac{2}{2'103} = 10-3A$$

Current gain a =  $\frac{IC}{IB}$  =100

$$b I_B = \frac{I_C}{100} = \frac{10-3}{100} = 10^{-5} A$$

$$V = RI^{BB}$$
  $V_i = 1 \times 10^3 \times 10^{-5}$   
 $V_i = 10 - 2V$   $V_i = 10$  mV

18. (a) Initial potential energy of the system

$$= \frac{1}{4_{pe0}} \frac{\acute{e}q2}{\ddot{e}a} + \frac{q2}{a} + \frac{q2}{a} \frac{\dot{u}}{\dot{u}} = \frac{1}{4_{pe0}} \frac{\cancel{e}^3 q2\ddot{o}}{\dot{e}^a} \div \frac{2}{a} \frac{\dot{u}}{\dot{u}} = \frac{1}{4_{pe0}} \frac{\cancel{e}^3 q2\ddot{o}}{\dot{e}^a} \div \frac{\dot{e}^3 q2\ddot{o}}{\dot{e}^3 q2\ddot{o}} \div \frac{\ddot{e}^3 q2\ddot{o}}{\dot{e}^3 q2\ddot{o}} \div \frac{\ddot{e}^3 q2\ddot{o}}{\dot{e}^3 q2\ddot{o}} \div \frac{\ddot{e}^3 q2\ddot{o}}{\ddot{e}^3 q2\ddot{o}}$$

Let charge at A is moved to mid-point O, Then final potential energy of thhe system

Uf = 
$$\frac{1}{4^{\text{pe}0}} \stackrel{\text{\'e}}{\stackrel{\text{\'e}}{\stackrel{\text{c}}}{\stackrel{\text{c}}}{\stackrel{\text{c}}{\stackrel{\text{c}}}{\stackrel{\text{c}}}{\stackrel{\text{c}}}{\stackrel{\text{c}}}{\stackrel{\text{c}}}{\stackrel{\text{c}}}{\stackrel{\text{c}}}}\stackrel{\text{c}}{\stackrel{\text{c}}}}\stackrel{\text{c}}{\stackrel{\text{c}}}}\stackrel{\text{c}}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}}\stackrel{\text{c}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel{\text{c}}}\stackrel$$

Work done =  $U \xi$ -  $Ui = 18 \times 107$ 

Also, energy supplied per sec = 1000 J (given)

Time required to move one of the mid-point of the line joining the other two

$$t = \frac{18'107}{1000} = 18'10s = 50h$$

19. (d) Let there are n1 moles of hydrogen and n2 moles of helium in the given mixture. As Pv = nRT

Then the pressure of the mixture

$$P = \frac{n1RT}{V} + \frac{n2RT}{V} = (n_1 + n_2)RT$$

þ

$$2'101.3'103 = (n_1 + n_2)' \frac{(8.3300)}{2010-3}$$

or

$$(n_1 + n_2) = \frac{2^{101.3'10'20'10-3}}{(8.3(300))}$$

or, n1 + n2 = 1.62 ... (1) The mass of the mixture is (in grams)

$$n1 \times 2 + n2 \times 4 = 5$$

 $(n1 \triangleright 2n2) = 2.5$  .... (2) Solving the eqns. (1) and (2), we get n1 = 0.74 and n2 = 0.88

Hence, 
$$\frac{\text{mH}}{\text{mHe}} = \frac{0.74'2}{0.88'4} = \frac{=1.48=2}{3.52}$$

20. (c) Resistance of wire () = rl

If wire is bent in the middle then

$$l \neq \frac{l}{2}, A = 2A$$

\ New resistance, R¢ =  $r \frac{l¢}{A¢} = \frac{r \frac{l}{2}}{2A} = \frac{rl}{4A} = \frac{R}{4}$ .

21. (b) The path difference when transparent sheet is introduced Dx = (m-1)t

If the central maxima occupies position of nth fringe, then (m-1)t = n l = d sin q

$$\Rightarrow \sin q = \frac{(m-1)t}{d} = \frac{(1.17-1)^{\cdot}1.5 \cdot 10^{-7}}{3 \cdot 10^{-7}} = 0.085$$

Therefore, angular position of central maxima

$$q = \sin^{-1}(0.085) = 4.88^{\circ} \times 4.9$$

For small angles, sin q » q » tan q

$$\Rightarrow$$
  $\tan q = \frac{y}{D}$ 

$$\frac{y}{D} = \frac{(m-1)t}{d}$$
  $y = \frac{D(m-1)t}{d}$ 

22. (c) From question,

Horizontal velocity (initial),

$$u_X = \frac{40}{2} = 20 \text{m/s}$$

Vertical velocity (initial),  $50 = uyt + \frac{1}{2} gt2$ 

$$\Rightarrow uy \times 2 + \frac{1}{2} (-10) \times 4$$

or, 
$$50 = 2uy - 20$$

or, 
$$uy = \frac{70}{2} = 35 \text{m/s}$$

$$\tan q = \frac{u_y}{u_x} = \frac{3}{5} = \frac{7}{4}$$

$$\Rightarrow$$
 Angle q =  $\tan_0^{2} \frac{7}{4}$ 

23. (a) Newton's law of viscosity, 
$$F = hA \frac{dv}{dy}$$

Stress = 
$$\frac{F}{A}$$
 =  $h \frac{\partial dv}{\partial y} \frac{\partial v}{\partial z} = hk$   $\frac{\partial v}{\partial z} - \frac{3y^2}{a^3} \frac{\ddot{o}}{a}$   
At  $y =$ , astress =  $hk \frac{\partial A}{\partial x} - \frac{\partial v}{\partial z} = \frac{hk}{a}$ 

If, x1 is maximum elongation in the spring when the particle is in its lowest extreme position. Then,

mgh = 
$$\frac{1}{2}$$
kx<sub>1</sub><sup>2</sup> - mgx1  
 $\frac{1}{2}$   
 $\frac{1}{2}$  \_ kx21-mgx1-mgh=0

or, 
$$1 - \frac{2mg}{k} \times 1 - \frac{2mg}{k} \cdot h = 0$$

$$-\frac{k}{2mg} + \sqrt{\frac{\acute{e}}{\hat{e}} \frac{2mg}{k} \frac{\ddot{o}^2}{\dot{e}} + 4 \cdot \frac{2mg}{k} h \dot{u}}{\dot{u}}}$$

$$\sqrt{x1} = \frac{\sqrt{\frac{\acute{e}}{\hat{e}} \frac{2mg}{k} \frac{\ddot{o}^2}{\dot{e}} + 4 \cdot \frac{2mg}{k} h \dot{u}}}{\sqrt{2}}$$

Amplitude A =  $X^{\frac{2}{3}}$  – X0 (elongation in spring for equilibrium position)

$$A = \frac{mg}{k} \sqrt{\frac{æ}{c_1 + 2hk}} = \frac{\ddot{o}}{c_1 + 2hk}$$

 $A = \frac{mg}{k} \sqrt[k]{\frac{e}{c^{1+2hk^{\div}}}}$ Let the initial mass of uranium be M0 25. (c) Final mass of uranium after time t.  $M = \frac{3}{4}M_{\odot}$ 

> According to the law of radioactive disintegration.

