

MATHEMATICS

1. Let, ρ be the relation on \mathbb{R} (set of all real numbers) defined by $\rho = \{(a,b): a, b \in \mathbb{R}, a^2 + b^2 = 1\}$, then ρ is

- (A) symmetric and transitive
(B) symmetric but neither reflexive nor transitive
(C) transitive but neither reflexive nor symmetric
(D) None of the above

11. Let $\rho = \{(a,b): a, b \in \mathbb{R}, a^2 + b^2 = 1\}$ and $\hat{\rho} = \{(a,b): a, b \in \mathbb{R}, a^2 + b^2 = 1 \text{ and } a \leq b\}$, then $\hat{\rho}$ is

- (A) reflexive and transitive
(B) reflexive and symmetric
(C) transitive and symmetric
(D) reflexive, symmetric and transitive

2. If $[x]$ denotes the greatest integer less than or equal to x , then the range of the function $f(x) = [x] - x$ is

- (A) $[0,1)$ (B) $(-1,0]$
(C) $(-\infty, \infty)$ (D) $(-1,1)$

21. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x) = [x] - x$, where $[x]$ denotes the greatest integer less than or equal to x . Then the range of f is

- (A) $[0,1)$ (B) $(-1,0]$
(C) $(-\infty, \infty)$ (D) $(-1,1)$

3. z is a complex number such that $|z - 1| + |z + 1| \leq 4$. Then z lies in Argand plane

(A) on the boundary and in the interior of an ellipse

(B) on the boundary and in the interior of a circle

(C) in the interior of a hyperbola

(D) None of the above

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(A) on the boundary and in the interior of an ellipse

(B) on the boundary and in the interior of a circle

(C) in the interior of a hyperbola

(D) None of the above

4. Solution of the differential equation $x^2(xdx + ydy) + 2y(xdy - ydx) = 0$, subject to the condition $y(1) = 0$, is

(A) $(x^2 + y^2)(x - 2)^2 = 4x^2$

(B) $(x^2 + y^2)(x + 2)^2 = 9x^2$

(C) $(x^2 - y^2)(x + 2)^2 = 4x^2$

(D) $(x^2 - y^2)(x - 2)^2 = 9x^2$

44. $x^2(xdx + ydy) + 2y(xdy - ydx) = 0$ and $y(1) = 0$ is

(A) $(x^2 + y^2)(x - 2)^2 = 4x^2$

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(C) $(x^2 - y^2)(x + 2)^2 = 4x^2$

(D) $(x^2 - y^2)(x - 2)^2 = 9x^2$

5. In the quadratic equation $ax^2+bx+c=0$, if $\Delta = b^2-4ac$ and $\alpha+\beta$, $\alpha^2+\beta^2$, $\alpha^3+\beta^3$ are in GP, where α, β are the roots of $ax^2+bx+c=0$, then

(A) $\Delta \neq 0$

(B) $b\Delta = 0$

(C) $c\Delta = 0$

(D) $\Delta = 0$

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(B) $b\Delta = 0$

(C) $c\Delta = 0$

(D) $\Delta = 0$

6. The value of $\tan^{-1}\left[\frac{\sin 2-1}{\cos 2}\right]$ is

(A) $\frac{\pi}{2}-1$

(B) $1-\frac{\pi}{4}$

(C) $2-\frac{\pi}{2}$

(D) $\frac{\pi}{4}-1$

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(C) $2-\frac{\pi}{2}$

(D) $\frac{\pi}{4}-1$

7. The mean and standard deviation of 100 observations were found to be 40 and 10 respectively. If at the time of calculation two observations were wrongly taken as 30 and 70 in place of 3 and 27 respectively, then the correct standard deviation is

- (A) 8.24 (B) 9.24
(C) 10.24 (D) 7.24

7ú 100 [i; š™çìòÛ;io¹ KØl; (mean) &α} Î³A; [αW;â;[t; (standard deviation) ð⁰™=àÿû;ì³ 40 &α} 10. ™[f [Òîîα¹ Î³Ú fâ[i; š™çìòÛ;o 30 &α} 70 ëA; ®â;º A;ì¹™=àÿû;ì³ 3 &α} 27 &¹š[¹àìç; ë>*Úà ÒìÚ =àìA; t;àÒìº Î[k;A; Î³A; [αW;â;[t; Òìα

- (A) 8.24 (B) 9.24
(C) 10.24 (D) 7.24

8. The statement $(p \rightarrow r) \vee (q \rightarrow r)$ is logically equivalent to

- (A) $(p \wedge q) \vee r$
(B) $(p \vee q) \rightarrow r$
(C) $(p \wedge q) \rightarrow r$
(D) $(p \rightarrow q) \rightarrow r$

8ú $(p \rightarrow r) \vee (q \rightarrow r)$ l;ü[v;û;[i;¹Î³tâ;º, l;ü[v;û;[i; Òìα

- (A) $(p \wedge q) \vee r$
(B) $(p \vee q) \rightarrow r$
(C) $(p \wedge q) \rightarrow r$
(D) $(p \rightarrow q) \rightarrow r$

- (A) parallel to each other (B) pairwise perpendicular
(C) concurrent (D) not concurrent

(A) ʃ¹ĩĩʃ¹ĩ³à"z¹à° (B) ʃø[tᵢ ᵀᵐᵃK° &ìAᵢ "ʃĩ¹¹ lᵢüʃ¹ °ᵑᵑ

(C) ɦ³[ᵐ@fᵃ (D) ɦ³[ᵐ@fᵃ >ú

- 10ú** $ABC \sin A \sin B = \frac{ab}{c^2} \sin C$, $ABC \sin A \sin B = \frac{ab}{c^2} \sin C$
- (A) $\hat{P}^3 \hat{A} \hat{x}$ (B) $\hat{P}^3 [\hat{A} \hat{x}]$
- (C) $\hat{P}^3 \hat{A} \hat{a} \hat{o} \hat{a}$ (D) $\hat{P}^3 \hat{A} \hat{a} \hat{o} \hat{a}$

- 11** $y = |x|$ and $y = -|x| + 2$ intersect at points A and B. What is the distance between A and B?
- (A) 4 (B) 3 (C) 2 (D) 1

12. If $\begin{vmatrix} x+p & q & r \\ q & x+r & p \\ r & p & x+q \end{vmatrix} = 0$, then the values of x are

(A) $-(p+q+r), \pm \sqrt{p^2+q^2+r^2+pq+qr+rp}$

(B) $\pm(p^2+q^2+r^2), \pm \sqrt{p^2+q^2+r^2+pq+qr+rp}$

(C) $0, \pm(p+q+r)$

(D) $-(p+q+r), \pm \sqrt{p^2+q^2+r^2-pq-qr-rp}$

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(C) $0, \pm(p+q+r)$

(D) $-(p+q+r), \pm \sqrt{p^2+q^2+r^2-pq-qr-rp}$

13. If $y = \{\log_e(x + \sqrt{x^2 + a^2})\}^2$, then $(x^2 + a^2) \frac{d^2y}{dx^2} + x \frac{dy}{dx} = ?$

(A) 2

(B) a^2y

(C) $-a^2y$

(D) -2

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(B) a^2y

(C) $-a^2y$

(D) -2

14. $\int_0^{\pi} \frac{x \tan x}{\sec x + \tan x} dx = ?$

(A) $\frac{\pi}{2} - 1$

(B) $\pi \left[\frac{\pi}{2} + \frac{1}{1} \right]$

(C) $\frac{\pi}{2} + 1$

(D) $\pi \left[\frac{\pi}{2} - \frac{1}{1} \right]$

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(C) $\frac{\pi}{2} + 1$

(D) $\pi \left[\frac{\pi}{2} - \frac{1}{1} \right]$

15. $\int \frac{e^x(x^2 + 1)}{(x + 1)^2} dx = ?$

(A) $e^{\frac{x^2-1}{x+1}} + C$

(B) $e^x \frac{1}{(x + 1)^2} + C$

(C) $e^{\frac{x^2+1}{x-1}} + C$

(D) $e^x \frac{1}{x^2 + 1} + C$

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(D) $e^x \frac{1}{x^2 + 1} + C$