$$t = T \frac{\frac{10 e^{M_0} \ddot{o}}{e^{M_0} \dot{o}}}{\log 10(2)} = \frac{T \log 10 e^{\frac{34}{6} \ddot{o}} \ddot{o}}{\log 10 (2)}$$

$$= \frac{T \log 10 \cdot 1.333}{\log 10(2)} = \frac{3.5 \cdot 10 e^{0.1249 \ddot{o}}}{0.3010 \dot{o}}$$

$$= t = 1.867 \times 109 \text{ yr.}$$

(b) Total carrent,  $l = (5 + 10 \sin w_t)$ 

27. (a) If F be the equivalent focal length, then

$$\frac{1}{F} = \frac{1+1}{f1} \frac{1}{f2} \frac{1}{F} = (\mu 1 - 1) \frac{\text{ell}}{\xi} + \frac{1}{R} \frac{\ddot{o}}{\dot{e}} + \frac{1}{R} \frac{\ddot$$

28. (b) Total moment of inertia

= I1 + I2 + I3 + I4 = 2I1 + 2I2  
= 
$$2(I1 + I2) [I3 = I1, I1 = I4]$$
  
Now, I2 = I3  $\frac{\text{MI2}}{3}$ 

Using parallel axes theorem, we have

I=I <sub>CM</sub> +Mx2 and x= 
$$\sqrt{l^2} \frac{l^2}{4}$$
  
I<sub>1</sub> = I<sub>4</sub> =  $\frac{Ml^2}{12}$  + M  $\stackrel{\acute{e}}{e}$   $\sqrt{l^2 + \frac{el\ddot{Q}^2}{e^2}} \stackrel{\grave{u}}{2}$   $\stackrel{\acute{u}}{e}$   $\stackrel{\acute{u}}{e}$ 

Putting all values we get

Moment of inertia, 
$$I = 100$$
  $\stackrel{\text{def}}{\text{C}}$   $\stackrel{\text{def}}{\text{e}}$   $\stackrel{\text{def}}{\text{3}}$   $\stackrel{\text{def}}{\text{+}}$   $_{\text{0}}$ 

29. (b) For 2nd line of Balmer series in hydrogen spectrum

$$\frac{1}{1} = R(1) \frac{\text{@1}}{\text{@2}} - \frac{1}{42} = \frac{3}{9} = \frac{3}{16} R$$

For Li2+ 
$$\frac{\acute{e}1}{\acute{e}1}$$
 = R'9  $\frac{@1}{\acute{e}x}$ 2  $\frac{1}{12^2}\frac{\ddot{o}}{\acute{e}}$  =  $\frac{3R}{16}\frac{\mathring{u}}{\mathring{u}}$ 

which is satisfied by n = 12 ® n = 6.

30. (c) When a charge particle is allowed to move in a uniform magnetic field, then it describes spiral or circular path

Centripetal force, 
$$\frac{mv^2}{R} = qvB$$

Hence, 
$$\sqrt{\frac{2qV}{m}} = \underset{\stackrel{\longleftarrow}{e} \stackrel{\rightarrow}{m} \stackrel{\stackrel{\rightarrow}{e}}{\stackrel{\rightarrow}{m}} \stackrel{\stackrel{\leftarrow}{e}}{\stackrel{\rightleftharpoons}{e}} V = \sqrt{\frac{2qV}{m}} \overset{\stackrel{\leftarrow}{u}}{\overset{\leftarrow}{u}}$$

$$PR = \frac{e}{e} \frac{e}{q} \frac{\ddot{o}^{1/2}}{\ddot{o}}, \frac{1}{B}$$

or, m  $\mu$  R2

[Q V, q and B are constant]

or, 
$$\frac{m1}{m2} \stackrel{\text{æ}}{=} \frac{R\ddot{0}^2}{\mathring{e} \ QR \cancel{2}^{\frac{1}{2}}} \stackrel{\text{?}}{\text{Ø}}$$

31. (b) Water wets glass and so the angle of contact is zero.
For full rise, neglecting the small mass in the meniscus

 $_{2prT = p}$ r2hrgh=f[Qwater wets glass, q=0°]

As the tube is only 2 cm above the water and so, water will rise by 2 cm and meet the tube at an angle such that,

$$2pT\cos q = p^2h\phi rg$$

$$\Rightarrow$$
 2T cosq = h¢ rg

$$\Rightarrow \cos q = \frac{h^{\circ} rg}{2T}$$

$$= \frac{2^{10-2} 0.2510-310009.8}{20007}$$

The liquid will meet the tube at an angle, q @ 70°

32. (d) Given: Initial velocity u = 0.000 m/s; angle of projection  $q = 45^{\circ}$ 

Therefore horizontal and vertical components of initial velocity are

$$ux = 20\sqrt{2}\cos 45^{\circ} = 20 \text{ m/s}$$

and uy=202sin45°=20m/s

After 1s, horizontal component remains unchanged while the vertical component becomes

$$vy = uy - gt$$

Due to explosion, one part comes to rest. Hence, from the conservation of linear momentum, vertical component of second part will become v¢y=20m/s.

Therefore, maximum height attained by the second part will be

$$H = h1 + h2$$

= Using, h ut  $+\frac{1}{2}$ at2

P 
$$h_1 = (201') - \frac{1}{2} 10'(1) = 15 \text{ m}$$
  
  $a = g = 10 \text{ m/s} 2$ 

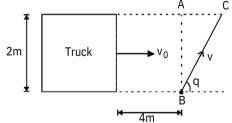
$$h_2 = \frac{\sqrt{Q}}{2g} = \frac{(20)2}{2'10} = 20m$$

H = 20 + 15 = 35 m

33. (c) Let the man starts crossing the road at an angle q as shown in figure. For safe crossing the condition is that the man must cross the road by the time the truck describes the distance 4 + AC or 4 + 2cotq.

$$\frac{4+2\cot q}{8} = \frac{2/\sin q}{v} \text{ or } v = \frac{8}{2\sin q + \cos q}$$
... (i)

For minimum v,  $\frac{dv}{da} = 0$ 



or 
$$\frac{-8(2\cos q - \sin q)}{(2\sin q + \cos q)^2} = 0$$
 or  $2\cos q - \sin q = 0$ 

or 
$$tanq = 2$$

From equation (i),

momentum.

$$v \min = \frac{8}{2 \frac{\approx 2}{6} \frac{\ddot{9}}{\sqrt{5}} + \frac{1}{\sqrt{5}}} = \frac{8}{\sqrt{5}} = 3.57 \text{ m/s}$$

34. (b) Let speed of neutron before collision = V Speed of neutron after collision = V1 Speed of proton or hydrogen atom after collision = V2

> Energy of excitation = DE From the law of conservation of linear

mv = mv1 + mv2 ...(1)And for law of conservation of energy,

$$\frac{1}{2} {\overset{m2=1}{v}} \frac{{\overset{m2+1}{2}} {\overset{mv2}{1}} \frac{1}{2} {\overset{mv2}{2}} \qquad ...(2)$$

From squaring eq. (i), we get

From squaring eq. (ii), we get

$$v2 = v21 + v22 \frac{2DE}{m}$$
 ...(4)

From eqn (3) & (4)

$$\sqrt{2v1v2} = \frac{2DE}{m}$$

$$(v1-v2)^{2} = (v_{1}^{+}v2)^{2} - 4v_{12}^{2} = v2 - \frac{4DE}{m}$$

As, v1 – v2 must be real,  $v^2 - \frac{4DE^30}{m}$ 

The minimum energy that can be absorbed by the hydrogen atom in the ground state to go into the excited state is 10.2 eV. Therefore, the maximum kinetic energy needed is

$$\frac{1}{2}$$
 mv<sub>min</sub> = 2 10.2 = 20.4 eV

35. (a) From, figure,

A<sub>R</sub> = 
$$\sqrt{(\sqrt{3})^2 + (21)} = 2$$

q =  $\tan^{-1}\frac{2\sqrt{3}}{\sqrt{9}}$ 

q =  $\tan^{-1}\frac{2\sqrt{3}}{\sqrt{9}}$ 

q =  $\tan^{-1}\frac{2\sqrt{3}}{\sqrt{9}}$ 

$$y = 2\sin \frac{e}{c} W t + \frac{p \ddot{o}}{c} 3 \phi$$

$$\frac{d2y}{dt2} = a = -w2 \sin \frac{\omega}{2} w t + \frac{\ddot{\omega}}{3\dot{\omega}} \tilde{\omega}$$

$$a_{max} = -2v^2 = 9$$

 $a_{max}$  = -  $2v^2$  = gFor which mass just breaks off the plank

$$w = \sqrt{g/2}$$

This will be happen for the first time when

$$wt+p+p$$
 or  $w=p$ 

$$3 \ 2$$
  $t = p = p/2$ 

$$t = \frac{p}{6w} = \frac{p}{6}\sqrt{\frac{2}{g}}$$

36. (b) From the figure.

The net charge shared between the two capacitors

$$Q2 = C2V \overline{2} = (2C)(2V) = 4CV$$

The two capacitors will have some potential, say V¢.

The net capacitance of the parallel combination of the two capacitors

The potential of the capacitors

$$V = \frac{C = \frac{C}{C}}{Q = \frac{3C}{3CV}} = V$$

The electrostatic energy of the capacitors

$$E = \frac{1}{2} C V = \frac{1}{2} (3C) V = \frac{3}{2} CV^2$$

$$Z = \sqrt{R2 + \underset{\xi}{\text{ew}}L - \frac{1}{\text{w} \div C\emptyset}}$$

$$= \sqrt{\frac{102 + 2000510^{-3} - \frac{1}{2000'50'10^{-6}}}{\dot{e}}} = 100$$

$$i = \frac{V_0}{Z} = \frac{20}{10} = 2A.$$

38. (b) The heat produced is given by

$$H = \frac{V^2}{R}$$
 and  $R = \frac{r_1}{pr_2}$ 

or 
$$H = \underset{\stackrel{\leftarrow}{\mathbb{R}}}{\mathbb{R}} \frac{V^2}{\frac{\ddot{o}r^2}{\dot{a}l}}$$

Thus heat (H) is doubled if both length (I) and radius (r) are doubled.

39. (b) As we know, frequency

$$f\mu \sqrt{mg}$$
 or  $f\mu \sqrt{g}$ 

In water, fw=0.8fair

$$\frac{g^{c}}{g}(0.8) = 0.64$$

$$\frac{r}{r} = 0.64$$

$$\frac{rw}{rm} = 0.36 \qquad ...(1)$$
In liquid,
$$r \qquad \frac{g^{+}}{g} = (0.6)2 = 0.36$$

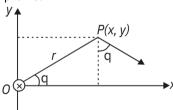
$$1 - \frac{1}{rm} = 0.36 \frac{r}{rm} = 0.64 \dots (2)$$

From eq. (1) and (2)

$$\frac{rl}{rn} = \frac{0.64}{0.36} \ rl = 1.77$$

40. (a) The wire carries a current *I* in the negative *z*-direction. We have to consider the

magnetic vector field  $\overset{\text{u r}}{B}$ at (x, y) in the z = 0 pl an e.



Maugrnetic field is perpendicular to OP.  $B=B\sin i$   $q - B\cos q \hat{i}$ 

$$\sin q = \frac{y}{r}, \cos q = \frac{x}{r} B = \frac{m_0 I}{2pr}$$

$$\lim_{B = \infty}^{B = \infty} \frac{m_0 I}{2pr^2} (\hat{y} \hat{t} \times \hat{j})$$
or
$$\lim_{B = \infty}^{B = \infty} \frac{m_0 I}{2pr^2} (\hat{y} \hat{t} \times \hat{j})$$

# PART - II: CHEMISTRY

- 41. (c) NO pollutant is the main product of automobiles exhaust. The high
- 42. (c) concentration of hydrocarbon pollutants in atmosphere causes
- 43. (b) Electronic configuration of element with atomic number 118 will be [Rn]5f146d10 7s27p6. Since its electronic configuration in the outer most orbit (ns2np6) resemble with
- 44. (c) that of inert or noble gases, therefore it will be noble gas element.

The third law helps to calculate the absolute entropies of pure substances at different temperature.

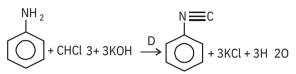
The entropy of the substance at different temperature. T may be calculated by the measurement of least rapacity change  $S_T - S_0 = DS = 0$ 

Where ST = Entropy at T K S0= Entropy at 0K

- = Cp.logeT
- = 2.303Cp.logT
- 45 (d CoCl3.5NH3.H2O is pink in colour
  - ) Cobalt is present in vitamin B12.
- 46 (b Cobalt (60) isotope is used in the treatment of cancer.
- PMMA is used in bullet proof glass
- 49. (a) ClO-4<ClO-3<ClO-2<ClO- is the correct increasing order of Bronsted base. With increase in the number of oxygen atoms in the conjugate bases, the delocalisation of the p bond becomes more and more extended. This results in decrease in the electron density. Consequently basicity also decreases.
- 50. (a) Due to dipole-dipole interaction the boiling point of alkyl halide is higher as compared to corresponding alkanes.
- 51. (c) Complex compounds contains two different metallic elements but give test only for one of them. Because complex ions such as [Fe

(CN)]4–6of K4 [Fe (CN)6], do not dissociate into Fe2+ and CN– ions.

52. (b) Primary amines (aromatic or aliphatic) on 62. warming with chloroform and alcoholic KOH, gives carbylamine having offensive smell. This reaction is called carbylamine reaction.



53 (b Nitrous oxide (i.e., N2O) is the laughing gas. Anthracene is purified by sublimation. )

54 (d

- sublimation, a solid is converted directly into gaseous state on heating without passing through liquid phase.
- 55. salt is common name of
- CaCl2 is produced as a by product in solvay 56. (c) ammonia process.
  - NaCl + CO2 + NH3 + H2O 34348NaHCO3 + NH4Cl
  - (ii) CaCO3 3434@CO2 + CaO

3/43/4®2NH3 + (iii)2NH2Cl + CaO CaCl<sub>2</sub> + H2O **Byproduct** 

57. (b) Semiconductor materials like Si and Ge are usually purified by zone refining. Zone refining is based on the principle of fractional crystallisation i.e. difference in solubilities of impurities in solid and molten states of metal, so that the zones of impurities are formed and finally removed.

58. (c) Order of basic character is NH3 > PH3 > AsH3 > SbH3. Basic-character decreases down the group from N to Bi due to

increase 59. in atomic size.

> Normal glass is calcium alkali silicate glass made by fusing the alkali metal carbonate,

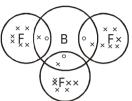
60 (c)

Exa = 1018 CaC03 and SiO2 More the oxidation state of the central (b)

61

(metal) more is its acidity. Hence SeO2 (O. S. of Se = +4) is acidic. Further for a given O.S., the basic character of the oxides increases with the increasing size of the central atom. Thus Al2O3 and Sb2O3 are amphoteric and Bi203 is basic.

BF3 does not follow octate rule because central atom, boron lacks an electron pair. Thus, it also acts as Lewis acid.