16. If $c_0, c_1, c_2, \dots, c_n$ denote the coefficients in the expansion of $(1+x)^n$, then the value of $c_1 + 2c_2 + 3c_3 + \dots + nc_n$ is

(A) $(n+1)2^{n-1}$

(B) $n2^{n-1}$

(C) $(n+1)2^n$

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(D) $(n+2)2^{n-1}$

17. If $\sec ax + \sec bx = 0$, then the values of x form

(A) two arithmetic progressions

(B) two geometric progressions

(C) one arithmetic progression and one geometric progression

(D) None of the above

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(B) two geometric progressions

(C) one arithmetic progression and one geometric progression

(D) None of the above

18. If the function $f(x) = x^3 + bx^2 + ax + 5$ satisfies Rolle's theorem on $[1, 3]$ with $\epsilon = 2 + \frac{1}{\sqrt{3}}$, then

(A) $a = 11, b = -6$

(B) $a = 11, b = 6$

(C) $a = -11, b = 6$

(D) $a = -11, b = -6$

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(D) $a = -11, b = -6$

19. A function whose graph is symmetrical about y-axis is given by

(A) $f(x) = \log_e(x + \sqrt{x^2 + 1})$

(B) $f(x + y) = f(x) + f(y), \forall x, y \in R$

(C) $f(x) = \cos x + \sin x$

(D) None of the above

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(D) None of the above

20. Let, the variables x_1 and x_2 satisfy the following conditions :

$$\begin{aligned} 3x_1 + x_2 &\leq 15 \\ 3x_1 + 4x_2 &\leq 24 \\ x_1, x_2 &\geq 0 \end{aligned}$$

Then the maximum value of the function $Z=4x_1+3x_2$ is

- (A) 20 (B) 25
(C) 15 (D) 30

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Then the maximum value of the function $Z = 4x_1 + 3x_2$ is

- (A) 20 (B) 25
(C) 15 (D) 30

21. How many 5-digit numbers divisible by 3 can be formed by using the digits 0,1,2,3,4 and 5, without repetition of digits?

- (A) 148 (B) 224
(C) 336 (D) 216

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- (A) 148 (B) 224
(C) 336 (D) 216

22. If $[x]$ denotes the greatest integer less than or equal to x , then $\lim_{x \rightarrow 0} \frac{x[x]}{\sin|x|} = ?$
- (A) 0 (B) 1
(C) Does not exist (D) -1

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- (A) 0 (B) 1
(C) Does not exist (D) -1

23. If $\vec{a} = \hat{i} + \hat{j} + \hat{k}$, $\vec{b} = \hat{i}$ and $\vec{c} = c_1 \hat{i} + 2\hat{j} + c_3 \hat{k}$, then $\vec{a}, \vec{b}, \vec{c}$ will be coplanar for
- (A) $c_1 = 1$ and $c_3 =$ any real number
(B) $c_1 = 2$ and $c_3 = 1$
(C) $c_1 =$ any real number and $c_3 = 1$
(D) $c_1 =$ any real number and $c_3 = 2$

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- (A) $c_1 = 1$ and $c_3 =$ any real number
(B) $c_1 = 2$ and $c_3 = 1$
(C) $c_1 =$ any real number and $c_3 = 1$
(D) $c_1 =$ any real number and $c_3 = 2$

24. The ratio in which the yz plane divides the line joining the points (1,2,3) and (4,5,6) is

- (A) -1:2 (B) -2:5
(C) 2:3 (D) -1:4

24. (1,2,3) ଓ (4,5,6) ରେଖାକୁ yz ଯୋଗୁଥିବା ସମତଳ ଦ୍ଵାରା କେଉଁ ଅନୁପାତରେ ବିଭକ୍ତ କରାଯାଇଛି ?