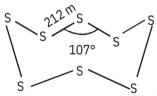
According to Le-Chatelier's principle increase in temperature favours the endothermic reaction while decrease in temperature favour the exothermic reaction. Increase in pressure shifts the equilibrium

in that side in which number of gaseous moles decreases. 64. (a)

Efficiency of fuel cell is:

- 65. The mass of the substance deposited when one Faraday of charge is passed through its solution is equal to gram equivalent weight. Unit of rate constant for
- second order 66. (a) reaction is L mol-1 sec-1.
- 67. For first order reaction  $[A] = [A]e_{\Gamma}kt$ \ The concentration of reactants will exponentially decreases with time.
- 68. In P4 molecule, the four sp3-hybridised phosphorous atoms lie at the corners of a regular tetrahedron with DPPP = 60°.

In S8 molecule S-S-S angle is 107° rings.



- (a) 40 elements are present in d-block.
- EDTA is hexadentate ligand (a)

69

70

- 71. (a) Am shows maximum number of oxidation states, + 3, + 4, + 5, + 6
- 72. (a) Fe3+ ion can be detected by K4[Fe(CN)6]  ${}^{4\text{Fe}3^{+}} + 3\text{K}_{4} \not \text{gFe}(\text{CN}) \dot{\text{H}}$

$$3/43/4$$
% Fe4 gFe ( C) 16 + 12K+

- 73. (d) DG = **D** TS; **D** is positive for a reaction to be non-spontaneous when DH is positive and DS is negative.
- 74. (a) This method is known as Clark's process.

  In this method temporary hardness is go removed by adding lime water or milk of lime.

Ca (OH) 2 + Ca(HCO)<sub>3 2</sub> 
$$^{3}4^{3}4^{\circ}$$
 2CaCO3  $^{-}$  +2H2O ppt.

- 75 (b Graphite is covalent solid.. )
- 76 (c) Xe + F2 <sup>3</sup>/<sub>4</sub>6<sup>3</sup>/<sub>4</sub>73<sup>3</sup>/<sub>4</sub>KeF2
- · (b 2:1 77

) Xe+2F<sub>2</sub> <sup>3</sup>46<sup>3</sup>473<sup>3</sup>4K<sup>®</sup>eF<sub>4</sub> 5-6Atm

1:5

Structures of Xenon fluorides

Xe F 2: Hybiidizite p3



Linear

Xe F:<sub>4</sub> Hybridization spd <sup>32</sup>



Square planar

XeF6: Hybribisation spd<sup>8</sup>



Pentagonal pyramidal or distorted octahedral Calcium silicophosphate (a

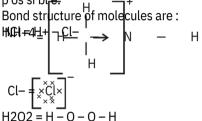
78. (c) mixture of

Ca3(PO4)2 & Ca2SiO4) is called Thomas 79. (a) Saa

The sequence of bases in mRNA are read in a serial order in groups of three at a

Each codon specifies one amino acid.

(b) Further since, there are four bases. therefore, 43 = 64 triplets or codons are p os si blee.



hece, cle  $\,^{\rm arly\ NH^+}$ 4ion contains all three types of bonds.

# PART - III (A): <u>ENGLISH PROFICIENCY</u>

- 81 (c) 'Immutable' means 'unchangeable'. So, option (c) is correct choice. 'ignominious'
  - (a) means 'shameful'. So, option (a) is correct choice. 'callous' means 'showing
- 82 (c) or having an insensitive and cruel disregard for others'. So, option (c) is correct choice. Option (d) institutional as
  - (a) the word means relating to principles esp. of law, so legally also every human has rights of freedom and equality. 86. (c) Immortal means living forever, never
- 85 (a) dying or decaying. So, perishable is the
- (b) correct opposite to it. Opposed is the correct answer of this. To patronise
- means favour or pat on the back. Tactful
  means having or showing skill and
  - senstivity in dealing with others or with defficult essues. So, in cautious is the
- correct opposite of factful. Atheist is the best alternative. 'Epicure' is the best alternative.
- 90 (c) . (c)

84. 83

. (C)

# PART - III (B): LOGICAL REASONING

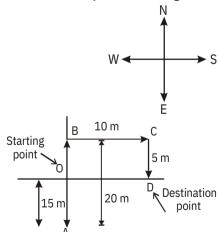
95 (c) 97. (c)

(b) The contents of the third figure in each row (and column) are determined by the contents of the first two figures. Lines are carried forward from the first two figures to the third one, except where two lines appear in the same position, in which they are cancelled out. From figure, (i), (iii) and

99. (b) (iv), we have concluded that 2, 6, 1 and 5 appear adjacent so 3. clearly, 4 will appear opposite to 3. In figure (A), the dot is placed in the region which is common to

100. (c) placed in the region which is common to the circle and triangle. Now, we have to find similar common region in all the four options. Only in figure (c), we find such a region which is common to the circle and triangle.

102. (a) According to the given information, the direction of Neeraj is as following.



103. (b) Let the average age of 8 men = x yr

Total age of 8 men =  $8 \times y$ r

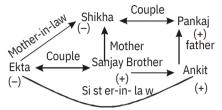
Now, new average age = (x + 2)yr

Total age = 8(x + 2)yr

Difference of ages = 8(x + 2) - 8x= 8x + 16 - 8x = 16 yr

\ Age of new man = 20 + 16 = 36 yr So, the new man is 16yr older to the man by whom the new man is replaced.

104. (d) The relation is as following:



It is clearly shown that Shikha is the mother of Ankit. Since Arun and Suresh 105. (b) interchange places, so Arun's new position (13th from left) is the same as Suresh's earlier position (6th from right). So, number of children in the queue = (12 + 1 + 5) = 18.

Now, Suresh's new position is the same as Arun's earlier position fifth from left. Therefore Suresh's position from the right = (18 - 4) = 14th.

# PART - IV: MATHEMATICS

106. (d) Consider  $\lim_{\substack{x^{\circ} \neq \\ 2x}} \frac{\dot{Q}^{2x} x e^{x^{2}} dx}{\frac{2}{e}^{4x^{2}}}$   $= \lim_{x^{\circ} \neq} \frac{2 \dot{Q}^{x} x e^{x} dx}{\frac{2}{e}^{4x^{2}}}$   $= \lim_{x^{\circ} \neq} \frac{2 \dot{Q}^{x} e^{x^{2}} d(x^{2})}{\frac{2}{e}^{2x^{2}} x^{2}}$   $= \lim_{x^{\circ} \neq} \frac{e^{x^{2}} d(x^{2})}{\frac{2}{e}^{2x^{2}} x^{2}}$ 

107. (a) Consider 
$$\frac{1}{2} + \frac{3}{8} + \frac{9}{32} + \frac{27}{128} + \dots$$
  
Which can be written as 
$$\frac{3^0}{2^1} + \frac{3^1}{2^3} + \frac{3^2}{2^5} + \frac{3^3}{2^7} + \dots$$

110. (d) tanq is of period p so that tan 3q is of period p/3.

111. (b) Let

$$f(x) = \frac{x}{1+x} + \frac{x}{(x+1)(2x+1)} + \frac{x}{(2x+1)(3x+1)} + ... + \frac{x}{(2x+1)(3x+1)(3x+1)} + ... + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)} + ... + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)} + ... + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)(3x+1)} + ... + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)} + ... + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)} + ... + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)} + ... + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)} + ... + \frac{x}{(2x+1)(3x+1$$

$$= \lim_{\substack{n = 1 \\ lim \\ lim \\ x = 1}} \mathring{\overset{n}{\mathbf{a}}} \underbrace{\overset{x}{\mathbf{e}}(r-1)x+1\mathring{\mathbf{e}}(rx+1)}_{\overset{i}{\mathbf{e}}}$$

$$= \overset{n}{\overset{n}{\mathbf{e}}} \overset{\acute{\mathbf{e}}}{\overset{i}{\mathbf{e}}} \underbrace{\overset{x}{\mathbf{e}}}_{r-1} \mathring{\overset{i}{\mathbf{e}}} \underbrace{\overset{i}{\mathbf{e}}}_{r-1} \mathring{\overset{i}} \underbrace{\overset{i$$

So, f(x) is not continuous at x = 0.

112. (c) Since, g is the inverse of function Therefore, g(x) = f-1(x)f[g(x)] = x

Þ fog (x=x,forallx

Differentiate both side, w.r.tx

$$\Rightarrow \frac{d}{dx} \{ fog(x) \} = \frac{d}{dx}(x), for all x$$

f.

$$\Rightarrow \sin gx$$
  $g'x = 1, \text{ for all } x$ 

(By defn of (x))

$$\Rightarrow g'(x) = \frac{1}{\sin\{g(x)\}}$$

113. (a) Total number of coins= 2n+1Consider the following events: E1= Getting a coin having head on both sides from the bag. E2= Getting a fair coin from the bag A = Toss results in a head

Given: P(A) = 
$$\frac{31}{42}$$
, P(1) =  $\frac{n}{2n+1}$ 

and  $P(E) = \frac{n+1}{2n+1}$ 

Th en .

$$P(A)=P(E)P(AE)P(AE)$$

$$\frac{5}{31} = \frac{n}{2n+1} \cdot 1 + \frac{n+1}{2+n} \cdot \frac{1}{2}$$

$$42 = \frac{4}{2} \frac{n}{2n+1} + \frac{n+1}{2(2n+1)}$$

$$\frac{3}{1} = \frac{3n+1}{2(2n+1)}$$

$$\frac{4}{2} = \frac{3n+1}{2n+1}$$

$$2n = 10$$

114. (a) Given differential equation is

$$dy + \{yf'(x)-f(x)f(x)\}$$

$$b \frac{dy}{dx} + f (x) y = f(x) f'(x)$$

which is a linear differential equation with P = f'(x, 0) = f(x) x and (

$$I.F = e^{\circ} f(x)$$

Solution is y.ef 
$$(x) = \grave{o}f(x).f'(x)ef^{x})dx + C$$

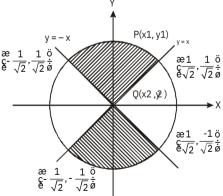
$$b y.e^{f(x)} = \grave{o}f(x)f.(e^{f(x)})f'(x)dx + C$$

$$b y.e^{f(x)} = f(e^{f(x)} - \grave{o}f(e^{x})ef^{x}dx + C$$

$$b y.e^{f(x)} = f(x)f(e^{x}) - e^{f(x)} + C$$

$$b y = e^{f(x)} = f(x) - e^{f(x)}$$

115. (c)



Required area = 4 (Area of the shaded region in first quadrant)

$$=4\dot{Q}^{1\sqrt{2}}(y_1-y_2)dx=4\dot{Q}^{1\sqrt{2}}\dot{Q}^{2}\dot{Q}^{2}\sqrt{1-x^2}-x\dot{Q}^{2}dx$$

$$=4 \overset{\acute{e}x}{\stackrel{?}{2}} \sqrt{1-x^2} + \frac{1}{2} \sin^{-1}x - \frac{x \overset{2\dot{u}}{u}}{\overset{\dot{u}}{u}} \sqrt{2}$$

$$=4 \overset{\acute{e}}{\stackrel{\dot{e}}{e}} \frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} + \frac{1}{2} \overset{\dot{p}}{4} - \frac{1}{4} \overset{\dot{u}}{\dot{u}}$$

$$= \overset{\dot{e}}{\overset{\dot{e}}{e}} \frac{1}{\sqrt{2}} + \overset{\dot{p}}{\sqrt{2}} - \frac{1}{2} \overset{\dot{u}}{\dot{u}} + \frac{1}{2} \overset{\dot{u}}{\dot{u}} + \frac{1}{2} \overset{\dot{u}}{\dot{u}} = \frac{1}{2} \overset{\dot{u}}{\dot{u}} + \frac{1}{2} \overset{\dot{u}}{\dot{u}} = \frac{1}{2} \overset{\dot{u}}{\dot{u}} + \frac{1}{2} \overset{\dot{u}}{\dot{u}} = \frac{1}{2} \overset{\dot{u$$

Solving for values of x, we get  $U = \{0, 1, 2, 3\}$  $A = \{x : x2 - 5x + 6 = 0\}$ Solving for values of x, we get  $A = \{2, 3\}$ and B =  $\{x : x2 - 3x + 2 = 0\}$ Solving for values of x, we get  $B = \{2, 1\}$  $A \ C B = \{2\}$  $\ \ (A \ C B)' = U - (A \ C B)$  $= \{0, 1, 2, 3\} - \{2\} = \{0, 1, 3\}$ 

117. (c) 
$$\cos^{-1} x - \cos^{-1} \frac{y}{2} = a$$
  

$$\Rightarrow \cos^{-1} \frac{e^{xy}}{c^{2}} + \sqrt{(1 - x^{2}) \frac{e^{2}}{c^{1}} - \frac{y^{2}}{4} \frac{\ddot{o}}{\dot{o}}} = a$$

$$\Rightarrow \cos^{-1} \frac{e^{xy}}{c^{2}} + \sqrt{4 - y^{2} - 4x^{2} + x^{2}} \frac{\ddot{y} \ddot{o}}{\dot{o}^{2}} = a$$

$$\Rightarrow \cos^{-1} \frac{e^{xy}}{c^{2}} + \sqrt{4 - y^{2} - 4x^{2} + x^{2}} \frac{\ddot{y} \ddot{o}}{\dot{o}^{2}} = a$$

$$\Rightarrow 4 - y \cdot 2 - 4x^{2} x^{2} x^{2} x^{2} y^{2} = 4$$

$$4\cos^{2} 2a + x^{2} y^{2} - 4 \cos^{2} a$$

 $b \quad 4x^2 + y^2 4xy \cos \quad a = 4\sin^2 a .$ 

118. (d) Let
$$\frac{e^{x} + \frac{5x}{e^{3x}}}{e^{3x}} = a_{0} + a_{1}x + a_{2}x^{2} + a_{3}a^{3} + ....$$

$$= \frac{e^{x}}{e^{3x}} + \frac{e^{5}}{e^{x}} = a_{0} + a_{1}x + a_{2}x^{2} + ....$$

$$= e^{-2x} + e^{2x} = a_{0} + a_{1}x + a_{2}x^{2} + ....$$

$$= e^{-2x} + e^{2x} = a_{0} + a_{1}x + a_{2}x^{2} + ....$$
By using x
$$e^{x} = 1 + x + \frac{x^{2}}{2!} + \frac{x^{3}}{3!} + - - - a_{1}x + a_{2}x^{2} + ....$$

$$e^{x} = 1 + x + \frac{x^{2}}{2!} + \frac{x^{3}}{3!} + - - - a_{2}x + a_{3}x^{3} + ....$$

$$e^{x} = 1 + x + \frac{x^{2}}{2!} + \frac{x^{3}}{3!} + - - - - a_{2}x + a_{3}x^{3} + ....$$

$$e^{x} = 1 + x + \frac{x^{2}}{2!} + \frac{x^{3}}{3!} + - - - - a_{2}x + a_{3}x^{3} + ....$$

$$e^{-2x} + e^{2x} + e^{2x} + \frac{e^{2x}}{2!} + \frac{e^{2x}}{4!} + \frac{e^{2x}}{4!} + .... + \frac{e^$$

= 
$$a_0 + a_1x + a_2x^2 + a_3a^3 + ...$$
  
=  $a_1 = a_3 = a_5 = ... = 0$   
Hence,  $2a_1 + 2^3 a_3 + 2^5 a_5 + ... = 0$ 

119. (d) Let gbe the angle between b and c.