- (A) -1:2 (B) -2:5
(C) 2:3 (D) -1:4

25. The equation of the plane passing through the line of intersection of the planes $2x+3y-5z+7=0$, $7x-4y+3z-11=0$ and parallel to the line joining the points (3,1,-2) and (1,-2,4) is

- (A) $333x - 124y + 49z - 361 = 0$ (B) $124x - 333y + 49z + 361 = 0$
(C) $49x + 124y + 331z + 61 = 0$ (D) $330x + 120y + 40z + 361 = 0$

25. $2x+3y-5z+7=0$ ଓ $7x-4y+3z-11=0$ ଦ୍ଵାରା ଗଠିତ ରେଖା ଦ୍ଵାରା ଗୁଚ୍ଛିତ ସମତଳର ସମୀକରଣ ଯଦି ଏହା (3,1,-2) ଓ (1,-2,4) ଦ୍ଵାରା ଗଠିତ ରେଖା ସହ ସମାନ୍ତର ହୁଏ ତେବେ ସମତଳର ସମୀକରଣ କେଉଁଟି ହେବ ?

- (A) $333x - 124y + 49z - 361 = 0$ (B) $124x - 333y + 49z + 361 = 0$
(C) $49x + 124y + 331z + 61 = 0$ (D) $330x + 120y + 40z + 361 = 0$

26. Two positive numbers x and y are such that $x^2 + y^2 = a^2$, ($a > 0$). Then the sum $x+y$ will be maximum when

- (A) $x = \frac{a}{\sqrt{2}}, y = \frac{a}{\sqrt{2}}$ (B) $x = a, y = a$
(C) $x = a, y = \frac{a}{2}$ (D) $x = \frac{a}{\sqrt{2}}, y = a$

26. ଧନାତ୍ମକ ସଂଖ୍ୟା x ଓ y ଯେପରିକି $x^2 + y^2 = a^2$, ($a > 0$) ଉପରେ ଥାନ୍ତି । ତେବେ $x+y$ ର ସର୍ବାଧିକ ମୂଲ୍ୟ ପାଇଁ x ଓ y ର ମୂଲ୍ୟ କେଉଁଟି ହେବ ?

- (A) $x = \frac{a}{\sqrt{2}}, y = \frac{a}{\sqrt{2}}$ (B) $x = a, y = a$
(C) $x = a, y = \frac{a}{2}$ (D) $x = \frac{a}{\sqrt{2}}, y = a$

27. If the straight lines $ax+y+1=0$, $x+by+1=0$, $x+y+c=0$ (a, b, c are unequal and $\neq 1$) are concurrent, then $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = ?$

(A) 0

(B) 2

(C) 1

(D) None of the above

27. If the straight lines $ax+y+1=0$, $x+by+1=0$, $x+y+c=0$ (a, b, c are unequal and $\neq 1$) are concurrent, then $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = ?$

(A) 0

(B) 2

(C) 1

(D) None of the above

28. The equations of tangents to the hyperbola $3x^2 - y^2 = 3$ parallel to the straight line $2x - y + 4 = 0$ are

(A) $y = 2x \pm 3$

(B) $y = 2x \pm 1$

(C) $y = 2x \pm 2$

(D) $y = 2x \pm 5$

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(B) $y = 2x \pm 1$

(C) $y = 2x \pm 2$

(D) $y = 2x \pm 5$

29. Two variable straight lines $ax \cos \alpha + by \sin \alpha = a$ and $ax \sin \alpha - by \cos \alpha = b$, ($b > a > 0$) intersect at the point P , α being a parameter. Then the locus of P is an ellipse with eccentricity

(A) $\frac{\sqrt{b^2 - a^2}}{a}$

(B) $\frac{\sqrt{b^2 - a^2}}{b}$

(C) $\sqrt{\frac{b^2 - a^2}{b^2 + a^2}}$

(D) None of the above

29. $ax \cos \alpha + by \sin \alpha = a$ and $ax \sin \alpha - by \cos \alpha = b$, ($b > a > 0$) intersect at the point P , α being a parameter. Then the locus of P is an ellipse with eccentricity

(A) $\frac{\sqrt{b^2 - a^2}}{a}$

(B) $\frac{\sqrt{b^2 - a^2}}{b}$

(C) $\sqrt{\frac{b^2 - a^2}{b^2 + a^2}}$

(D) None of the above

30. Let, A is a 3×3 matrix and B is its adjoint matrix. If $|B| = 144$, then $|A| = ?$

(A) ± 2

(B) ± 12

(C) ± 8

(D) ± 48

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(A) ± 2

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(D) ± 48