Given, 
$$b'c \models \sqrt{15}$$

$$|b|c \sin q = \sqrt{15}$$

$$\Rightarrow \frac{1/5}{\sin q} = \frac{1/5}{|bc|}$$

$$\Rightarrow \sin q = \sqrt{\frac{15}{4'1}} = \frac{\sqrt{15}}{4}$$

$$\cos q = \sqrt{1 - \frac{15}{16}} = \frac{1}{\sqrt{16}} = \frac{1}{4}$$

Now given,b-  $2c = |a|b-2c^2 = |a|^2$ 

$$|b|^2 + 4|c| - 4 (b) \in l^2|a|^2$$

$$p^{20} - 4 = l^{2}p l^{2} = 16^{\infty}_{e} \cos q = \frac{1}{4}^{0}_{\phi}$$

120. (b) Total number of arrangements of 10 digits 0, 1, 2, ..., 9 by taking 4 at a time =  $10C4 \times 4!$ We observe that in every arrangement of 4 selected digits there is just one arrangement in which the digits are in descending order. \ Required number of 4-digit numbers.

$$=\frac{^{10}C4'4!}{^{41}}=10C4$$

Given equation of a line parallel to X-axis is 121. (c) y = k.

Given equation of the curve is  $y = \sqrt{x}$ ,

On solving equation of line with the equation of curve, we get x = k2

Thus the intersecting point is (k2, k) It is given that the line y = k intersect the

kuntvenyangle of p/4. This

means that the slope of the tangent to

y= 
$$\sqrt{x}$$
 at (k2, k) is tan  $\stackrel{\text{get}}{\stackrel{\text{d}}{=}} \frac{p}{4} \stackrel{\text{o}}{\stackrel{\text{d}}{=}} \pm 1$ 

$$\triangleright k = \pm \frac{1}{2}$$

Let A, B and C be the three angles of DABC 122. (a)

Let a = 10 and b = 9

It is given that the angles are in AP. 

we get 3B = A + B + C

Þ 3B = 180° Þ B = 60°

Now, we know cosB =  $\frac{a^2 + c^2 - b^2}{a^2}$ 

$$b \frac{\cos 60^{\circ} = 10^{2} + c^{2} - 9^{2}}{2'10'c}$$

$$\Rightarrow$$
 c2 - 10c + 19 = 0 \( \text{c} = 5 \div 6 \)

123. (d) Since, Mean= 
$$\frac{\text{åfix}_i}{\text{å fi}}$$
 where x are

observations with frequencies fi, i = 1, 2,

The required mean is given by
$$\overline{X} = \frac{0.1 \cdot 1.nC_{1} + 2.nC_{2} + ...... \cdot a.nC}{1 + nC_{1} + nC_{2} + ..... \cdot a.nC} = \frac{1 + nC_{1} + nC_{2} + .... \cdot a.nC}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{2} + ... + nC_{1}}{1 + nC_{1} + nC_{2} + ... + nC_{1}} = \frac{1 + nC_{1} + nC_{1}}{1 + nC_{1} + nC_{1}} = \frac{1 + nC_{1} + nC_{1}}{1 + nC_{1} + nC_{1}} = \frac{1 + nC_{1} + nC_{1}}{1 + nC_{1} + nC_{1}} = \frac{1 + nC_{1} + nC_{1}}{1 + nC_{1} + nC_{1}} = \frac{1 + nC_{1} + nC_{1}}{1 + nC_{1} + nC_{1}} = \frac{1 + nC_{1} + nC_{1}}{1 + nC_{1} + nC_{1}} = \frac{1 + nC_{1} + nC_{1}}{1 + nC_{1} + nC_{1}} = \frac{1 + nC_{1} + nC_{1}}{1 + nC_{1} + nC_{1}} = \frac{1 + nC_{1}}{1 + nC_{1}} = \frac{1$$

124. (a) We have 
$$\prod_{i=1}^{r-1} a_{i}^{n} (x^{i} + 2)2 = 18$$
 and

$$\frac{1}{n} \mathring{a}_{i-1}^{n} (xi - 2)^2 = 10$$

$$\stackrel{\text{a}}{=} (x_i + 2)2 = 18n \text{ and}$$

$$\overset{n}{\hat{a}} (xi - 2)^2 = 10n$$

$$\overset{i=1}{\hat{a}} (xi + 2) 2 + \overset{n}{\hat{a}} (xi - 2) 2 = 28n$$

$$\overset{n}{\hat{a}} (xi + 2) 2 \overset{n}{\hat{a}} (xi - 2) 2 = 8n$$

$$\overset{n}{\hat{a}} (xi + 2) 2 \overset{n}{\hat{a}} (xi - 2) = 8n$$

$$\overset{n}{\hat{a}} (xi + 2) 2 \overset{n}{\hat{a}} (xi - 2) = 8n$$

Þ 2å₁ +4)2 æn and 
$$\sum_{i=1}^{n} 2å4 xi$$
8n

$$P \overset{\circ}{a}_{i=1}^{n} x^{2i+4n} = 14n \text{ and } \overset{\circ}{a} xi = n$$

125. The parametric equations of the parabola y2 = 8x are x = 2t and y = 4t.
and the given equation of circle is

$$x^2 + y^2 - 2x - 4y = 0$$

On putting x = 2t2 and y = 4t in circle we get

$$4t^4 + 16t^2 - 4t^2 - 16t = 0$$

$$4t2 + 12t2 - 16t = 0$$

$$4t(t3 + 3t - 4) = 0$$

$$b t(t-1)(t2+t+4) = 0$$

$$b t = 0, t = 1$$

Thus the coordinates of points of intersection of the circle and the parabola are Q (0, 0) and P(2, 4). Clearly these are diametrically opposite points on the circle.

The coordinates of the focus S of the parabola are (2, 0) which lies on the circle.

\Area of DPQS = 
$$\frac{1}{2} \times QS \times SP = \frac{1}{2} \times 2 \times 4$$
  
= 4 sq. units.

126. (a) Let 
$$f(x) = ex-1 + x - 2$$
  
check for  $x = 1$ 

Then, f(1) = e0 + 1 - 2 = 0 So, x = 1 is a real root of the equation f(x) = 0 Let x = a be the other root such that a > 1 or a < 1. Consider the interval 1,a] ora,1].

Clearly f(1) = f(a) = 0By Rolle's theorem  $f\phi(x) = 0$  has a root in (1, a) or in (a, 1).

But  $f_{\mathfrak{C}}(x) = ex-1 + 1 > 0$ , for all x. Thus, which is a contradiction, a)  $ext{ord}(x, x) = 0$  has no real root other than 1.

127. (c) Constraints will be

128. (c) Let A ° event that drawn ball is red
B ° event that drawn ball is white
Then AB and BA are two disjoint cases of the given event.
\P (AB + BA) = P(AB) + P (BA)

$$= P(A) P_{\xi A} \frac{\partial B}{\partial \dot{g}} + P(B) P_{\xi B} \frac{\partial \ddot{g}}{\partial \dot{g}}$$

$$= \frac{3}{6} \cdot \frac{3}{5} + \dots \cdot \frac{3}{5} = \frac{3}{5}$$

129. (b) We know that, M (adj M) = |M|IReplacing M by adj M, we get adj M [adj (adj M) = det (adj M) I = det (M) M-1 [adj (adj M) =  $a^2l$ 

$$\hat{e}QM-1=\overline{|M|}$$
  $adj(M)\dot{u}$   
 $\hat{e}\ddot{e}$   
 $\Rightarrow$  a M-1 [adj (adj M)] = a2I  
 $\Rightarrow$  M-1 [adj (adj M)] = a I  
But M-1 [adj (adj M)] = KI  
Hence, K = a

130. (c) Let 
$$(x1, y1)$$
 be one of the points of contact. Given curve is  $y = \cos x$ 

$$b \frac{dy}{dx} = -\sin x$$

$$b \frac{dy}{dx}\Big|_{(x_1, y_1)} = -\sin x 1$$

Now the equation of the tangent at (x1,y1) is

$$\begin{array}{ccc} & \text{y-y1}\underset{c}{\overset{\text{ædy}}{\in}} \overset{\ddot{o}}{\overset{\cdot}{\text{edx}}} \overset{(x-x1)}{\overset{\cdot}{\text{edx}}} \\ \text{b} & \text{y} \\ & \text{-y}_1 = -\sin x_1 (0-x_1) \end{array}$$

Since, it is given that equation of tangent passes through origin.

\ 
$$0-y1 = -\sin x 1 (0-x1)$$

$$P = y1 = -x1 \sin x1 ...(i)$$

Also, point (x1, y1) lies on  $y = \cos x$ .

$$\sqrt{1 = \cos x1}$$

From Eqs. (i), (ii), we get

$$\sin 2x_1 + \cos 2x_1 = \frac{y_2}{x_2^2} + y_{2_1}^2 = 1$$

$$\Rightarrow x_1^2 = y_1^2 + y_1^2$$

Hence, the locus of (x1, y1) is

$$x2 = y2 + y2x2 \Rightarrow x2y2 = x2 - y2$$

# 131. (b) Let m be the slope of the tangent to the curve

y = ex cos x.

Then, m 
$$=\frac{dy}{dx} = ex(osx-sinx)$$

Diff. w.r.t 'x'

$$b \frac{dm}{dx} = ex(COSX \sin x) + ex (\sin x - \cos x)$$

\_ 2ex sins

and 
$$\frac{d2m}{dx^2} = -2ex(sinx+cosx)$$

Put 
$$\frac{dm}{dx} = 0$$
  $\Rightarrow$   $\sin x = 0$   $\Rightarrow$   $x = 0$ , p, 2p

Clearly, 
$$\frac{d2m}{dx2} > 0$$
 for  $x = p$ 

Thus, y is minimum at x = p

Hence the value of a = .p

132. (a) The equations of given lines can be written

L1:x-5=
$$\frac{y}{3-a}=\frac{z}{2}$$

$$L2: x^{-a} = \frac{y}{-1} \frac{z}{2-a}$$

Since, these lines are coplanar.

Therefore, 
$$\begin{vmatrix} 5-a & 0-0 & 0-0 \\ 0 & 3-a-2 \\ 0 & -1 & 2-a \end{vmatrix} = 0$$

$$(5-a)(3-a)(2-a)-2=0$$

$$\triangleright (5 - a) (6 - 3a - 2a + a2 - 2] = 0$$

$$(5-a)(a2-5a+4]=0$$

$$\flat (5 - a) (a - 1)(a - 4) = 0$$

$$\Rightarrow a = 1, 4, 5$$

133. (b) 
$$e^{-\frac{1}{2}}$$
 Directrix,  $x = \frac{a}{e} = 4$ 

$$a = 4 \cdot \frac{1}{2} = 2 \quad b = 2\sqrt{1 - \frac{1}{4}} = \sqrt{3}$$

Equation of ellispe is

$$\frac{x^2}{4} + \frac{y^2}{3} = 1 \Rightarrow 3x^2 + 4y^2 = 12$$

134. (d) 
$$\frac{x}{2} + \frac{2}{x}$$
 is of the form  $x + \frac{1}{x}$  2 and equality holds for  $x = 1$ 

135. (a) 
$$y = (x + \sqrt{1 + x^2})n$$

$$\frac{dy}{d} = n(x + \sqrt{1 + x^2})^{n-1} \mathop{\text{cl}}_{\frac{1}{2}} \frac{1}{2} (1 + x^2)^{-1/2} \cdot 2 x_{\bar{\emptyset}}^{\ddot{o}};$$

$$\frac{d}{y} = n(x + \sqrt{1 + x})^{n-1} \frac{(\sqrt{1 + 2x} + x)}{\sqrt{1 + x^2}}$$

$$\frac{d}{x} = \frac{n(\sqrt{1+2x+} x)^n}{\sqrt{1+x^2}}$$

or 
$$\sqrt{1+x^2} \frac{dy}{d} = ny$$
 or  $\sqrt{1+x^2} y_1 = ny$   
 $(y1) = \frac{dy}{dx}$ 

Squaring,  $(1 + x^2) v 1^2 = n^2 v^2$ Differentiating.  $(1+2x)2v_1v_2 + v_1^2.2x = n^2.2vv1$ or  $(1+x2)y_2 + xy = n2 y$ 

136. (a) As given,

$$A = \lim_{x^{\otimes ¥}} x \sin \frac{\text{el \ddot{o}}}{\overset{\circ}{x}} \lim_{\phi \div = x^{\otimes ¥}} \frac{\sin \frac{\text{el \ddot{o}}}{cx^{\div \phi}}}{\text{el \ddot{o}}}$$

$$c$$

$$c$$

$$c$$

$$c$$

Let  $t = \frac{1}{x}$  when  $x \cdot a$ ,  $t \cdot 0$ 

$$\begin{array}{ccc}
& = & \\
& \downarrow & \underset{t = 0}{\text{lim}} & \frac{\sin t}{t} = 1 \\
& & \stackrel{\acute{e}}{\text{RQ}} & \frac{\sin x}{x} = 1 \\
& & & \stackrel{\grave{v}}{\text{lim}} & \frac{\sin x}{x} = 1 \\
& & & & & & \\
\end{array}$$

and  $B = \lim_{x \to 0} x \sin \frac{\text{el}}{x} \ddot{o}$  $(x \div 0)$ 

$$P B = \lim_{x \to 0} x. \lim_{x \to 0} \sin \frac{ad \ddot{o}}{c} \dot{c}$$

$$c \times \dot{\phi}$$

A = 1 and B = 0 is correct

137. (b) As given a and b are the roots of the equation

$$x^2 + ax + b = 0$$

sum of roots, a + b = -a

$$b = -2a...(1)$$

and product of roots, ab = b

$$\Rightarrow$$
 ab - b = 0

$$b (a-1) = 0$$

if b = 0 then a = 0

if  $b^{1}$  0 then a = 1 and b = -2

so, the expression will be,

$$f(x) = x^2 + x - 2$$

$$= x^2 + 2.\frac{1}{2}x + \frac{\text{ed}}{5}\frac{\ddot{0}^2}{2} - \frac{\text{ed}}{5}\frac{\ddot{0}^2}{2} - 2$$

$$f(x) = \frac{e}{e^{x}} + \frac{1}{2} \frac{\ddot{0}^{2}}{\dot{\theta}} - \frac{9}{4}$$

So, f (x) will be minimum, if  $\hat{\xi}^{x} + \frac{1}{2} \hat{\xi}^{02} = 0$ 

i.e. when 
$$x = -\frac{1}{2}$$

minimum value of function =  $-\frac{9}{4}$ 

138. (d) Let us assume the functions f(x) and g(x)

 $f(x) = \tan x - x$  and  $g(x) = x - \sin x$ , for

$$0 < x < \frac{p}{2}$$

Now,  $f(x) = \sec 2x - 1$  and

$$g(x) = 1 - \cos x$$

$$b \qquad f(x) > 0 \text{ and } g(x) > 0, \qquad \overset{\text{"x} \hat{I} \approx}{\underline{2}} 0, \frac{p\ddot{o}}{\underline{2}}$$

 $\begin{array}{ll} \begin{tabular}{ll} \begin{tabular}{ll$ 

 $\tan x > x$  and  $x > \sin x$ ,  $\stackrel{\text{ee}}{=} 0, \frac{p \ddot{o}}{2}$ 

139. (a) Put  $x = \sin q$  and  $y = \sin f$ 

 $\cos q + \cos f = a (\sin q - \sin f)$ 2 cos

$$\frac{q+f}{2}\cos\frac{q-f}{2} = 2a\cos\frac{q+f}{2}\sin\frac{q-f}{2}$$

$$\Rightarrow \cot \frac{q-f}{2} = a \Rightarrow q - f = 2 \cot^{-1} a$$

Þ sin-1 x − sin-1 y = 2 cot-1 a

Differentiate  $\frac{1}{\sqrt{1-x}} - \frac{1}{\sqrt{1-y}} \frac{dy}{dx} = 0$ 

so the degree is one

140. (b) Let f(x) = ax3 + bx2 + cx + d

Put x = 0 and x = 1

Then, we get f(0) = -1 and f(1) = 0

$$b = d = -1$$
 and  $a + b + c + d = 0$ 

$$\Rightarrow$$
 a + b + c = 1 ...(i)

It is given that x = 0 is a stationary point of f(x), but it is not a point of extremum.

# Therefore, f(0) = 0 = f(0) and f(0) = 0

Now, 
$$f(x) = ax3 + bx2 + cx + d$$

$$f \phi(x) = 6ax + 2b$$
 and  $f \phi(x)$ 

$$f = 0$$
,  $f = 0$  and  $f = 0$ 

 $\triangleright c = 0$ , b = 0 and  $a^{1}0$ 

From Eqs. (i) and (ii), we get

a = 1, b = c = 0 and d = -1

Put these values in f(x)

we get f(x) = x3 - 1

Hence, 
$$\dot{O}_{x^{3}}^{f(x)}dx = \dot{O}_{x^{3}}^{x^{3}}dx = 1 \dot{O}dx = x + C$$

141. (b) 
$$f(x)^{3} = \frac{\sin^{-1}(x-3)}{\sqrt{9-x^{2}}}$$
 is defined

if (i)-1£x-3£1Þ2£x£4 and

Taking common solution of (i) and (ii), we get 2£x<3

\ Domain = [2, 3)

142. (a) The equations of the lines are

$$p1x + q1y - 1 = 0$$

$$p2x + q2y - 1 = 0$$
 ...(ii)

and p3x +q3y-1= 0 ...(iii)

As they are concurrent,

$$\begin{vmatrix} p_1 & q_1 & -1 \\ p_2 & q_2 & -1 \\ p_3 & q_3 & -1 \end{vmatrix} = 0 \quad P \begin{vmatrix} p_1 & q_1 & 1 \\ p_2 & q_2 & 1 \\ p_3 & q_3 & 1 \end{vmatrix} = 0$$

This is also the condition for the points (p1, q1), (p2, q2) and (p3, q3) to be collinear.

143. (c) Let AB be the chord of length  $\sqrt{\phantom{a}}$  2. Let O be the centre of the circle and let OC be the perpendicular from O on AB.

Then, AC = BC = 
$$\frac{\sqrt{2}}{2} = \frac{1}{\sqrt{2}}$$
  
In DOBC, we have  
OB= BC cosec 45°

$$=\frac{1}{\sqrt{2}}, \sqrt{2}=1$$

144. (b)

\ Area of the circle = p(OB)2 = p sq units

 $\cos A = n \cos B$  and  $\sin A = m \sin B$ 

Squaring and adding, we get

$$1 = n2 \cos 2B + m2 \sin 2B$$

$$(m2 - n2) \sin 2B = 1 - n2$$

145.(a) z1, z2, 0 are vertices of an equilateral triangle, so we have  $\frac{z^2}{1} + \frac{z^2}{2} + 0^2 = z1$  z2 + z2. 0 + 0. z1

$$\Rightarrow z_1^2 + z_2^2 = z$$
  $\Rightarrow z_1^2 + z_2^2 - z_1 z_2^2 = 0$ 

146. (b) Obviously, the relation is not reflexive and transitive, but it is symmetric, because

$$x2 + x2 = 2x2^{1}1$$

and 
$$x^2 + y^2 = 1$$
,  $y^2 + z^2 = 1$ 

$$Þ x2 + z2 = 1$$

But 
$$x^2 + y^2 = 1$$
  $y^2 + x^2 = 1$ 

147. (c) Let *l*, m and n be the direction cosines.

Then,  $l = \cos q$  =  $\cos b$ ,  $n = \cos q$ 

we have 
$$l2 + m2 + n2 = 1$$

$$\triangleright$$
 cos2q + cos2b + cos2q = 1

$$\Rightarrow$$
 2cos2q + 1 - sin2b = 1

$$\Rightarrow$$
 2cos2q - sin2b = 0

$$2\cos 2q - 3\sin 2b = 0$$

$$\stackrel{\text{\'e}}{\approx} \sin^2 b = 3\sin^2 q \left( \text{given} \right)$$

 $P \tan 2q = 2/3$ 

$$\cos^2 q = \frac{1}{1+\tan 2} = \frac{1}{1+2/3} = \frac{3}{5}$$

Given n = 4 and P(X = 0) = 
$$\frac{16}{81}$$

Let p be the probability of success and q that of failure in a trial.

Then, 
$$P(X = 0) = 4C$$

$$0pQ = \frac{16}{81}$$

$$f(x) = f(x) = f(0)$$

$$f(x) = x f(0) + C$$
But  $f(0) = 0$ 

$$C = 0$$
Hence,  $f(x) = x f(0)$ , "xÎR
Clearly,  $f(x)$  is everywhere continuous and differentiable and  $f(x)$  is constant.

"xÎ R

150. (d) Let the coefficients of rth, (r + 1)th, and (r + 2)th terms be in HP.

Then, 
$$\frac{2}{{}^{n}C_{r}} \bar{c}_{r} \frac{1}{{}^{n}C_{r}-1} + \frac{1}{{}^{n}C_{r}+1}$$
 $p = 2 = \frac{n}{{}^{n}C_{r}} = \frac{n C_{r}}{{}^{n}C_{r}+1}$ 
 $p = 2 = \frac{n-r+1}{r} + \frac{r+}{r} = \frac{1}{r}$ 
 $p = n2 - 4nr + 4r2 + n = 0$ 
 $p = (n-2r)2 + n = 0$ 

which is not possible for any value for n.